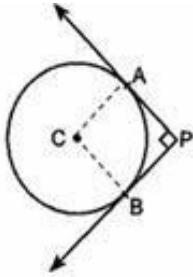


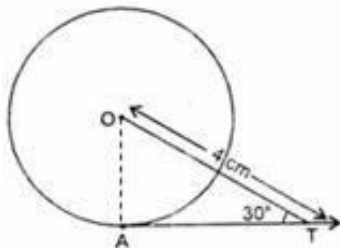
CBSE Test Paper 03

Chapter 10 Circle

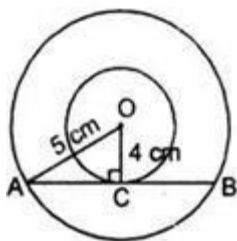
1. In the given figure, the pair of tangents A to a circle with centre O are perpendicular to each other and length of each tangent is 5 cm, then the radius of the circle is : **(1)**



- a. 2.5 cm
b. 5 cm
c. 7.5 cm
d. 10 cm
2. In the given figure, AT is a tangent to the circle with centre O such that $OT = 4$ cm and $\angle OTA = 30^\circ$. Then AT is equal to: **(1)**



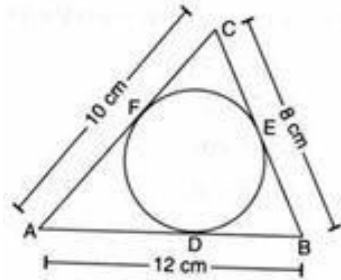
- a. 2 cm
b. $2\sqrt{3}$ cm
c. 4 cm
d. $4\sqrt{3}$ cm
3. If radii of two concentric circles are 4 cm and 5 cm, then the length of the chord of one circle which is tangent to the other circle is: **(1)**



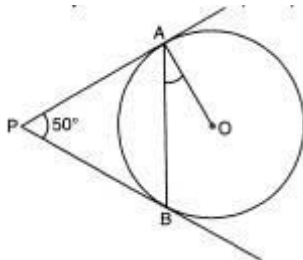
- a. 9 cm

- b. 3 cm
- c. 1 cm
- d. 6 cm

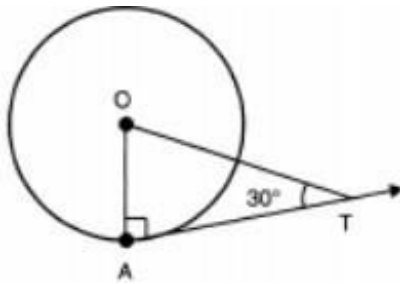
4. A circle is inscribed in $\triangle ABC$ having sides 8 cm, 10 cm and 12 cm as shown in the figure. Then the measure of AD and BE are... **(1)**



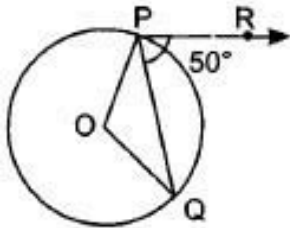
- a. AD = 8 cm, BE = 5 cm.
 - b. AD = 8 cm, BE = 6 cm
 - c. AD = 5 cm, BE = 7 cm
 - d. AD = 7 cm, BE = 5 cm
5. PQ is a tangent drawn from a point P to a circle with centre O and QOR is a diameter of the circle such $\angle POR = 120^\circ$, then $\angle OPQ$ is **(1)**
- a. 60°
 - b. 35°
 - c. 30°
 - d. 45°
6. At which point a tangent is perpendicular to the radius? **(1)**
7. In fig., PA and PB are tangents to the circle with centre O such that $\angle APB = 50^\circ$. Write the measure of $\angle OAB$ **(1)**



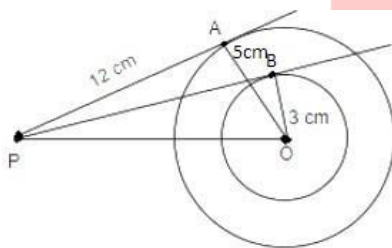
8. In given figure, if AT is a tangent to the circle with centre O, such that $OT = 4$ cm and $\angle OTA = 30^\circ$, then find the length of AT (in cm). **(1)**



