## CBSE Test Paper 01 Chapter 6 Triangles

- **1.** In an isosceles triangle ABC if AC = BC and  $AB^2 = 2AC^2$  then the measure of  $\angle C$  is (1)
  - a. 90<sup>0</sup>
  - b. 45<sup>o</sup>
  - c. 60<sup>0</sup>
  - d. 30<sup>0</sup>
- 2. In the given figure XY || BC. If AX = 3cm, XB = 1.5cm and BC = 6cm, then XY is equal to (1)



- 3. What will be the length of the hypotenuse of an isosceles right triangle whose one side is  $4\sqrt{2}\ cm$  (1)
  - a.  $12\sqrt{2} \ cm$ .
  - b. 12 cm.
  - c. 8 cm.
  - d.  $8\sqrt{2}cm$ .

4. In the given figure, if  $\frac{ar(\Delta ALM)}{ar(trapezium \ LMCB)} = \frac{9}{16}$ , and LM||BC, Then AL:LB is equal to





- b. 4:1
- c. 3:4
- d. 2:3
- **5.** In the following figure AD : DB = 1 : 3, AE : EC = 1 : 3 and BF : FC = 1 : 4, then **(1)** 
  - a. AD||FC. b. AD||FE. c. DE||BC. d. AE||DF.
- 6. In the given figure, ST || RQ, PS = 3 cm and SR = 4 cm. Find the ratio of the area of  $\triangle$  PST to the area of  $\triangle$  PRQ. (1)



7. If D and E are points on the sides AB and AC respectively of  $\triangle ABC$  such that AB = 5.6 cm, AD = 1.4 cm, AC = 7.2 cm and AE = 1.8 cm, show that DE ||BC. (1)



- **8.** A ladder is placed in such a way that its foot is at a distance of 5 m from a wall and its tip reaches a window 12 m above the ground. Determine the length of the ladder. **(1)**
- 9. Triangles ABC and DEF are similar. If AC = 19 cm and DF = 8 cm, find the ratio of the area of two triangles. (1)
- 10. In the given figure, DE  $\parallel$  BC.



Find AD. (1)

11. In  $\triangle$ ABC, X is any point on AC. If Y, Z, U and V are the middle points on AX, XC, AB and BC respectively, then prove that UY || VZ and UV || YZ.



- 12. If the angles of one triangle are respectively equal to the angles of another triangle, Prove that the ratio of their corresponding sides is the same as the ratio of their corresponding angle bisectors. (2)
- **13.** In a  $\triangle$ ABC, D and E are points on the sides AB and AC respectively such that DE || BC. If AD = x, DB = x-2, AE = x + 2 and EC = x - 1, find the value of x. (2)
- 14. A man goes 10m due south and then 24m due west. How far is he from the starting point? (3)
- 15. In the given figure A, B and C are points on OP, OQ and OR respectively such that AB  $\parallel$  PQ and AC  $\parallel$  PR. Prove that BC  $\parallel$  QR.



- 16. In a  $\Delta ABC$ , D and E are points on the sides AB and AC respectively such that DE || BC. If AD = 8x 7, DB = 5x 3, AE = 4x 3 and EC = (3x 1), find the value of x. (3)
- **17.** In Fig. find ∠F. **(3)**



- 18. Prove that ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides. (4)
- **19.** In a trapezium ABCD, AB | | DC and DC = 2AB. EF | | AB, where E and F lie on BC and AD respectively such that  $\frac{BE}{EC} = \frac{4}{3}$  Diagonal DB intersects EF at G. Prove that, 7EF = 11AB. **(4)**
- **20.** In a triangle, if the square of one side is equal to the sum of the squares on the other two sides. Prove that the angle opposite to the first side is a right angle. Use the above theorem to find the measure of  $\angle$  PKR in the figure given below. **(4)**



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## Solution

1. a. 90<sup>o</sup>

**Explanation:** Given:  $AB^2 = 2AC^2$   $\Rightarrow AB^2 = AC^2 + AC^2$   $\Rightarrow AB^2 = AC^2 + BC^2$  [Given: AC = BC]  $\therefore \Delta ABC$  is a right angled triangle, by converse of Pythagoras theorem Now, since  $\Delta ABC$  is an isosceles triangle also. Therefore, its two sides are equal i.e., AC = BC Therefore, AB is hypotenuse.  $\therefore \angle C$  is a right angle i.e.,  $90^\circ$ 

2. d. 4 cm.

