CBSE Test Paper 02 Chapter 10 Circles

1. If O is the centre of a circle, PQ is a chord and tangent PR at P makes an angle of 60° with PQ, then \angle POQ is equal to **(1)**



- b. 3 cm
- c. 5 cm
- d. 6 cm
- **3.** In figure, PA and PB are two tangents drawn from an external point P to a circle with centre C and radius 4 cm. If PA \perp PB, then the length of each tangent is: **(1)**



- c. 4 cm
- d. 8 cm

- 4. In the given figure, O is the centre of the circle with radius 10 cm. If $AB \parallel CD$, AB = 16 cm and CD = 12 cm, the distance between the two chords AB and CD is : **(1)**
 - a. 12 cm
 - b. 20 cm
 - c. 16 cm
 - d. 14 cm
- **5.** The length of tangent PQ, from an external point Q is 24 cm. If the distance of the point Q from the centre is 25 cm, then the diameter of the circle is **(1)**



- a. 15 cm
- b. 14 cm
- c. 12 cm
- d. 7 cm
- **6.** In the given figure, AB is a chord of the circle and AOC is its diameter such that $\angle ACB =$

50°. If AT is the tangent to the circle at the point A, find \angle BAT (1)



- 7. What term will you use for a line which intersect a circle at two distinct points? (1)
- **8.** In the fig. there are two concentric circles with centre O. PRT and PQS are tangents to the inner circle from a point P lying on the outer circle. If PR = 5 cm find the length of PS. **(1)**



9. A triangle ABC is drawn to circumscribe a circle. If AB = 13 cm, BC = 14 cm and AE = 7 cm, then find AC. (1)



10. Find the distance between two parallel tangents of a circle of radius 3 cm. **(1)**



11. In the given figure, TP and TQ are tangents from T to the circle with centre O and R is any point on the circle. If AB is a tangent to the circle at R, prove that TA + AR = TB + BR. **(2)**



12. In figure, if OL = 5 cm, OA = 13 cm, then length of AB is (2)



13. In figure, if TP and TQ are the two tangents to a circle with centre O so that $\angle POQ = 110^{\circ}$, then find $\angle PTQ$. **(2)**



- 14. From an external point P, tangents PA and PB are drawn to a circle with centre O. At one point E on the circle tangent is drawn which intersects PA and PB at C and D respectively. If PA = 14 cm, find the perimeter of \triangle PCD. (3)
- **15.** In the given figure, O is the centre of the circle. Determine $\angle AQB$ and $\angle AMB$, if PA and PB are tangents **(3)**



- 16. Prove that the line segment joining the points of contact of two parallel tangents of a circle, passes through its centre. (3)
- 17. The tangent at a point C of a circle and a diameter AB when extended intersect at P. If

 \angle PCA = 110°, find \angle CBA.

[Hint: Join C with centre O]. (3)



- 18. In figure, the sides AB, BC and CA of triangle ABC touch a circle with centre O and radius r at P, Q and R respectively. Prove that
 - i. AB + CQ = AC + BQ
 - **ii.** Area (ABC) = $\frac{1}{2}$ (perimeter of \triangle ABC) \times r (4)



19. In Fig. there are two concentric circles with centre O of radii 5 cm and 3 cm. From an external point P, tangents PA and PB are drawn to these circles. If AP = 12 cm, find the length of BP. (4)



20. In fig. two tangents AB and AC are drawn to a circle with centre O such that $\angle BAC = 120^{\circ}$. Prove that OA = 2AB. **(4)**



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Soluiton

1. b. 120°

Explanation: Here $\angle RPO = 90^{\circ}$

 $\angle RPQ = 60^{\circ}$ (given) $\therefore \angle OPQ = 90^{\circ} - 60^{\circ} = 30^{\circ} \angle PQO = 30^{\circ}$ Also [Opposite angles of equal radii] Now, In triangle OPQ, $\angle OPQ + \angle PQO + \angle QOP = 180^{\circ}$ $\Rightarrow 30^{\circ} + 30^{\circ} + \angle QOP = 180^{\circ}$ $\Rightarrow \angle QOP = 120^{\circ}$

2. a. 4 cm

Explanation: Here $\angle Q = 90^{\circ}$ [Angle between tangent and radius through the point of

contact]

Now, in right angled triangle OPQ,

$$OP^2 = OQ^2 + PQ^2$$

$$\Rightarrow (5)^2 = (3)^2 + PQ^2$$

$$\Rightarrow PQ^2 = 25 - 9 = 16$$

 \Rightarrow PQ = 4 cm

But PQ = PR [Tangents from one point to a circle are equal]

Therefore, PR = 4 cm

3. c. 4 cm



Construction: Joined AC and BC. Here CA \perp AP and CB \perp BP and PA \perp PB Also AP = PB