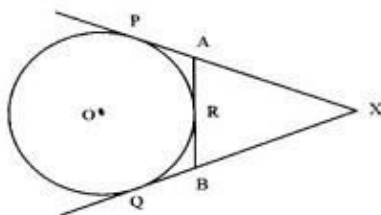
9. In figure, if O is the centre of a circle, PQ is a chord and the tangent PR at P makes an angle of 50° with PQ. Find $\angle POQ$. **(1)**



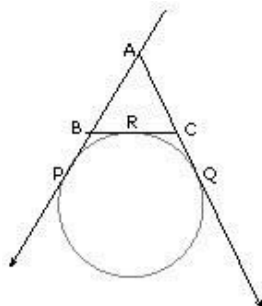
10. Two concentric circles with centre O are of radii 5 cm and 3 cm. From an external point P, two tangents PA and PB are drawn to these circles, respectively. If PA = 12 cm, then find the length of PB **(1)**



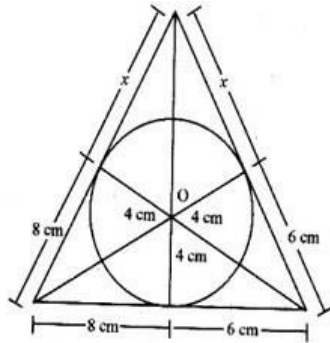
11. A quadrilateral ABCD is drawn to circumscribe a circle. Prove that $AB + CD = AD + BC$. **(2)**
12. In given Fig. XP and XQ are tangents from X to the circle with centre O. R is a point on the circle. Prove that $XA + AR = XB + BR$. **(2)**



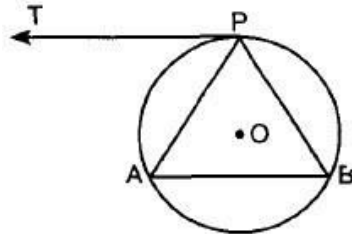
13. In the given figure, find the perimeter of ABC, if AP = 10 cm. **(2)**



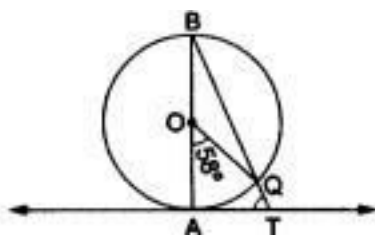
14. Prove that parallelogram circumscribing a circle is a rhombus. (3)
15. The radius of the incircle of a triangle is 4 cm and the segment into which one side is divided by the point of contact are 6 cm and 8 cm. Determine the other two sides of the triangle. (3)



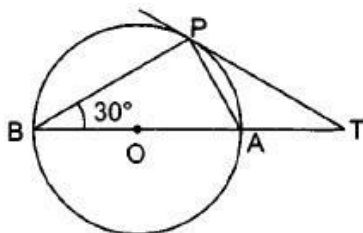
16. A tangent PT is drawn parallel to a chord AB as shown in figure. Prove that APB is an isosceles triangle. (3)



17. A chord PQ of a circle is parallel to the tangent drawn at a point R of the circle. Prove that R bisects the arc PRQ. (3)
18. In the given figure, AB is the diameter of a circle with centre O and AT is a tangent. If $\angle AOQ = 58^\circ$, find $\angle ATQ$. (4)



19. In figure, O is the centre of the circle and TP is the tangent to the circle from an external point T. If $\angle PBT = 30^\circ$, prove that $BA : AT = 2 : 1$. (4)



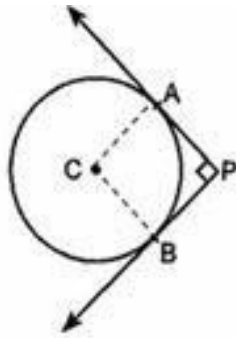
20. If from an external point B of a circle with centre 'O', two tangents BC, BD are drawn such that $\angle DBC = 120^\circ$, prove that $BC + BD = BO$, i.e., $BO = 2BC$. (4)

CBSE Test Paper 03
Chapter 10 Circle

Solution

1. b. 5 cm

Explanation:



Construction: Joined OA and OB.

Here $OA \perp AP$ and $OB \perp BP$ and $PA \perp PB$

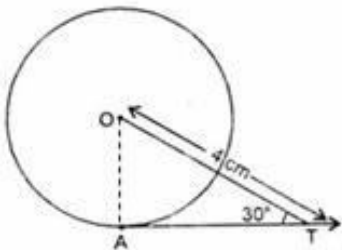
Also $AP = PB$

Therefore, APBO is a square.