**Explanation:** Since XY||BC, then using Thales theorem,

$$\Rightarrow \frac{AX}{AB} = \frac{XY}{BC}$$
$$\Rightarrow \frac{3}{4.5} = \frac{XY}{6}$$
$$\Rightarrow XY = 4 \text{ cm}$$

3. c. 8 cm.

**Explanation:** Let AC be hypotenuse. Its equal sides are AB and BC and AB = BC =  $4\sqrt{2}$ cm.

Using Pythagoras Theorem,

$$AC^{2} = AB^{2} + BC^{2}$$
  

$$\Rightarrow AC^{2} = (4\sqrt{2})^{2} + (4\sqrt{2})^{2} = 32 + 32 = 64 \text{ cm}^{2}$$
  

$$\Rightarrow AC = 8 \text{ cm}$$

4. b. 4 : 1

 $\begin{array}{l} \textbf{Explanation: In } \Delta ALM \text{ and } \Delta ABC, \ \angle A = \ \angle A \ [Common] \\ \ \angle ALM = \ \angle ABC \ [Corresponding angles as LM \ |BC] \end{array}$ 

$$\therefore \Delta ALM \sim \Delta ABC \text{ [AA similarity]}$$
  

$$\therefore \frac{\operatorname{ar}(\Delta ALM)}{\operatorname{ar}(\Delta ABC)} = \frac{AL^2}{AB^2} \text{ Now, } \frac{\operatorname{ar}(\operatorname{trap.LMCB})}{\operatorname{ar}(\Delta ALM)} = \frac{9}{16}$$
  

$$\Rightarrow \frac{\operatorname{ar}(\Delta ABC) - \operatorname{ar}(\Delta ALM)}{\operatorname{ar}(\Delta ALM)} = \frac{9}{16}$$
  

$$\Rightarrow \frac{\operatorname{ar}(\Delta ABC)}{\operatorname{ar}(\Delta ALM)} - 1 = \frac{9}{16}$$
  

$$\Rightarrow \frac{\operatorname{ar}(\Delta ABC)}{\operatorname{ar}(\Delta ALM)} = \frac{9}{16} + 1$$
  

$$\Rightarrow \frac{\operatorname{ar}(\Delta ABC)}{\operatorname{ar}(\Delta ALM)} = \frac{25}{16}$$
  

$$\Rightarrow \frac{AB^2}{AL^2} = \frac{25}{16}$$
  

$$\Rightarrow \frac{AB}{AL} = \frac{5}{4}$$
  
Let AB = 5x and AL = 4x then LB = AB - AL = 5x - 4x = 1x  

$$\therefore \frac{AL}{LB} = \frac{4x}{1x} = \frac{4}{1}$$
  

$$\Rightarrow AL : LB = 4 : 1$$

5. c. DE||BC.

**Explanation:** Given:  $\frac{AD}{DB} = \frac{1}{3}$  and  $\frac{AE}{EC} = \frac{1}{3}$ Therefore, in  $\triangle ABC$ ,  $\frac{AD}{DB} = \frac{AE}{EC}$  $\therefore DE |BC$  [Using Thales Theorem] Here we are not considering BF : FC =1 : 4.

6. PS = 3 cm, SR = 4 cm and ST || RQ.



PR = PS + SR= 3 + 4 = 7 cm

In  $\triangle$  PST and  $\triangle$  PRQ

 $\angle$ SPT  $\cong \angle$ RPQ (common angle)

 $\angle PST \cong \angle PRQ$  (Alternate angle)

 $riangle \mathsf{PST} \sim riangle \mathsf{PRQ}$  (AA configuration)

 $\frac{\operatorname{ar} \Delta PST}{\operatorname{ar} \Delta PQR} = \frac{PS^2}{PR^2} = \frac{3^2}{7^2} = \frac{9}{49}$ 

Hence required ratio = 9 : 49.

