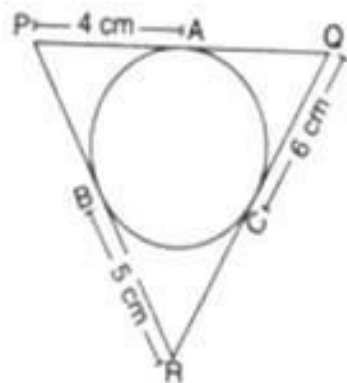


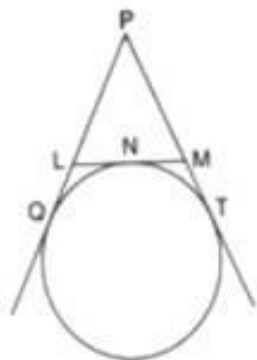
CBSE Test Paper 01

Chapter 10 Circles

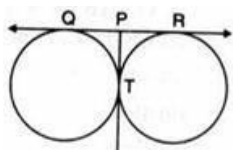
1. The perimeter of $\triangle PQR$ in the given figure is **(1)**



- a. 15 cm
 b. 60 cm
 c. 45 cm
 d. 30 cm.
2. If $PQ = 28$ cm, then the perimeter of $\triangle PLM$ is **(1)**



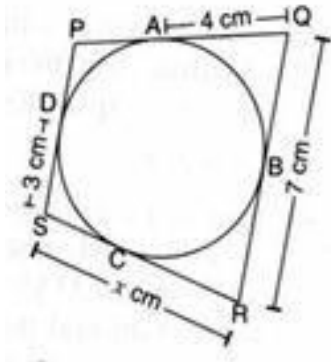
- a. 48 cm
 b. 56 cm
 c. 42 cm
 d. 28 cm
3. In the given figure if $QP = 4.5$ cm, then the measure of QR is equal to **(1)**



- a. 15 cm
 b. 9 cm

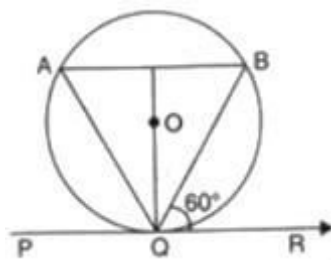
- c. 18 cm
- d. 13.5 cm

4. In the given figure, if $AQ = 4$ cm, $QR = 7$ cm, $DS = 3$ cm, then x is equal to **(1)**



- a. 6 cm
- b. 10 cm
- c. 11 cm
- d. 8 cm

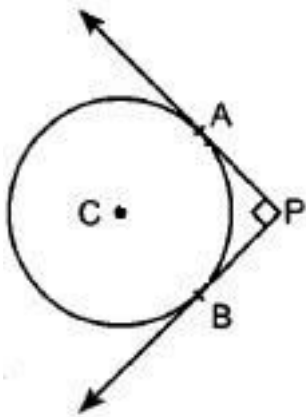
5. If PQR is a tangent to a circle at Q whose centre is O , AB is a chord parallel to PR and $\angle BQR = 60^\circ$, then $\angle AQB$ is equal to **(1)**



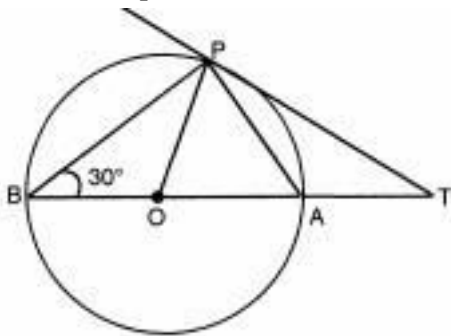
- a. 60°
- b. 30°
- c. 90°
- d. 45°

6. How many common tangents can be drawn to two circles touching internally? **(1)**
7. How many tangents can a circle have? **(1)**
8. A quadrilateral $ABCD$ is drawn to circumscribe a circle. If $AB = 12$ cm, $BC = 15$ cm and $CD = 14$ cm, find AD . **(1)**
9. How many tangents, parallel to a secant can a circle have? **(1)**

