CBSE Test Paper 01

Chapter 05 Arithmetic Progression

- **1.** In an AP, if a = 4, n = 7 and a_n = 4, then the value of 'd' is (1) a. 0 b. 1 c. 3 d. 2 **2.** The next two terms of the AP : k, 2k + 1, 3k + 2, 4k + 3, are (1) a. 5k + 4 and 6k + 5 b. 4k + 4 and 4k + 5 c. 5k + 5 and 6k + 6 d. 5k and 6k **3.** The common difference of the A.P. can be **(1)** a. only negative b. only zero c. positive, negative or zero d. only positive **4.** The 7th term from the end of the A.P. – 11, – 8, – 5,, 49 is (1) a. 28 b. 31 c. -11 d. -8 5. The common difference of the A.P whose $a_n=-3n+7$ is (1) a. 3 b. 1 c. -3 d. 2
 - 6. If 5 times the 5th term of an AP is equal to 10 times the 10th term, show that its 15th term is zero. (1)
 - 7. Write the first term a and the common difference d of A.P. -1.1, -3.1, -5.1, -7.1, ... (1)

- For what value of n are the nth term of the following two AP's are same 13, 19, 25, and 69, 68, 67 (1)
- 9. Find k, if the given value of x is the kth term of the given AP $5\frac{1}{2}$, 11, $16\frac{1}{2}$, 22, ..., x = 550. **(1)**
- **10.** Find the 6th term from the end of the A.P. 17,14,11,..., 40 (1)
- 11. How many terms of the AP 17,15,13,11, ... must be added to get the sum 72? (2)
- **12.** Find n. Given a = first term = -18.9, d = common difference = 2.5, a_n = the nth term = 3.6, n = ? (2)
- **13.** Find the number of terms in each of the following APs. 18, $15\frac{1}{2}$, 13, ..., 47. (2)
- 14. The first and the last terms of an AP are 5 and 45 respectively. If the sum of all its terms is 400, find the common difference and the number of terms. (3)
- **15.** The 14th term of an A.P. is twice its 8th term. If the 6th term is -8, then find the sum of its first 20 terms. **(3)**
- **16.** Find the 6th term from end of the AP 17, 14, 11, ..., -40. (3)
- 17. The houses of a row in a colony are numbered consecutively from 1 to 49. Show that there is a value of x such that the sum of the numbers of the houses preceding the house numbered x is equal to the sum of the numbers of the houses following it. Find the value of x. (3)
- **18.** The sum of first n terms of an A.P. is $3n^2 + 4n$. Find the 25^{th} term of this A.P. (4)
- 19. If sum of first 6 terms of an A.P. is 36 and that of the first 16 terms is 256, find the sum of the first 10 terms. (4)
- 20. The sum of the third and the seventh terms of an AP is 6 and their product is 8. Find the sum of the first sixteen terms of the AP. (4)

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Answers

1. a. 0

2.

Explanation: Given: a = 4, n = 7 and $a_n = 4$, then $a_n = a + (n - 1) d$ $\Rightarrow 4 = 4 + (7 - 1) d$ $\Rightarrow 4 - 4 = 6d$ $\Rightarrow 6d = 0$ $\Rightarrow d = 0$ a. 5k + 4 and 6k + 5 **Explanation:** Given: $k, 2k + 1, 3k + 2, 4k + 3, \dots$

Here d = 2k+1-k=k+1Therefore, the next two terms are 4k+3+k+1=5k+4 and 5k+4+k+1=6k+5

3. c. positive, negative or zero

Explanation: The common difference of the A.P. can be positive, e.g. 1, 2, 3, 4 d is +ve and series is increasing negative e.g 4, 3, 2, 1 d is - ve and series is decreasing

or zero also and the AP becomes constant e.g 4, 4, 4, 4

4. b. 31

Explanation: Reversing the given A.P., we have

$$\begin{array}{l} 49, 46, 43, \dots, -11 \\ \text{Here, } a = 49, d = 46 - 49 = -3 \text{ and } n = 7 \\ \therefore a_n = a + (n - 1) d \\ \Rightarrow a_7 = 49 + (7 - 1) \times (-3) \\ = 49 + 6 \times (-3) \\ \Rightarrow a_7 = 49 - 18 = 31 \end{array}$$

