

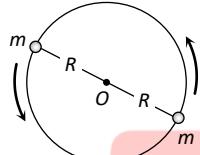
ANSWER KEY											
1.	(C)	2.	(A)	3.	(A)	4.	(A)	5.	(B)	6.	(B)
8.	(D)	9.	(B)	10.	(D)	11.	(A)	12.	(B)	13.	(A)
15.	(B)	16.	(A)	17.	(C)	18.	(B)	19.	(D)	20.	(C)
22.	(D)	23.	(C)	24.	(B)	25.	(B)	26.	(D)	27.	(B)
29.	(A)	30.	(A)	31.	(A)	32.	(D)	33.	(B)	34.	(A)
36.	(D)	37.	(C)	38.	(C)	39.	(C)	40.	(D)	41.	(C)
43.	(C)	44.	(C)	45.	(B)	46.	(C)	47.	(A)	48.	(D)
50.	(C)										

**SOLUTIONS**

**SECTION-A**

1. (C)

**Sol.** Centripetal force provided by the gravitational force of attraction between two particles



$$\text{i.e. } \frac{mv^2}{R} = \frac{Gm \times m}{(2R)^2}$$

$$\Rightarrow v = \frac{1}{2} \sqrt{\frac{Gm}{R}}$$

2. (A)

**Sol.**  $k$  represents gravitational constant which depends only on the system of units.

3. (A)

**Sol.** Gravitational force does not depend on the medium.

4. (A)

**Sol.**  $g = \frac{4}{3}\pi\rho GR$ . If  $\rho = \text{constant}$  then  $\frac{g_1}{g_2} = \frac{R_1}{R_2}$

5. (B)

**Sol.** Time of decent  $t = \sqrt{\frac{2h}{g}}$ . In vacuum no other force works except gravity so time period will be exactly equal.

6. (B)

**Sol.** We know that  $g = \frac{GM}{R^2}$

$$\text{On the planet } g_p = \frac{GM/7}{R^2/4} = \frac{4g}{7} = \frac{4}{7}g$$

$$\text{Hence weight on the planet} \\ = 700 \times \frac{4}{7} = 400 \text{ gm wt}$$

7. (C)  
**Sol.**

For the condition of weightlessness at equator

$$\omega = \sqrt{\frac{g}{R}} \therefore \omega = \sqrt{\frac{1}{640 \times 10^3}} = \frac{1}{800} \text{ rad/s}$$

8. (D)

**Sol.**  $g = \frac{4}{3}\pi\rho GR \therefore \frac{g_1}{g_2} = \frac{R_1\rho_1}{R_2\rho_2}$

9. (B)

**Sol.**  $g' = g \left( \frac{R}{R+h} \right)^2 \Rightarrow \text{when } h=R \text{ then } g' = \frac{g}{4}$

So the weight of the body at this height will become one-fourth.

10. (D)

**Sol.** The correct option is D 100 N

$$g' = g \left( 1 - \frac{d}{R} \right)$$

$$\Rightarrow g' = g \left( 1 - \frac{R/2}{R} \right)$$

$$\Rightarrow mg' = mg \left( \frac{1}{2} \right)$$

$$\therefore W' = \frac{200}{2} = 100 \text{ N}$$

11. (A)

**Sol.**  $g' = g \left( \frac{R}{R+h} \right)^2 = g \left( \frac{R}{R + \frac{R}{2}} \right)^2 = \frac{4}{9}g$

$$\therefore W' = \frac{4}{9} \times W = \frac{4}{9} \times 72 = 32 \text{ N}$$

12. (B)

**Sol.**  $g' = g \left( 1 - \frac{d}{R} \right) \Rightarrow \frac{g}{n} = g \left( 1 - \frac{d}{R} \right) \Rightarrow d = \left( \frac{n-1}{n} \right) R$

13. (A)

$$\text{Sol. } g' = g \left( \frac{R}{R+h} \right)^2 = \frac{g}{\left( 1 + \frac{h}{R} \right)^2}$$

14. (B)

**Sol.** Using  $g = \frac{GM}{R^2}$  we get  $g_m = g/5$

15. (B)

$$\text{Sol. } \frac{g'}{g} = \frac{M'}{M} \times \frac{R^2}{R'^2} = \frac{1}{2} \times \frac{4}{1} = \frac{2}{1}$$

16. (A)

**Sol.** Gravitational potential at mid point

$$V = \frac{-GM_1}{d/2} + \frac{-GM_2}{d/2}$$

$$\text{Now, } PE = m \times V = \frac{-2Gm}{d} (M_1 + M_2)$$

[ $m$  = mass of particle]