$\Rightarrow AP = OA = OB = 5 \text{ cm}$

2. b. $2\sqrt{3} \text{ cm}$

Explanation: Construction: Joined OA.



Since OA is perpendicular to AT, then

$\angle OAT = 90^\circ$ In right angled triangle OAT

$$\cos 30^\circ = \frac{AT}{OT} \Rightarrow$$

$$\frac{\sqrt{3}}{2} = \frac{AT}{4} \Rightarrow AT = 2\sqrt{3} \text{ cm}$$

3. d. 6 cm

Explanation: Here OC is perpendicular to AB.

Then OC bisects AB i.e., $AC = BC$

Now, in triangle OAC, $OA^2 = AC^2 + OC^2$

$$\Rightarrow (5)^2 = AC^2 + (4)^2 \Rightarrow AC^2 = 25 - 16$$

$$\Rightarrow AC = 3 \text{ Therefore, length of tangent } AB = AC + BC = 3 + 3 = 6 \text{ cm}$$

4. d. AD = 7 cm, BE = 5 cm

Explanation: Let AD = x and BE = y

$$\therefore BD = 12 - x \Rightarrow BE = y$$

But BD = BE (Tangents to a circle from an external point B)

$$\Rightarrow y = 12 - x \Rightarrow x + y = 12 \dots\dots\dots (i)$$

$$\text{Also, } AF = x$$

$$\text{and } CF = 10 - x$$

$$\text{and } CE = 8 - y$$

$$\therefore 10 - x = 8 - y$$

$$x - y = 2 \dots\dots\dots (ii)$$

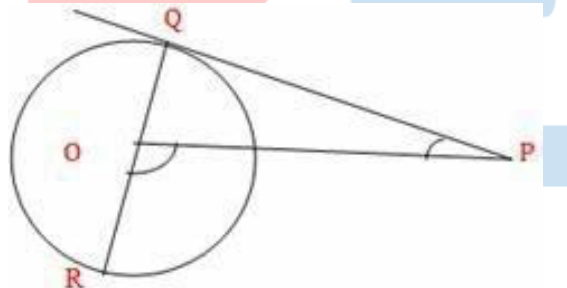
On solving eq. (i) and (ii), we get

$$x = 7 \text{ and } y = 5$$

Therefore AD = 7 cm and BE = 5 cm

5. c. 30°

Explanation:



Here $\angle PQO = 90^\circ$ Since, $\angle QOR = 120^\circ$

$$\therefore \angle POQ + \angle POR = 180^\circ$$

$$\Rightarrow \angle POQ + 120^\circ = 180^\circ$$

$$\Rightarrow \angle POQ = 60^\circ$$

Now, in triangle OPQ,

$$\angle OPQ + \angle PQO + \angle QOP = 180^\circ$$

$$\Rightarrow \angle OPQ + 90^\circ + 60^\circ = 180^\circ$$

$$\Rightarrow \angle OPQ = 30^\circ$$

6. A line which intersects a circle at any one point is called the tangent. The tangent at any point of a circle is perpendicular to the radius through the all point of contact.

7. Here, $\angle APB = 50^\circ$

$$\angle PAB = \angle PBA = \frac{180^\circ - 50^\circ}{2} = 65^\circ$$

$$\angle OAB = 90^\circ - \angle PAB$$

$$= 90^\circ - 65^\circ = 25^\circ$$

8. In given figure, AT is a tangent to the circle with centre O, such that OT = 4 cm and

$\angle OTA = 30^\circ$, then we have to find the length of AT (in cm).

$$\cos \theta = \frac{\text{Base}}{\text{Hypotenuse}}$$

$$\frac{AT}{OT} = \cos 30^\circ$$

$$\therefore AT = OT \cos 30^\circ$$

$$\text{or, } AT = 4 \times \frac{\sqrt{3}}{2}$$

$$= 2\sqrt{3}\text{cm}$$

9. $OP \perp PR$ [\because Tangent and radius are \perp to each other at the point of contact]

$$\angle OPQ = 90 - 50 = 40$$

$$OP = OQ \text{ [By isosceles triangle's property]}$$

$$\angle OPQ = \angle OQP = 40$$

In $\triangle OPQ$,

$$\Rightarrow \angle O + \angle P + \angle Q = 180^\circ$$

$$\Rightarrow \angle O + 40 + 40 = 180$$

$$\angle O = 180 - 80 = 100$$

10. Two concentric circles with centre O are of radii 5 cm and 3 cm. From an external point P, two tangents PA and PB are drawn to these circles, respectively. If PA = 12 cm, then we have to find the length of PB.