5. c. – 3

Explanation: Given: $a_n = -3n + 7$

Putting n = 1, 2, 3, we get $a = -3 \times 1 + 7 = -3 + 7 = 4$ $a_2 = -3 \times 2 + 7 = -6 + 7 = 1$ $a_3 = -3 \times 3 + 7 = -9 + 7 = -2$ \therefore Common difference $(d) = a_2 - a = 1 - 4 = -3$

6. Let 1^{st} term = a and common difference = d.

 $a_5 = a + 4d, a_{10} = a + 9d$

According to the question, 5 \times a₅ = 10 \times a₁₀ \Rightarrow 5(a + 4d) = 10(a + 9d) \Rightarrow 5a + 20d = 10a

 $+90d \Rightarrow a = -14d$

Now, $a_{15} = a + 14d \Rightarrow a_{15} = -14d + 14d = 0$.

7. -1.1, -3.1, -5.1, -7.1,...

First term (a) = -1.1

We know that common difference is difference between any two consecutive terms of an A.P.

So, common difference(d) = (-3.1) - (-1.1)

8. nth term of 13, 19, 25, = nth term of 69, 68, 67, 13 + (n - 1) 6 = 69 + (n - 1) (-1)13 + 6n - 6 = 69 - n + 1n + 6n = 70 - 77n = 63n = 9 Therefore, n = 911

9.
$$a = 5\frac{1}{2} = \frac{11}{2}$$
, $d = a_2 - a_1 = 11 - \frac{11}{2} = \frac{11}{2}$ and $x = 550$
A.T.Q., $a_k = x$
 $\Rightarrow a + (k-1)d = 550$
 $\Rightarrow \frac{11}{2} + (k-1)\frac{11}{2} = 550$
 $\Rightarrow \frac{11}{2} + \frac{11}{2}k - \frac{11}{2} = 550$
 $4 \text{ of } 11 \Rightarrow \frac{11}{2}k = 550$
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$$\Rightarrow$$
 k = $rac{550 imes 2}{11} = 100$

10. A.P. is 17,14,11,..., - 40

We have,

l = Last term = -40 , a = 17 and, d = Common difference= 14 - 17 = - 3

: 6th term from the end = l - (n - 1)d

= l - (6-1) d

= -40 - 5 imes (-3)

= -40 + 15

= -25

So, 6th term of given A.P. is -25.

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11. Given A.P. is 17, 15, 13, 11......
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Here, 1st term (a) = 17 and common difference (d) = (15 - 17) = -2
Let the sum of n terms be 72. Then,
S_n = 72
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$$\Rightarrow \frac{n}{2} \cdot \{2a + (n - 1)d\} = 72$$

$$\Rightarrow n \{2 \times 17 + (n - 1)(-2)\} = 144$$

$$\Rightarrow n(36 - 2n) = 144$$

$$\Rightarrow 2n^{2} - 36n + 144 = 0$$

$$\Rightarrow n^{2} - 18n + 72 = 0$$

$$\Rightarrow n^{2} - 18n + 72 = 0$$

$$\Rightarrow n(n - 12) - 6(n - 12) = 0$$

$$\Rightarrow (n - 12)(n - 6) = 0$$

$$\Rightarrow n = 6 \text{ or } n = 12.$$

 \therefore sum of first 6 terms = sum of first 12 terms = 72.

This means that the sum of all terms from 7th to 12th is zero.

12.
$$a_n = a + (n - 1)d$$

$$\Rightarrow 3.6 = -18.9 + (n - 1) (2.5)$$

$$\Rightarrow 3.6 + 18.9 = (n - 1) (2.5)$$

$$\Rightarrow 22.5 = (n - 1) (2.5)$$

$$\Rightarrow n - 1 = \frac{22.5}{2.5}$$

$$\Rightarrow n - 1 = 9$$

 \Rightarrow n = 10

13.
$$18, 15\frac{1}{2}, 13, \dots, -47$$

Here, a = 18
 $d = 15\frac{1}{2} - 18 = \frac{31}{2} - 18 = -\frac{5}{2}$
 $a_n = -47$
Let the number of terms be n.