So, for projecting particle from mid point to infinity

$$KE = |PE|$$

$$\Rightarrow \frac{1}{2}mv^2 = \frac{2Gm}{d}(M_1 + M_2)$$

$$\Rightarrow v = 2\sqrt{\frac{G(M_1 + M_2)}{d}}$$

17. (C)

$$\text{Sol. } \frac{G \times 100}{x^2} = \frac{G \times 10000}{(1-x)^2}$$

$$\Rightarrow \frac{10}{x} = \frac{100}{1-x} \Rightarrow x = \frac{1}{11}m$$

18. (B)

$$\text{Sol. } v_e = \sqrt{\frac{2GM}{R}} \Rightarrow v_e \propto \sqrt{M} \text{ if } R = \text{constant}$$

If the mass of the planet becomes four times then escape velocity will become 2 times.

19. (D)

**Sol.** Change in potential energy in displacing a body from  $r_1$  to  $r_2$  is given by

$$\Delta U = GMm \left[ \frac{1}{r_1} - \frac{1}{r_2} \right] = GMm \left( \frac{1}{2R} - \frac{1}{3R} \right) = \frac{GMm}{6R}$$

20. (C)

$$\text{Sol. } \frac{v_p}{v_e} = \sqrt{\frac{M_p}{M_e} \times \frac{R_p}{R_e}} = \sqrt{8 \times \frac{1}{2}} = 2$$

$$\therefore v_p = 2 \times v_e = 22.4 \text{ km/s}$$

21. (C)

$$\text{Sol. On earth } v_e = \sqrt{\frac{2GM}{R}} = 11.2 \text{ km/s}$$

$$\text{On moon } v_m = \sqrt{\frac{2GM \times 4}{81 \times R}} = \frac{2}{9} \sqrt{\frac{2GM}{R}} \\ = \frac{2}{9} \times 11.2 = 2.5 \text{ km/s}$$

22. (D)

**Sol.** Escape velocity does not depends upon the angle of projection.

23. (C)

$$\text{Sol. } v = \sqrt{2gR} \Rightarrow \frac{v_p}{v_e} = \sqrt{\frac{g_p}{g_e} \times \frac{R_p}{R_e}} = \sqrt{1 \times 4} = 2 \\ \Rightarrow v_p = 2 \times v_e = 2 \times 11.2 = 22.4 \text{ km/s}$$

24. (B)

**Sol.** For a moving satellite kinetic energy  $= \frac{GMm}{2r}$

$$\text{Potential energy} = \frac{-GMm}{r}$$

$$\therefore \frac{\text{Kinetic energy}}{\text{Potential energy}} = \frac{1}{2}$$

25. (B)

$$\text{Sol. } v_e = \sqrt{2gR} \text{ and } v_0 = \sqrt{gR} \therefore \sqrt{2} v_0 = v_e$$

26. (D)

**Sol.** Escape velocity from surface of earth

$$v_e = \sqrt{2gR}$$

$$= \sqrt{2 \times 9.8 \times 6.4 \times 10^6} = 11.2 \times 10^3 \text{ m/s}$$

27. (B)

$$\text{Sol. } v = \sqrt{\frac{GM}{R}} \Rightarrow \frac{v_A}{v_B} = \sqrt{\frac{R_B}{R_A}} = \sqrt{\frac{R}{4R}} = \frac{1}{2}$$

$$\therefore \frac{v_A}{v_B} = \frac{3V}{v_B} = \frac{1}{2} \therefore v_B = 6V$$

28. (B)

$$\text{Sol. } v = \sqrt{\frac{GM}{r}}$$

29. (A)

**Sol.** Escape velocity is same for all angles of projection.

30. (A)