We know that radius is perpendicular to the tangent at the point of contact therefore, $AO \perp AP$.

Now, in right-angled triangle PAO, $\angle PAO = 90^\circ$

$$OP^2 = (PA)^2 + (AO)^2 \text{ [by Pythagoras theorem]}$$

$$\Rightarrow OP = \sqrt{(PA)^2 + (AO)^2}$$

$$\Rightarrow OP = \sqrt{169} = 13 \text{ cm}$$

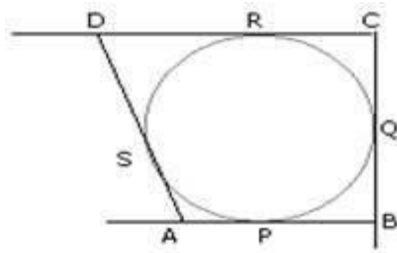
Similarly, in right-angled triangle PBO, $\angle PBO = 90^\circ$

$$PO^2 = (PB)^2 + (OB)^2 \text{ [by Pythagoras theorem]}$$

$$\Rightarrow PB = \sqrt{(OP)^2 - (OB)^2}$$

$$\Rightarrow PB = \sqrt{(13)^2 - (3)^2} = \sqrt{160} = 4\sqrt{10} \text{ cm } [\because \text{radius, } OB = 3 \text{ cm, given}]$$

11.



\therefore AP, AS are tangents from a point A (Outside the circle) to the circle.

$$\therefore AP = AS$$

Similarly BP = BQ

$$CQ = CR$$

$$DR = DS$$

$$\text{Now } AB + CD = AP + PB + CR + RD$$

$$= AS + BQ + CQ + DS$$

$$= (AS + DS) + (BQ + CQ)$$

$$= AD + BC$$

$$AB + CD = AD + BC$$

12. Since the lengths of tangents from an exterior point to a circle are equal.

$$\therefore XP = XQ \dots\dots\dots (i)$$

$$AP = AR \dots\dots\dots (ii)$$

$$BQ = BR \dots\dots\dots (iii)$$

$$\text{Now } XP = XQ \text{ i.e. } XA + AP = XB + BQ$$

$$\Rightarrow XA + AR = XB + BR$$

Hence proved.

13. \therefore BC touches the circle at R

\therefore Tangents drawn from external point to the circle are equal.

$$\therefore AP = AQ, BR = BP$$

$$\text{And } CR = CQ$$

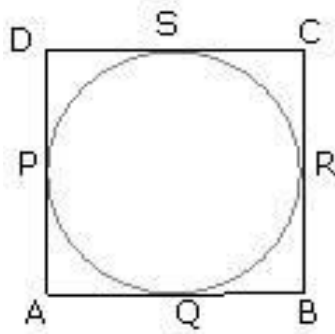
$$\therefore \text{Perimeter of } \triangle ABC = AB + BC + AC$$

$$= AB + (BR + RC) + AC$$

$$= AB + BP + CQ + AC$$

$$= AP + AQ = 2AP = 2 \times 10 = 20 \text{ cm}$$

14.



Given ABCD is a parallelogram in which all the sides touch a given circle

To prove:- ABCD is a rhombus

Proof:-

\therefore ABCD is a parallelogram

\therefore AB = DC and AD = BC

Again AP, AQ are tangents to the circle from the point A

\therefore AP = AQ

Similarly, BR = BQ

CR = CS

DP = DS

\therefore (AP + DP) + (BR + CR) = AQ + DS + BQ + CS = (AQ + BQ) + (CS + DS)

\Rightarrow AD + BC = AB + DC

\Rightarrow BC + BC = AB + AB [\because AB = DC, AD = BC]

\Rightarrow 2BC = 2AB

\Rightarrow BC = AB

Hence, parallelogram ABCD is a rhombus

15. Equate the areas of the triangle formed by using the formula

$\sqrt{s(s-a)(s-b)(s-c)}$ and also found by dividing it into three triangles.

Let the length of tangent from third vertex = x.