Then,

$$a_{n} = -47$$

$$\Rightarrow a + (n - 1)d = -47$$

$$\Rightarrow 18 + (n - 1)\left(-\frac{5}{2}\right) = -47$$

$$\Rightarrow -\frac{5}{2}(n - 1) = -47 - 18$$

$$\Rightarrow -\frac{5}{2}(n - 1) = -65$$

$$\Rightarrow \frac{5}{2}(n - 1) = 65$$

$$\Rightarrow n - 1 = \frac{65 \times 2}{5}$$

$$\Rightarrow n - 1 = 26$$

$$\Rightarrow n = 26 + 1$$

$$\Rightarrow n = 27$$

Hence, the number of terms of the given AP is 27.

14. Let the given AP contains n terms.

First term, a = 5 Last term, l = 45 S_n = 400 $\Rightarrow \frac{n}{2} [a + l] = 400$ $\Rightarrow \frac{n}{2} [5 + 45] = 400$ $\Rightarrow n \times 50 = 800$ $\Rightarrow n = 16$ Thus, the given AP contains 16 terms.

Let d be the common difference of the given AP.

then,

 $T_{16} = 45$

 \Rightarrow a + 15d = 45

 \Rightarrow 5 + 15d = 45 \Rightarrow 15d = 40 \Rightarrow d = $\frac{40}{15} = \frac{8}{3}$. Therefore, common difference of the given AP is $\frac{8}{3}$. 15. Let first term be a and common difference be d. Here, $a_{14} = 2a_8$ a + 13d = 2(a + 7d)a + 13d = 2a + 14da = - d...(i) $a_6 = -8$ $a + 5d = -8 \dots (ii)$ Putting the value of a from (i) in (ii), we get -d + 5d = -84d = -8d = -2 Put d = -2 in (i) a = -(-2)a = 2 So a = 2, d = -2 $S_{20} = rac{20}{2} [2 imes 2 + (20 - 1)(-2)] \ = 10 [4 + 19 imes (-2)]$ = 10(4 - 38) $= 10 \times (-34)$ = - 340. Which is the required sum of first 20 terms. 16. The given AP is 17, 14, 11,, – 40 Here, a = 17

Here, a = 17 d = 14 - 17 = -3 l = -40Let there be n terms between in the given AP Then, nth term = -40 $\Rightarrow a + (n - 1)d = -40$ $\therefore a_n = a + (n - 1)d$ $\Rightarrow 17 + (n - 1)(-3) = -40$

$$\Rightarrow (n - 1) (-3) = -40 - 17$$

$$\Rightarrow (n - 1) (-3) = -57$$

$$\Rightarrow n - 1 = \frac{-57}{-3}$$

$$\Rightarrow n - 1 = 19$$

$$\Rightarrow n = 19 + 1$$

$$\Rightarrow n = 20$$

Hence, there are 20 terms in the given AP.
Now, 6th term from the end

$$= (20 - 6 + 1)$$
th term from the beginning

$$= 15$$
th term from the beginning

$$= a + (15 - 1)d \therefore a_n = a + (n - 1)d$$

$$= 17 + 14 (-3)$$

$$= 17 - 42$$

$$= -25$$

Hence, the 6th term fr<mark>om t</mark>he end of the given AP is -25.

- 17. According to the question, we have to find the value of x. We are given an AP, namely 1,2,3,..., (x -1), x, (x +1),..., 49 such that 1 + 2 + 3 +... + (x -1) = (x +1) + (x + 2) +... + 49. Thus, we have $S_{x-1} = S_{49} - S_x$... (i) Using the formula, $S_n = \frac{n}{2}$ (a + 1) in (i), we have, $\frac{(x-1)}{2} \cdot \{1 + (x - 1)\} = \frac{49}{2} \cdot (1 + 49) - \frac{x}{2} \cdot (1 + x)$ $\Rightarrow \frac{x(x-1)}{2} + \frac{x(x+1)}{2} = 1225$ $\Rightarrow 2x^2 = 2450 \Rightarrow x^2 = 1225 \Rightarrow x = \sqrt{1225} = 35$ Hence, x = 35.
- 18. According to the question,

Sum of n terms of the A.P. $S_n = 3n^2 + 4n$ $S_1 = 3 \times 1^2 + 4 \times 1 = 7 = t_1 \dots (i)$ $S_2 = 3 \times 2^2 + 4 \times 2 = 20 = t_1 + t_2 \dots (i)$ $S_3 = 3 \times 3^2 + 4 \times 3 = 39 = t_1 + t_2 + t_3 \dots (iii)$ From (i), (ii), (iii) t₁ = 7, t₂ = 13, t₃ = 19

Common difference, d = 13 - 7 = 6

 $25^{\rm th}$ of the term of this A.P., t $_{25}$ = 7 + (25 - 1)6

= 7 + 144 = 151

- : The 25th term of the A.P. is 151.
- 19. Consider the A.P. whose first term and common difference are 'a' and 'd' respectively. If sum of first 6 terms of an A.P. is 36.