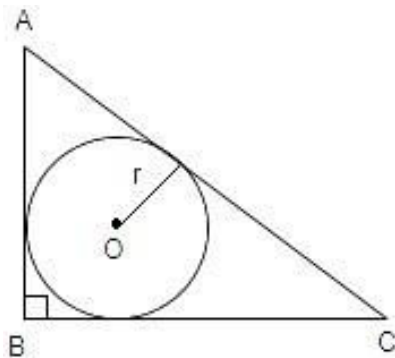
10. In figure, PA and PB are two tangents drawn from an external point P to a circle with centre C and radius 4 cm. If $PA \perp PB$, find the length of each tangent. **(1)**



11. In the given figure, line BOA is a diameter of a circle and the tangent at a point P meets BA when produced at T. If $\angle PBO = 30^\circ$ what is the measure of $\angle PTA$? **(2)**

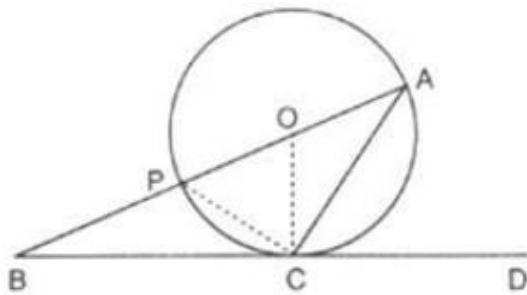


12. Two concentric circles are of radii 7 cm and r cm respectively where $r > 7$. A chord of the larger circle of the length 48 cm, touches the smaller circle. Find the value of r . **(2)**
13. In the adjoining figure, a right angled $\triangle ABC$, circumscribes a circle of radius r . If AB and BC are of lengths 8 cm and 6 cm respectively, then find the value of r . **(2)**

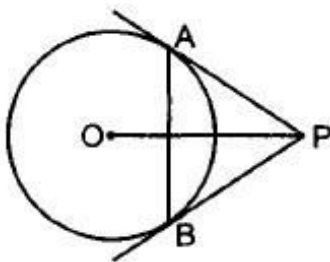


14. PQR is a right angled triangle right angled at Q. $PQ = 5$ cm, $QR = 12$ cm. A circle with centre O is inscribed in $\triangle PQR$, touching its all sides. Find the radius of the circle. **(3)**

15. ABC is a right-angled triangle, right angled at A. A circle is inscribed in it. The lengths of two sides containing the right angle are 24 cm and 10 cm. Find the radius of the incircle. **(3)**
16. Two concentric circles are of radii 5 cm and 3 cm, find the length of the chord of the larger circle which touches the smaller circle. **(3)**
17. The common tangents AB and CD to two circles with centres O and O' intersect at E between their centres. Prove that the points O, E and O' are collinear. **(3)**
18. In fig O is the centre of the circle and BCD is tangent to it at C. Prove that $\angle BAC + \angle ACD = 90^\circ$. **(4)**



19. If a, b, c are the sides of a right triangle where c is the hypotenuse, prove that the radius r of the circle which touches the sides of the triangle is given by $r = \frac{a+b-c}{2}$ **(4)**
20. In figure, PA and PB are two tangents drawn from an external point P to a circle with centre O. Prove that OP is the right bisector of line segment AB. **(4)**



CBSE Test Paper 01
Chapter 10 Circles

Solution

1. d. 30 cm.