Then the sides of triangle are 14, x + 6, x + 8

$$\therefore s = \frac{14+x+6+x+8}{2} = \frac{28+2x}{2} = 14 + x$$

$$\therefore \sqrt{(14+x)(14+x-x-6)(14+x-x-8)(14+x-14)}$$

$$= \frac{1}{2} \times 4 \times 14 + \frac{1}{2} \times 4 \times (x+6) + \frac{1}{2} \times 4(x+8)$$

$$\Rightarrow \sqrt{(14+x) \times 8 \times 6 \times x} = 2(14+x+6+8)$$

$$\Rightarrow \sqrt{42x + 3x^2} = 14 + x$$

$$\Rightarrow 42x + 3x^2 = (14+x)^2$$

$$\Rightarrow 42x + 3x^2 = 196 + x^2 + 28x$$

$$\Rightarrow 2x^2 + 14x - 196 = 0$$

$$\Rightarrow x^2 + 7x - 98 = 0$$

$$\Rightarrow x^2 + 14x - 7x - 98 = 0$$

$$\Rightarrow x(x + 14) - 7(x + 14) = 0$$

$$\Rightarrow (x + 14)(x - 7) = 0$$

$$\Rightarrow x - 7 = 0$$

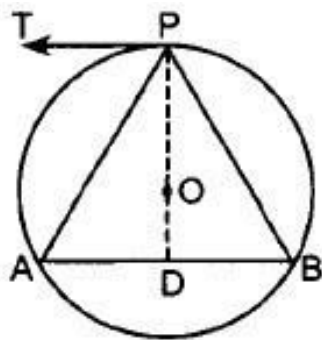
$$\text{Or } x + 14 = 0$$

$$\Rightarrow x = 7$$

Or $x = -14$ extraneous

\therefore The remaining two sides of the triangle are $(x + 6)$ cm and $(x - 8)$ cm,
i.e., $(7 + 6)$ cm or 13 cm and 15 cm.

16. Given,



Construction: Join PO and produce it to D.

Proof: Here, $OP \perp TP$

$$\angle OPT = 90^\circ$$

Also, $TP \parallel AB$

$$\therefore \angle TPD + \angle ADP = 180^\circ$$

$$\Rightarrow \angle ADP = 90^\circ$$

OD bisects AB [Perpendicular from the centre bisects the chord]

In $\triangle ADP$ and $\triangle BDP$

$$AD = BD$$

$$\angle ADP = \angle BDP \text{ [Each } 90^\circ]$$

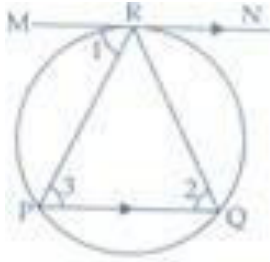
$$PD = PD$$

$$\therefore \triangle ADP \cong \triangle BDP \text{ [SAS]}$$

$$\angle PAB = \angle PBA \text{ [C.P.C.T.]}$$

$\therefore \triangle PAB$ is isosceles triangle.

17. Given: In a circle a chord PQ and a tangent MRN at R such that $QP \parallel MRN$



To prove: R bisects the arc PRQ.

Construction: Join RP and RQ.

Proof: Chord RP subtends $\angle 1$ with tangent MN and $\angle 2$ in alternate segment of circle so $\angle 1 = \angle 2$.

$MRN \parallel PQ$

$\therefore \angle 1 = \angle 3$ [Alternate interior angles]

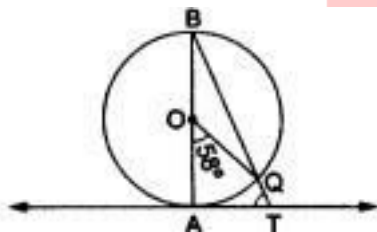
$\Rightarrow \angle 2 = \angle 3$

$\Rightarrow PR = RQ$ [Sides opp. to equal \angle s in $\triangle RPQ$]

\therefore Equal chords subtend equal arcs in a circle so
arc PR = arc RQ

or R bisect the arc PRQ. Hence, proved.

18.



$\angle AOQ = 58^\circ$

$\Rightarrow \angle ABQ = \frac{1}{2} \angle AOQ = 29^\circ$ [\therefore the angle subtended by an arc at the centre is double the angle subtended by it at any point on the remaining part of the circle]

$\Rightarrow \angle ABT = 29^\circ$

Now, AT is a tangent at A and OA is the radius through the point of contact A.