Therefore, BPAC is a square. \Rightarrow AP = PB = BC = 4 cm

4. d. 14 cm



Let OP be the perpendicular to chord AB and P bisects the chord AB and OQ be the perpendicular to chord CD and Q bisects the chord CD.

$$\therefore AP = BP = 8 \text{ cm and } CQ = DQ = 6 \text{ cm}$$

In triangle AOP, $OA^2 = OP^2 + AP^2$
 $\Rightarrow (10)^2 = OP^2 + (8)^2$
 $\Rightarrow OP^2 = 100 - 64 = 36$
 $\Rightarrow OP = 6 \text{ cm}$
And in right angled triangle COQ,
 $OC^2 = OQ^2 + CQ^2$
 $\Rightarrow (10)^2 = OQ^2 + (6)^2$
 $\Rightarrow OQ^2 = 100 - 36 = 64$
 $\Rightarrow OQ = 8 \text{ cm}$

Therefore, distance between two chord AB and CD = OP + OQ = 6 + 8 = 14 cm

5. b. 14 cm



Here $\angle OPQ = 90^{\circ}$ [Angle between tangent and radius through the point of contact]

$$\therefore OQ^{2} = OP^{2} + PQ^{2} \Rightarrow (25)^{2} = OP^{2} + (24)^{2}$$
$$\Rightarrow OP^{2} = 625 - 576 \Rightarrow OP^{2} = 49$$
$$\Rightarrow OP^{2} = 49 \Rightarrow OP = 7 \text{ cm}$$
Therefore, the diameter = 2 × OP = 2 × 7 = 14 cm

- 6. $\therefore \angle ACB = 50^{\circ}$ $\angle CBA = 90^{\circ}$ (Angle in semi-circle) $\therefore \angle OAB = 90^{\circ} - 50^{\circ}$ $= 40^{\circ}$ $\angle BAT = 90^{\circ} - \angle OAB$ $= 90^{\circ} - 40^{\circ}$ $= 50^{\circ}$
- 7. A line that interests a circle at two points in a circle is called a Secant.
- 8. PQ = PR = 5 cm (Length of Tangents from same external point are always equal) and PQ = QS (perpendicular from center of the circle to the chord bisects the chord)
 ∴ PS = 2PQ = 2 × 5 = 10cm
- 9. AF = AE = 7cm (tangents from same external point are equal) $\therefore BF = AB - AF = 13 - 7 = 6cm$ BD = BF = 6cm (tangents from same external point) $\therefore CD = BC - BD = 14 - 6 = 8cm$ CE = CD = 8cm $\therefore AC = AE + EC$ = 7 + 8 = 15cm.
- 10. Distance between two parallel tangents = diameter = PQ
 PQ = OP + OQ = 3 + 3 = 6cm
 The total distance between two parallel tangents lines is 6 cm.
- 11. Length of tangents from same external point are equal.

 \therefore TP = TQ AP = AR and BR = BQ We have, TP = TQ $\Rightarrow TA + AP = TB + BQ$ $\Rightarrow TA + AR = TB + BR$ Hence proved.

12. AB = 2 AL =
$$2\sqrt{OA^2 - OL^2}$$

= $2\sqrt{13^2 - 5^2}$
= $2\sqrt{169 - 25} = 2\sqrt{144}$
= $2 \times 12 = 24$ cm

13. $\angle POQ = 110^{\circ}$

 \angle OPT = 90° [Angle between tangent and radius through the point of contact] \angle OQT = 90° [Angle between tangent and radius through the point of contact] In quadrilateral OPTQ,

 $\angle POQ + \angle OQT + \angle PTQ = 360^{\circ}$

 \therefore The sum of all the angles of a quadrilateral is 360° .

$$\Rightarrow 110^{\circ} + 90^{\circ} + \angle PTQ = 360^{\circ}$$

$$\Rightarrow 290^{\circ} + \angle PTQ = 360^{\circ} - 290^{\circ} = 70^{\circ}$$

$$\Rightarrow \text{Hence, the } \angle PTQ \text{ is } 70^{\circ}.$$

14. We have,

$$AC = CE, BD = DE$$

And, AP = BP = 14 cm

$$\therefore \text{ Perimeter of } \Delta PCD = PC + CD + PD$$

$$\Rightarrow \text{ Perimeter of } \Delta PCD = PC + (CE + ED) + PD$$

$$= (PC + CE) + (ED + PD)$$

$$= (PC + AC) + (BD + PD)$$

$$= PA + PB$$

- = 14 + 14
- = 28
- \therefore Perimeter of \triangle PCD = 28 cm.
- 15. Given,



16.

Given: l and m are the tangent to a circle such that l || m, intersecting at A and B respectively.

To prove: AB is a diameter of the circle.