Explanation Since Tangents from an external point to a circle are equal.

$$\therefore PA = PB = 4 \text{ cm},$$

$$BR = CR = 5 \text{ cm}$$

$$CQ = AQ = 6 \text{ cm}$$

$$\text{Perimeter of } \triangle PQR = PQ + QR + RP$$

$$= PA + AQ + QC + CR + BR + PB$$

$$= 4 + 6 + 6 + 5 + 5 + 4 = 30 \text{ cm}$$

2. b. 56 cm

Explanation: We know that, $PQ = \frac{1}{2}$ (Perimeter of $\triangle PLM$)

$$\Rightarrow 28 = \frac{1}{2} (\text{Perimeter of } \triangle PLM)$$

$$\Rightarrow (\text{Perimeter of } \triangle PLM) = 28 \times 2 = 56 \text{ cm}$$

3. b. 9 cm

Explanation: Here $QP = PT = 4.5 \text{ cm}$ [Tangents to a circle from an external point P]

Also $PT = PR = 4.5 \text{ cm}$ [Tangents to a circle from an external point P]

$$\therefore QR = QP + PR = 4.5 + 4.5 = 9 \text{ cm}$$

4. a. 6 cm

Explanation: Here $AQ = 4 \text{ cm}$

$\therefore QB = AQ = 4 \text{ cm}$ [Tangents from an external point]

$$\therefore BR = 7 - 4 = 3 \text{ cm}$$

$\therefore BR = CR = 3 \text{ cm}$ [Tangents from an external point]

Also $SD = SC = 3 \text{ cm}$ [Tangents from an external point]

$$\text{Therefore, } x = CS + CR = 3 + 3 = 6 \text{ units}$$

5. a. 60°

Explanation: Since $AB \parallel PR$ and BQ is intersecting them.

$$\therefore \angle BQR = \angle QBA = 60^\circ \text{ [Alternate angles]}$$

$$\text{And } \angle BQR = \angle QAB = 60^\circ \text{ [Alternate segment theorem]}$$

Now, in triangle AQB,

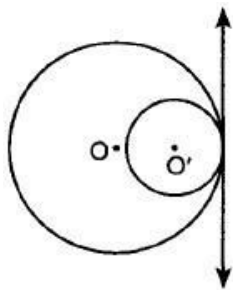
$$\angle AQB + \angle QBA + \angle BAQ = 180^\circ$$

$$\Rightarrow \angle AQB + 60^\circ + 60^\circ = 180^\circ$$

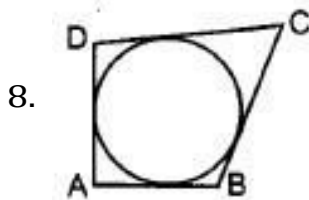
$$\Rightarrow \angle AQB = 60$$

6. One common tangent can be drawn to two circles touching internally

Figure:



7. A circle can have infinitely many tangents since there are infinitely many points on the circumference of the circle and at each point of it, it has a unique tangent.



8.

Now,

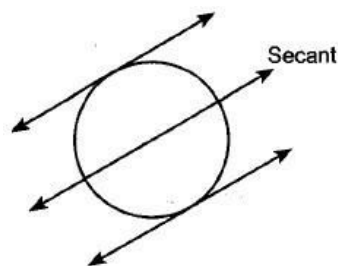
$$AB + CD = BC + AD$$

$$\Rightarrow 12 + 14 = 15 + AD$$

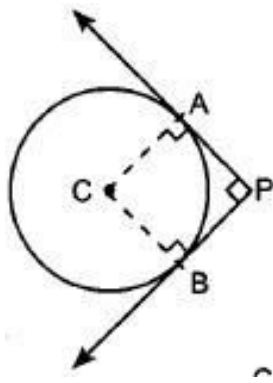
$$\Rightarrow AD = 11\text{cm}$$

9. A circle can have 2 tangents parallel to a secant.

Diagram:



10. PA and PB are two tangents drawn from an external point P to a circle.



$$CA \perp AP$$

$$CB \perp BP$$

$$PA \perp PB$$

\therefore BPAC is a square.