$\therefore OA \perp AT$, i.e,

$\angle OAT = 90^\circ$

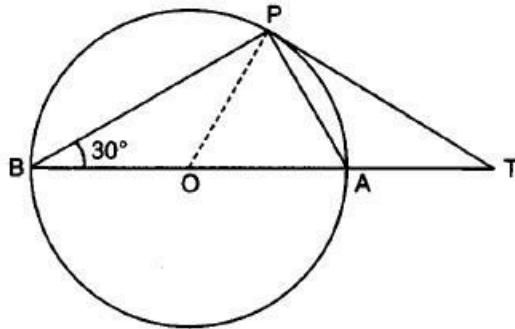
$\Rightarrow \angle BAT = 90^\circ$.

in $\triangle BAT$,

we have

$$\begin{aligned}\angle BAT + \angle ABT + \angle ATB &= 180^\circ \\ \Rightarrow 90^\circ + 29^\circ + \angle ATB &= 180^\circ \\ \angle ATB &= 61^\circ. \\ \therefore \angle ATQ &= \angle ATB = 61^\circ.\end{aligned}$$

19. According to the question,



AB is the chord passing through the centre

So, AB is the diameter

Since, angle in a semi circle is a right angle

$$\angle APB = 90^\circ$$

By using alternate segment theorem

$$\text{We have } \angle APB = \angle PAT = 30^\circ$$

Now, in $\triangle APB$

$$\angle BAP + \angle APB + \angle BPA = 180^\circ \text{ (Angle sum property of triangle)}$$

$$\angle BAP = 180^\circ - 90^\circ - 30^\circ = 60^\circ$$

$$\text{Now, } \angle BAP = \angle APT + \angle PTA \text{ (Exterior angle property)}$$

$$60^\circ = 30^\circ + \angle PTA$$

$$\angle PTA = 60^\circ - 30^\circ = 30^\circ$$

We know that sides opposite to equal angles are equal

$$AP = AT$$

In right triangle ABP:

$$\sin \angle ABP = \frac{AP}{BA}$$

$$\sin 30^\circ = \frac{AP}{BA}$$

$$\frac{1}{2} = \frac{AP}{BA}$$

$$BA : AP = 2 : 1$$

20. According to the question, we are given that from an external point B of a circle with centre 'O', two tangents BC, BD are drawn such that $\angle DBC = 120^\circ$, we have to

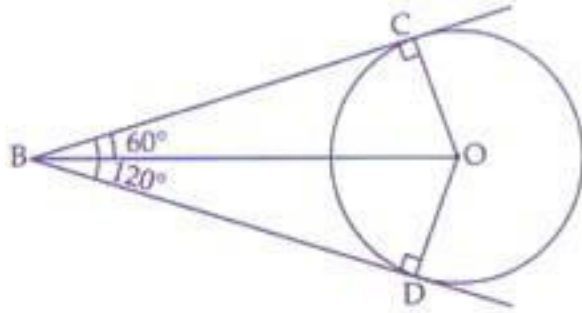
prove that $BC + BD = BO$, i.e., $BO = 2BC$.

Given: A circle with centre O.

Tangents BC and BD are drawn from an external point B such that $\angle DBC = 120^\circ$

To prove: $BC + BD = BO$, i.e., $BO = 2BC$

Construction: Join OB, OC and OD.



Proof: In $\triangle OBC$ and $\triangle OBD$, we have

$OB = OB$ [Common]

$OC = OD$ [Radii of same circle]

$BC = BD$ [Tangents from an external point are equal in length] ...(i)

$\therefore \triangle OBC \cong \triangle OBD$ [By SSS criterion of congruence]

$\Rightarrow \angle OBC = \angle OBD$ (CPCT)

$\therefore \angle OBC = \frac{1}{2} \angle DBC = \frac{1}{2} \times 120^\circ$ [$\because \angle CBD = 120^\circ$ given]

$\Rightarrow \angle OBC = 60^\circ$

OC and BC are radius and tangent respectively at contact point C.

Hence, $\angle OCB = 90^\circ$

Now, in right angle $\triangle OCB$, $\angle OBC = 60^\circ$

$\therefore \cos 60^\circ = \frac{BC}{BO}$

$\Rightarrow \frac{1}{2} = \frac{BC}{BO}$

$\Rightarrow OB = 2BC$

$\Rightarrow OB = BC + BC$

$\Rightarrow OB = BC + BD$ [$\because BC = BD$ from (i)]

Hence, proved.