7. Given: AB = 5.6 cm, AD = 1.4 cm, AC = 7.2 cm and AE = 1.8 cm  $\therefore \frac{AD}{AB} = \frac{1.4}{5.6} = \frac{1}{4}$  and  $\frac{AE}{AC} = \frac{1.8}{7.2} = \frac{1}{4}$ 

Hence, by the converse of Thales' theorem,  $DE \| BC$ .

8. Let AC be the ladder, AB be the wall and BC be the distance of ladder from the foot of the wall.

In right  $\triangle ABC$ ,



9. We have,

 $\Delta$ abc ~  $\Delta$ def

AC = 19 cm and DF = 8 cm

By area of similar triangle theorem

$$\frac{Area(\Delta ABC)}{Area(\Delta DEF)} = \frac{AC^2}{DF^2} = \frac{(19)^2}{8^2} = \frac{361}{64}$$

10. : DE || BC

$$\therefore \quad \frac{\text{AD}}{\text{BD}} = \frac{\text{AE}}{\text{CE}} \text{ (from BPT)}$$
  
$$\Rightarrow \quad \frac{\text{AD}}{7.2} = \frac{1.8}{5.4} \Rightarrow \text{AD} = 2.4 \text{ cm}$$

11. Join BX

In ABX, U is midpoint of AB and Y is mid-point AX (given)

.... UY || BX (using mid-point theorem) ..... (i)



In BCX, v is mid-point of BC and z is mid-point of XC

VZ || BX ..(ii)

from (i) and (ii)

UY || VZ

In ABC, U is mid-point of AB and V is mid-point of BE.

- .:. UV || AC
- $\Rightarrow$  UV || YZ Hence proved.

E



Given: Two triangles ABC and DEF in which  $\angle A = \angle D$ ,  $\angle B = \angle E$  and  $\angle C = \angle F$ , AL and DM are angle bisectors of  $\angle A$ and  $\angle D$  respectively To prove:  $\frac{BC}{EF} = \frac{AL}{DM}$ Proof: Triangle ABC and DEF are Similar.  $\Rightarrow \frac{AB}{DE} = \frac{BC}{EF}$  ......(i) In  $\triangle$  ABL and  $\triangle$  DEM, we have  $\angle B = \angle E$  [Given]  $\angle$  BAL=  $\angle$  EDM [ $\because \angle A = \angle D \Rightarrow \frac{1}{2} \angle A = \frac{1}{2} \angle D$ ]  $\Rightarrow \triangle$  ABL  $\sim \triangle$  DEM [AA similarity]  $\Rightarrow \frac{AB}{DE} = \frac{AL}{DM}$  ......(ii)

From (i) and (ii) we have

$$\frac{BC}{EF} = \frac{AL}{DM}$$

13. We have,



## DE || BC

Therefore, by basic proportionality theorem,

We have,  

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{x}{x-2} = \frac{x+2}{x-1}$$

$$\Rightarrow x(x-1) = (x+2)(x-2)$$

$$\Rightarrow x^2 - x = x^2 - (2)^2 [\because (a-b)(a+b) = a^2 - b^2]$$

$$\Rightarrow -x = -4$$

$$\Rightarrow x = 4 \text{ cm.}$$

14. Starting from O, let the man goes from O to A and then A to B as shown in the figure. Then,

Using Pythagoras theorem:

$$OB^2 = OA^2 + AB^2$$

 $\Rightarrow OB^{2} = 10^{2} + 24^{2}$  $\Rightarrow OB^{2} = 100 + 576$  $\Rightarrow OB^{2} = 676$  $\Rightarrow OB = \sqrt{676} = 26m$ 

Hence, the man is 26m south-west from the starting position.