$$\Rightarrow AP = PB = BC = 4\text{cm}$$

11. $\angle AOP = 2\angle ABP$ (Angle subtended by an arc is twice angle subtended by same arc at any other point on the circle)

$$\Rightarrow \angle AOP = 2 \times 30 = 60^\circ$$

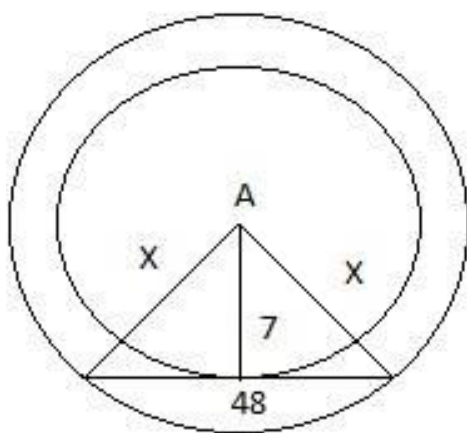
$$\angle OPT = 90^\circ \text{ (Radius and Tangent are perpendicular to each other)}$$

In $\triangle OPT$

$$90^\circ + 60^\circ + \angle T = 180^\circ \text{ (ASP)}$$

$$\Rightarrow \angle ATP = 30^\circ$$

12.



Let us take $r = x$

Now using Pythagoras theorem

$$(x)^2 = 24^2 + 7^2$$

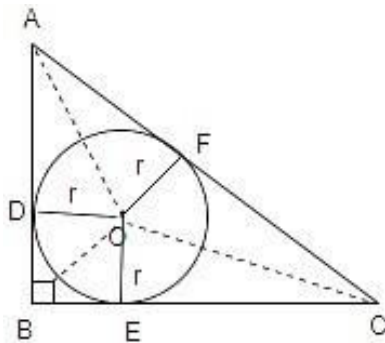
$$(x)^2 = 576 + 49$$

$$(x)^2 = 625$$

Therefore, $x = 25$ cm.

$r = 25$ cm.

13. Let D, E and F are points where the in-circle touches the sides AB, BC and CA respectively. Join OA, OB and OC.



In $\triangle ABC$, $AC^2 = AB^2 + BC^2$ [By Pythagoras theorem]

$$= 8^2 + 6^2$$

$$= 64 + 36$$

$$= 100$$

$\therefore AC = \sqrt{100} = 10$ cm [taking positive square root, as length cannot be negative]

$$\text{Now, } ar(\triangle OAB) = \frac{1}{2} \times OD \times AB = \frac{1}{2} \times r \times 8 = \frac{8r}{2} = 4rcm^2$$

$$ar(\triangle OBC) = \frac{1}{2} \times OE \times BC = \frac{1}{2} \times r \times 6 = \frac{6r}{2} = 3rcm^2$$

$$\text{and } ar(\triangle OAC) = \frac{1}{2} \times OF \times AC = \frac{1}{2} \times r \times 10 = \frac{10r}{2} = 5rcm^2$$

$$\therefore ar(\triangle ABC) = ar(\triangle OAB) + ar(\triangle OBC) + ar(\triangle OAC)$$

$$\Rightarrow \frac{1}{2} \times AB \times BC = 4r + 3r + 5r = 12r$$

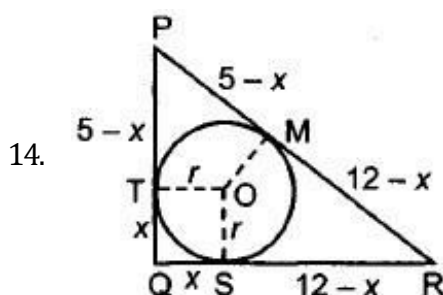
$$\Rightarrow \frac{1}{2} \times 8 \times 6 = 12r$$

$$\Rightarrow 24 = 12r$$

$$\Rightarrow r = \frac{24}{12}$$

$$\Rightarrow r = 2 \text{ cm}$$

The value of r is 2 cm.