S₆ = 36
∴
$$\frac{6}{2}$$
 [2a + (6 - 1)d] = 36 [∴ S_n = $\frac{n}{2}$ [2a + (n - 1)d]
⇒ 3[2a + 5d] = 36
⇒ 2a + 5d = $\frac{36}{3}$
⇒ 2a + 5d = 12 ...(i)
If sum of first 16 terms is 256,
So, S₁₆ = 256
⇒ $\frac{16}{2}$ [2a + (16 - 1)d] = 256
⇒ 8[2a + 15d] = 256
⇒ 2a + 15d = $\frac{256}{8}$
⇒ 2a + 15d = 32 ...(ii)
Subtracting (i) from (ii), we get
2a + 15d = 32 ...(ii)
2a + 5d = 12 [From (i)]
 $\frac{-2}{10d} = 20$
2a + 15d = 32
2a + 5d = 12
 $\frac{-2}{10d} = 20$
⇒ d = 2
Now, 2a + 5d = 12 [From (i)]
⇒ 2a + 5(2) = 12
⇒ 2a + 10 = 12

 $\Rightarrow 2a = 12 - 10$ $\Rightarrow a = \frac{2}{2}$ $\Rightarrow a = 1$ Hence, a = 1 and d = 2So, $S_{10} = \frac{10}{2} [2a + (10 - 1)d]$ = 5[2(1) + 9(2)] = 5[2 + 18] = 5[20] = 100 $\Rightarrow S_{10} = 100$

Hence, the sum of first 10 terms is 100.

20. Let the first term and the common difference of the AP be a and d respectively.

According to the question, Third term + seventh term = 6 \Rightarrow [a + (3 - 1)d] + [a + (7 - 1)d] = 6 = a + (n - 1)d \Rightarrow (a + 2d) + (a + 6d) = 6 \Rightarrow 2a + 8d = 6 \Rightarrow a + 4d = 3.....(1) Dividing throughout by 2 & (third term) (seventh term) = 8 \Rightarrow (a + 2d) (a + 6d) = 8 \Rightarrow (a + 4d - 2d) (a + 4d + 2d) = 8 \Rightarrow (3 - 2d) (3 + 2d) = 8 \Rightarrow 9 - 4d² = 8 $\Rightarrow 4d^2 = 1 \Rightarrow d^2 = rac{1}{4} \Rightarrow d + \pm rac{1}{2}$ Case I, when $d = \frac{1}{2}$ Then from (1), $a + 4\left(\frac{1}{2}\right) = 3$ \Rightarrow a + 2 = 3 \Rightarrow a = 3 - 2 \Rightarrow a = 1 : Sum of first sixteen terms of the AP = S_{16} $=rac{16}{2}[2a+(16-1)d]::S_n=rac{n}{2}[2a+(n-1)d]$ = 8[2a + 15d] $= 8[2(1) + 15(\frac{1}{2})]$ $=8[12+\frac{15}{2}]$

$$= 8\left[\frac{19}{2}\right]$$

= 4 × 19 = 76
Case II. When $d = -\frac{1}{2}$
Then from (1),
 $a + 4\left(-\frac{1}{2}\right) = 3$
 $\Rightarrow a - 2 = 3 \Rightarrow a = 3 + 2 \Rightarrow a = 5$
 \therefore Sum of first sixteen terms of the AP = S₁₆
 $= \frac{16}{2}[2a + (16 - 1)d] \therefore S_n = \frac{n}{2}[2a + (n - 1)d]$

$$= \frac{32}{2} [2a + (16 - 1)d] \therefore S_n = \frac{3}{2} [2a + (n - 1)d]$$
$$= 8[2a + 15d] = 8 \left[2(5) + 15\left(-\frac{1}{2}\right)\right] = 8 \left[10 - \frac{15}{2}\right] = 8 \left[\frac{5}{2}\right] = 20$$