15. Proof : In  $\triangle POQ, AB || PQ$ ,(Given)  $\frac{AO}{AP} = \frac{OB}{BQ}$ .....(i) (BPT) In  $\triangle$ OPR AC || PR  $\frac{OA}{AP} = \frac{OC}{CR}$ ....(ii) From eqn (I) and (ii)  $\frac{OB}{BQ} = \frac{OC}{CR}$ Hence BC || QR (By converse of BPT)

16. We have,

(8x-7) (8x-7) (4x-3) E (5x-3) (3x1) C

We are given that, DE || BC

Therefore, by thales theorem,

We have,  

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{8x-7}{5x-3} = \frac{4x-3}{3x-1}$$

$$\Rightarrow (8x - 7)(3x - 1) = (4x - 3)(5x - 3)$$

$$\Rightarrow 24x^{2} - 8x - 21x + 7 = 20x^{2} - 12x - 15x + 9$$

$$\Rightarrow 24x^{2} - 20x^{2} - 29x + 27x + 7 - 9 = 0$$

$$\Rightarrow 4x^{2} - 2x - 2 = 0$$

 $\Rightarrow 2[2x^2 - x - 1] = 0$   $\Rightarrow 2x^2 - x - 1 = 0$   $\Rightarrow 2x^2 - 2x + 1x - 1 = 0$   $\Rightarrow 2x(x - 1) + 1(x - 1) = 0$   $\Rightarrow (2x + 1)(x - 1) = 0$   $\Rightarrow 2x + 1 = 0 \text{ or } x - 1 = 0$   $\Rightarrow x = -\frac{1}{2} \text{ or } x = 1$   $x = -\frac{1}{2} \text{ is not possible.}$  $\therefore x = 1.$ 

- 17. In triangles ABC and DEF, we have  $\frac{AB}{DF} = \frac{BC}{FE} = \frac{CA}{ED} = \frac{1}{2}$ Therefore, by SSS-criterion of similarity, we have  $\Delta ABC \sim \Delta DFE$   $\Rightarrow \angle A = \angle D, \angle B = \angle F \text{ and } \angle C = \angle E$   $\Rightarrow \angle D = 80^{\circ}, \angle F = 60^{\circ}$ Hence,  $\angle F = 60^{\circ}$ .
- 18. Given :  $\Delta ABC \sim \Delta PQR$

To Prove : 
$$\frac{\operatorname{ar}(\Delta ABC)}{\operatorname{ar}(\Delta PQR)} = \left(\frac{AB}{PQ}\right)^2 = \left(\frac{BC}{QR}\right)^2 = \left(\frac{AC}{PR}\right)^2$$
  
Construction: Draw AD  $\perp$  BC and PE  $\perp$  OR

Proof :



 $\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$  (Ratio of corresponding sides of similar triangles are equal) ...(i)  $\angle B = \angle Q$  (Corresponding angles of similar triangles) ......(ii) In  $\triangle ADB$  and  $\triangle PEQ$   $\angle B = \angle Q$  (From (ii))  $\angle ADB = \angle PEQ$  [each 90°]  $\therefore \triangle ADB \sim \triangle PEQ$  [By AA criteria]  $\Rightarrow \frac{AD}{PE} = \frac{AB}{PQ}$  (Corresponding sides of similar triangles) ...(iii)

From equation (i) and equation (iii)

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} = \frac{AD}{PE} \dots \text{(iv)}$$

$$\frac{\operatorname{ar}(\Delta ABC)}{\operatorname{ar}(\Delta PQR)} = \frac{\frac{1}{2} \times BC \times AD}{\frac{1}{2} \times QR \times PE}$$

$$= \left(\frac{BC}{QR}\right) \times \left(\frac{AD}{PE}\right)$$

$$\left(\frac{AD}{PE} = \frac{BC}{QR}\right)$$

$$= \frac{BC}{QR} \times \frac{BC}{QR}$$

$$\Rightarrow \frac{ar(\Delta ABC)}{ar(\Delta PQR)} = \frac{BC^{2}}{QR^{2}} \dots \text{(v) [from eq. (iv)]}$$

From equation (iv) and equation (v),

$$\therefore \frac{\operatorname{ar}(\Delta ABC)}{\operatorname{ar}(\Delta PQR)} = \left(\frac{AB}{PQ}\right)^2 = \left(\frac{BC}{QR}\right)^2 = \left(\frac{AC}{PR}\right)^2$$

: Ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.

$$F \xrightarrow{G} G$$

19.