**Sol.**  $w = mg \{g = 0 \text{ for artificially satelite}\}$   
So  $w = 0$  for astronaut.

<p><b>31.</b> (A)</p> <p><b>Sol.</b> <math>v = \sqrt{\frac{GM}{r}} = \sqrt{\frac{6.67 \times 10^{-11} \times 6 \times 10^{24}}{384000 \times 10^3}} = 1 \text{ km/s}</math></p>	<p><b>42.</b> (B)</p> <p><b>Sol.</b> <math>T_2 = T_1 \left( \frac{R_2}{R_1} \right)^{3/2} = 1 \times (2)^{3/2} = 2.8 \text{ year}</math></p>
<p><b>32.</b> (D)</p> <p><b>Sol.</b> <math>v_0 = \sqrt{\frac{GM}{r}}</math></p>	<p><b>43.</b> (C)</p>
<p><b>33.</b> (B)</p> <p><b>Sol.</b> Gravitational force provides the required centripetal force for orbiting the satellite  <math>\frac{mv^2}{R} = \frac{K}{R}</math> because <math>(F \propto \frac{1}{R})</math>  <math>\therefore v \propto R^\circ</math></p>	<p><b>44.</b> (C)</p> <p><b>Sol.</b> <math>g = \frac{GM}{R^2}</math>. If mass remains constant then  <math>g \propto \frac{1}{R^2}</math>  % increase in <math>g = 2(\% \text{ decrease in } R) = 2 \times 1\% = 2\%</math>.</p>
<p><b>34.</b> (A)</p> <p><b>Sol.</b> Potential energy =  <math display="block">\frac{-GMm}{r} = \frac{GMm}{R_e + h} = \frac{-GMm}{2R_e}</math>  <math>= -\frac{gR_e^2 m}{2R_e} = -\frac{1}{2} mgR_e = -0.5mgR_e</math></p>	<p><b>45.</b> (B)</p> <p><b>Sol.</b> <math>\Delta U = \frac{mgh}{1 + \frac{h}{R}} = \frac{1}{2} mgR \text{ (since } h = R\text{)}</math></p>
<p><b>35.</b> (B)</p> <p><b>Sol.</b> <math>T^2 \propto r^3</math>  It depends on distance.</p>	<p><b>46.</b> (C)</p> <p><b>Sol.</b> Kepler's law <math>T^2 \propto R^3</math></p>
<h2>SECTION-B</h2>	
<p><b>36.</b> (D)</p> <p><b>Sol.</b> <math>T_2 = T_1 \left( \frac{R_2}{R_1} \right)^{3/2} = T_1 (4)^{3/2} = 8T_1 = 40 \text{ hr}</math></p>	<p><b>47.</b> (A)</p> <p><b>Sol.</b> If a pendulum is suspended in a lift and lift is moving downward with some acceleration <math>a</math>, then time period of pendulum is given by, <math>T = 2\pi \sqrt{\frac{l}{g-a}}</math>.  In the case of free fall, <math>a=g</math> then <math>T=\infty</math> i.e., the time period of pendulum becomes infinite.</p>
<p><b>37.</b> (C)</p> <p><b>Sol.</b> <math>\frac{T_1}{T_2} = \left( \frac{R_1}{R_2} \right)^{3/2} = \left( \frac{10^{13}}{10^{12}} \right)^{3/2} = (1000)^{1/2} = 10\sqrt{10}</math></p>	<p><b>48.</b> (D)</p> <p><b>Sol.</b> <math>v_e = \sqrt{\frac{2GM}{R}} = \sqrt{\frac{2GM}{R} \times \frac{4}{3}\pi R^3 \rho}</math>  <math>= \sqrt{\frac{8\pi G \rho}{3} R^2}</math>  <math>\Rightarrow v_e \propto R</math>  <math>\Rightarrow \frac{v_e}{v} = \frac{4R}{R} \Rightarrow v_e = 4v</math></p>
<p><b>38.</b> (C)</p> <p><b>Sol.</b> Areal velocity of the planet remains constant. If the areas <math>A</math> and <math>B</math> are equal then <math>t_1 = t_2</math>.</p>	<p><b>49.</b> (A)</p> <p><b>Sol.</b> Gravitational force <math>F_G = E_g \times m</math>, where <math>E_g</math> = Gravitational field at the given point  <math>E_g = \frac{F_G}{m} = \frac{3}{60 \times 10^{-3}} = 50 \text{ N kg}^{-1}</math></p>
<p><b>39.</b> (C)</p> <p><b>Sol.</b> <math>\frac{T_1}{T_2} = \left( \frac{R_1}{R_2} \right)^{3/2} = \left( \frac{R}{4R} \right)^{3/2} \Rightarrow T_2 = 8T_1</math></p>	<p><b>50.</b> (C)</p> <p><b>Sol.</b> Kepler's law <math>T^2 \propto R^3</math>  <math>g = \frac{GM}{R^2}</math>  <math>g = g_0 \left( 1 + \frac{h}{R} \right)^{-2}</math>  <math>v_e = \sqrt{\frac{2GM}{R}}</math></p>
<p><b>40.</b> (D)</p> <p><b>Sol.</b> Mass of the satellite does not effects on time period  <math display="block">\frac{T_A}{T_B} = \left( \frac{r_1}{r_2} \right)^{3/2} = \left( \frac{r}{2r} \right)^{3/2} = \left( \frac{1}{8} \right)^{1/2} = \frac{1}{2\sqrt{2}}</math></p>	
<p><b>41.</b> (C)</p> <p><b>Sol.</b> <math>T^2 \propto r^3</math>. If <math>r</math> made half then <math>T</math> will become <math>\frac{T}{8}</math>.</p>	