Let $QS = x$; $SR = 12 - x$

$\therefore PT = 5 - x$, $PM = PT$

$\therefore PM = 5 - x$

Also $SR = MR \Rightarrow MR = 12 - x$

Also $PQ^2 + QR^2 = PR^2$

$\Rightarrow PR = 13 \Rightarrow PM + MR = 13$

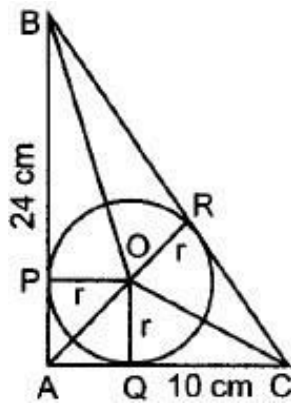
$\Rightarrow 5 - x + 12 - x = 13 \Rightarrow 2x = 4 \Rightarrow x = 2$

Also OSQT is a square

$OS = QS$

$\Rightarrow OS = 2\text{cm}$

15. Given,



$AB = 24\text{cm}$, $AC = 10\text{cm}$

In right-angled $\triangle ABC$

$$BC^2 = AB^2 + AC^2$$

$$= 24^2 + 10^2$$

$$= 676$$

$$\Rightarrow \mathbf{BC = 26\text{cm}}$$

Let r be the radius of the incircle

$\Rightarrow OP \perp AB$, $OQ \perp AC$ and $OR \perp BC$

$OP = OQ = OR$ [Incentre of a triangle is equidistant from its sides]

$$\text{ar}(\triangle ABC) = \text{ar}(\triangle AOB) + \text{ar}(\triangle BOC) + \text{ar}(\triangle AOC)$$

$$\frac{1}{2} AB \times AC = \frac{1}{2} AB \times OP + \frac{1}{2} AC \times OQ + \frac{1}{2} \times BC \times OR$$

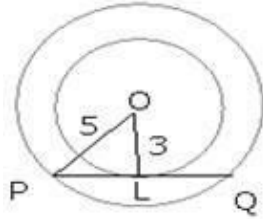
$$\frac{1}{2} \times 24 \times 10 = \frac{1}{2} [24 \times r + 10 \times r + 26 \times r]$$

$$\Rightarrow 120 = r[24 + 10 + 26]$$

$$\Rightarrow 120 = r[24 + 10 + 26]$$

$$\Rightarrow 120 = 30r \Rightarrow r = 4 \text{ cm}$$

16. \therefore PQ is the chord of the larger circle which touches the smaller circle at the point L.
Since PQ is tangent at the point L to the smaller circle with centre O.



$$\therefore OL \perp PQ$$

$$\therefore PQ \text{ is a chord of the bigger circle and } OL \perp PQ$$

$$\therefore OL \text{ bisects } PQ$$

$$\therefore PQ = 2 PL$$

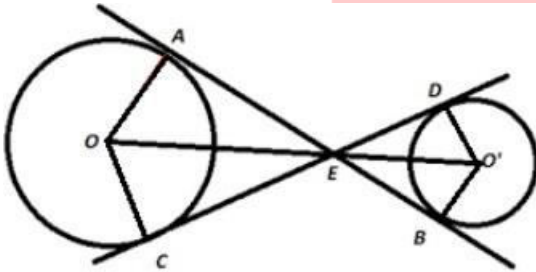
In $\triangle OPL$,

$$PL = \sqrt{OP^2 - OL^2} = \sqrt{5^2 - 3^2} = \sqrt{25 - 9} = 4$$

$$\therefore \text{Chord } PQ = 2PL = 8 \text{ cm}$$

$$\therefore \text{Length of chord } PQ = 8 \text{ cm}$$

17. Construction: Join OA and OC.



$$\angle AEC = \angle DEB \text{(vertically opposite angles)}$$

In $\triangle OAE$ and $\triangle OCE$,

$$OA = OC \text{ ...(Radii of the same circle)}$$

$$OE = OE \text{ ...(Common side)}$$

$$\angle OAE = \angle OCE \text{(each is } 90^\circ)$$

$$\Rightarrow \triangle OAE \cong \triangle OCE \text{(RHS congruence criterion)}$$