Proof:

A tangent at any point of a circle is perpendicular to the radius through the point of contact.

 $\therefore \angle XAO = 90^{\circ}$ and $\angle YBO = 90^{\circ}$

0

Since $\angle XAO + \angle YBO = 180^{\circ}$

An angle on the same side of the transversal is 180°.

Hence the line AB passes through the centre and is the diameter of the circle.

17. According to the question, we are given that tangent at a point C of a circle and a diameter AB when extended intersect at P. If \angle PCA = 110^o, find \angle CBA.



OC and CP are radius and tangent respectively at contact point C.

So, $\angle OCP = 90^{\circ}$ $\angle OCA = \angle ACP - \angle OCP$ $\Rightarrow \angle OCA = 110^{\circ} - 90^{\circ}$

 $\Rightarrow \angle \text{OCA} = 20^{\circ}$

In \triangle OAC,

OA = OC [Radii of same circle]

Therefore, $\angle OCA = \angle A = 20^{\circ}$ [Since, Angles opposite to equal sides are equal] CP and CB are tangent and chord of a circle.

Therefore, $\angle CBP = \angle A$ [Angles in alternate segments are equal] In $\triangle CAP$,

 $\angle P + \angle A + \angle ACP = 180^{\circ}$ [Angled sum property of a triangle]

$$\Rightarrow \angle P + 20^{\circ} + 110^{\circ} = 180^{\circ}$$
$$\Rightarrow \angle P = 180^{\circ} - 130^{\circ}$$
$$\Rightarrow \angle P = 50^{\circ}$$
In $\triangle BPC$,
Exterior angle $\angle CBA = \angle P + \angle BCP$
$$\Rightarrow \angle CBP = 50^{\circ} + 20^{\circ}$$
$$\Rightarrow \angle CBP = 70^{\circ}$$

18. Given, the sides AB, BC and CA of triangle ABC touch a circle with centre O and radius

r at P, Q and R respectively.

$$A = AR [Tangents from A] ...(i)$$

$$Similarly, BP = BQ ...(ii)$$

$$CR = CQ ...(iii)$$
Now,

$$\therefore AP = AR$$

$$\Rightarrow (AB-BP) = (AC - CR)$$

$$\Rightarrow AB + CR = AC + BP$$

$$\Rightarrow AB + CQ = AC + BQ [Using eq. (ii) and (iii)]$$
(ii) Let AB = x, BC = y, AC = z

$$\therefore Perimeter of \triangle ABC = \frac{1}{2} [area of \triangle AOB + area of \triangle BOC + area of \triangle AOC]$$

$$\Rightarrow Area of \triangle ABC = \frac{1}{2} \times AB \times OP + \frac{1}{2} \times BC \times OQ + \frac{1}{2} \times AC \times OR$$

$$\Rightarrow Area of \triangle ABC = \frac{1}{2} (x + y + z) \times r$$

$$\Rightarrow Area of \triangle ABC = \frac{1}{2} (Perimeter of \triangle ABC) \times r$$





Join OA, OB and OP.

 $\angle OAP = 90^\circ$ as the tangent makes a right angle with the radius of the circle at the point of contact.

In \triangle OAP, we have, OP² = OA² + AP²

$$\Rightarrow 0P^2 = 5^2 + 12^2$$

 \Rightarrow OP = 13 cm

 $\angle OBP = 90^{\circ}$ as the tangent makes a right angle with the radius of the circle at the point of contact.

In \triangle OBP, we have,

$$OP^{2} = OB^{2} + BP^{2}$$

$$\Rightarrow 13^{2} = 3^{2} + Bp^{2}$$

$$\Rightarrow BP^{2} = 169 - 9 = 160$$

$$\Rightarrow BP = \sqrt{160} \text{ cm} = 4\sqrt{10} \text{ cm}$$

20.

In Δ 's OAB and OAC, we have, $\angle OBA = \angle OCA = 90^{\circ}$ OA = OA [Common] AB = AC [:. Tangents from an external point are equal in length] Therefore, by RHS congruence criterion, we have, $\Delta OBA \cong \Delta OCA$ $\Rightarrow \angle OAB = \angle OAC$ [By c.p.c.t.] $\therefore \angle OAB = \angle OAC = \frac{1}{2} \angle BAC$ $= \frac{1}{2} \times 120^{\circ} = 60^{\circ}$ $\Rightarrow \angle OAB = \angle OAC = 60^{\circ}$ In Δ OBA, we have, $\cos B = \frac{AB}{OA}$

$$\Rightarrow \cos 60^{\circ} = \frac{AB}{OA}$$
$$\Rightarrow \frac{1}{2} = \frac{AB}{OA}$$
$$\Rightarrow 0A = 2AB$$

Hence proved.