In a trapezium ABCD, AB|| DC ,. EF || AB and CD=2AB  
and also 
$$\frac{BE}{EC} = \frac{4}{3}$$
 ------(1)  
AB || CD and AB || EF  
 $\therefore \frac{AF}{FD} = \frac{BE}{EC} = \frac{4}{3}$   
In  $\triangle BGE$  and  $\triangle BDC$   
 $\angle BEG = \angle BCD$  ( $\because$  corresponding angles)  
 $\angle GBE = \angle DBC$  (Common)  
 $\therefore \triangle BGE \sim \triangle BDC$  [ By AA similarity]  
 $\Rightarrow \frac{EG}{CD} = \frac{BE}{BC}$  ------(2)  
Now, from (1)  $\frac{BE}{EC} = \frac{4}{3}$   
 $\Rightarrow \frac{EC}{BE} = \frac{3}{4}$   
 $\Rightarrow \frac{EC}{BE} + 1 = \frac{3}{4} + 1$ 

$$\Rightarrow \frac{EC+BE}{BE} = \frac{7}{4}$$

$$\Rightarrow \frac{BC}{BE} = \frac{7}{4} \text{ or } \frac{BE}{BC} = \frac{4}{7}$$
from equation (2),  $\frac{EG}{CD} = \frac{4}{7}$ 
so  $EG = \frac{4}{7}CD \dots$ (3)
Similarly,  $\Delta DGF \sim \Delta DBA$  (by AA similarity)
$$\Rightarrow \frac{DF}{DA} = \frac{FG}{AB}$$

$$\Rightarrow \frac{FG}{AB} = \frac{3}{7}$$

$$\Rightarrow FG = \frac{3}{7}AB \dots$$
(4)
$$\begin{bmatrix} \because \frac{AF}{AD} = \frac{4}{7} = \frac{BE}{BC} \\ \Rightarrow \frac{EC}{BC} = \frac{3}{7} = \frac{DE}{DA} \end{bmatrix}$$
Adding equations (3) and (4), we get,
 $EG + FG = \frac{4}{7}CD + \frac{3}{7}AB$ 

$$\Rightarrow EF = \frac{4}{7} \times (2AB) + \frac{3}{7}AB$$

$$= \frac{8}{7}AB + \frac{3}{7}AB = \frac{11}{7}AB$$

$$\therefore \ 7EF = 11AB$$
20.

i. Given: In  $\triangle$  ABC such that

$$AC^2 = AB^2 + BC^2$$

To prove: Triangle ABC is right angled at B

Construction: Construct a triangle DEF such that

DE = AB, EF = BC and  $\angle E = 90^\circ$ 

Proof:  $\therefore$  DEF is a right angled triangle right angled at E [construction]

... By Pythagoras theorem, we have  

$$DF^2 = DE^2 + EF^2$$
  
 $\Rightarrow DF^2 = AB^2 + BC^2$  [  $\therefore$  DE = AB and EF = BC]

 $\Rightarrow$  DF<sup>2</sup> = AC<sup>2</sup>[ $\therefore$  AB<sup>2</sup> + BC<sup>2</sup> = AC<sup>2</sup>]  $\Rightarrow$  DF = AC Thus, in  $\triangle$  ABC and  $\triangle$  DEF, we have AB = DEBC = EFand AC = DF [By Construction and (i)]  $\therefore \triangle ABC \cong \triangle DEF (SSS)$  $\Rightarrow \angle B = \angle E = 90^{\circ}$ Hence,  $\triangle$  ABC is a right triangle. ii. In  $\triangle$  QPR ,  $\angle$  QPR = 90°  $\Rightarrow 24^2 + x^2 = 26^2$  $\Rightarrow$  x = 10  $\Rightarrow$  PR = 10 cm Now in  $\triangle$  PKR, PR<sup>2</sup> = PK<sup>2</sup> + KR<sup>2</sup>[as  $10^2 = 8^2 + 6^2$ ] . PKR is right angled at K  $\Rightarrow \angle PKR = 90^{\circ}$