$$\Rightarrow \angle AEO = \angle CEO \text{(cpct)}$$

Similarly, for the circle with centre O' ,

$$\angle DEO' = \angle BEO'$$

$$\text{Now, } \angle AEC = \angle DEB$$

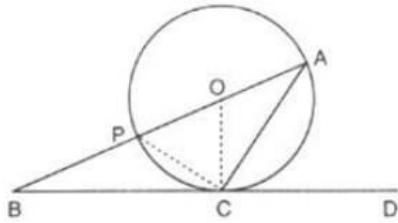
$$\Rightarrow \frac{1}{2} \angle AEC = \frac{1}{2} \angle DEB$$

$$\Rightarrow \angle AEO = \angle CEO = \angle DEO' = \angle BEO'$$

Hence, all the four angles are equal and bisected by OE and O'E.

So, O, E and O' are collinear.

18.



$\angle OCD = 90^\circ$ (tangent and radii are \perp to one another at the point of contact)

In $\triangle OCA$,

$OC = OA$ (radii of circle)

Hence, $\angle OCA = \angle OAC$ (angles opposite to equal sides are equal)

Also, $\angle OCD = \angle OCA + \angle ACD$

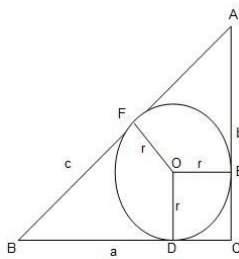
$$90^\circ = \angle OAC + \angle ACD (\because \angle OCA = \angle OAC)$$

$$90^\circ = \angle BAC + \angle ACD$$

$$\text{Hence, } \angle BAC + \angle ACD = 90^\circ$$

Hence proved.

19.



The circle touches the sides BC, CA, AB of the right triangle ABC at D, E and F respectively. Let $BC = a$, $CA = b$ and $AB = c$

Now, $AF = AE$ and $BD = BF$

$$\Rightarrow AF = AE = AC - CE \text{ and } BF = BD = BC - CD$$

$$\Rightarrow AF = b - r \text{ and } BF = a - r (\because OEDC \text{ is a square})$$

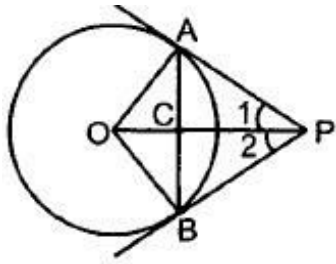
$$\Rightarrow AF + BF = (b - r) + (a - r)$$

$$\Rightarrow AB = a + b - 2r$$

$$\Rightarrow c = a + b - 2r$$

$$\Rightarrow r = \frac{a+b-c}{2}$$

20. Given, PA and PB are two tangents.



Construction: Join OA and OB .

In $\triangle PAO$ and $\triangle PBO$, $OA = OB$ [Radii]

$OP = OP$ [Common]

and $AP = BP$ [Tangents from P]

$\therefore \triangle PAO = \triangle PBO$ (SSS)

$\Rightarrow \angle 1 = \angle 2$

In $\triangle APC$ and $\triangle BPC$, $\angle 1 = \angle 2$ [Proved]

$AP = BP$ and $PC = PC$,

$\triangle APC \cong \triangle BPC$ [SAS]

$AC = BC$

and $\angle ACP = \angle BCP$

Also, $\angle ACP + \angle BCP = 180^\circ$ [by linear pair axiom]

$\angle ACP + 90^\circ = 180^\circ$

$\Rightarrow \angle ACP = 90^\circ$

$\therefore OP$ is right bisector of AB .