

ANSWER KEY											
1.	(D)	2.	(B)	3.	(B)	4.	(C)	5.	(A)	6.	(D)
8.	(C)	9.	(D)	10.	(C)	11.	(A)	12.	(B)	13.	(B)
15.	(C)	16.	(B)	17.	(D)	18.	(C)	19.	(B)	20.	(D)
22.	(C)	23.	(A)	24.	(C)	25.	(C)	26.	(B)	27.	(A)
29.	(A)	30.	(B)	31.	(C)	32.	(D)	33.	(D)	34.	(A)
36.	(B)	37.	(D)	38.	(B)	39.	(B)	40.	(A)	41.	(D)
43.	(C)	44.	(A)	45.	(A)	46.	(A)	47.	(D)	48.	(A)
50.	(C)										

SOLUTIONS

SECTION-A

1. (D)
Sol. Centre of mass is a point which can lie within or outside the body.

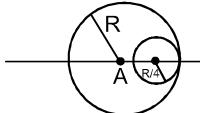
2. (B)
Sol. Centre of mass is nearer to heavier mass

3. (B)
Sol. we have $m_1 r_1 = m_2 r_2$
 $\Rightarrow mr = 2m(3a - r) \Rightarrow r = 2a$

4. (C)

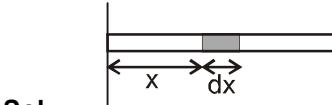
5. (A)

Sol. $A_1 = \pi R^2$ $A_2 = \frac{\pi R^2}{16}$
 $x_1 = 0$ $x_2 = \frac{3R}{4}$



$$x_{cen} = \frac{0 - \frac{\pi R^2}{16} \times \frac{3R}{4}}{\pi R^2 - \frac{\pi R^2}{16}} = -\frac{R}{20}$$

6. (D)



Sol. mass of small element is $dm = \lambda dx = K(x/L)^n dx$

$$x_{CM} = \frac{\int dm \cdot x}{\int dm} = \frac{\int_0^L K \left(\frac{x}{L}\right)^n dx \cdot x}{\int_0^L K \left(\frac{x}{L}\right)^n dx} =$$

$$\frac{(n+1)L}{n+2}$$

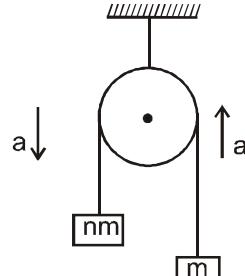
So, graph shown in option (D) is correct.

7. (D)
Sol. In absence of external force both move away from each other to keep the centre of mass at rest.

8. (C)
Sol. $V_{cm} = \frac{M_1 V_1 + M_2 V_2}{M_1 + M_2}$
 $= \frac{200 \times 10\hat{i} + 500(3\hat{i} + 5\hat{j})}{700} = 5\hat{i} + \frac{25}{7}\hat{j}$

9. (D)
Sol. $V_{CM} = 0$, because internal force cannot change the velocity of centre of mass

10. (C)
Sol. $a = \frac{(nm - m)}{nm + m} g$
 $= \frac{(n-1)}{(n+1)} g$
 $a_1 = a_2 = a$



$$a_{cm} = \frac{nma_1 - ma_2}{(nm+m)} = \frac{(n-1)}{(n+1)} \times a$$

$$a_{cm} = \frac{(n-1)^2}{(n+1)^2} g .$$

11. (A)
Sol. Equation of motion
 $M\vec{g} + \vec{R} = M\vec{a}_{cm}$
so $\vec{a}_{cm} = \frac{M\vec{g} + \vec{R}}{M}$

12. (B)

Sol. $\vec{a}_{CM} = \frac{\vec{F}_{ext}}{m}$
 $= \frac{3\hat{i} - 2\hat{j} + 2\hat{k} + (-\hat{i}) + 2\hat{j} - \hat{k} + \hat{i} + \hat{j} + \hat{k}}{6}$
 $\vec{a}_{CM} = \frac{1}{2}\hat{i} + \frac{1}{6}\hat{j} + \frac{1}{3}\hat{k}$
 $= \sqrt{\frac{1}{4} + \frac{1}{9} + \frac{1}{36}} = \sqrt{\frac{9+4+1}{36}} =$
 $\frac{1}{6}\sqrt{13+1}$
 $\frac{\sqrt{14}}{6} \text{ ms}^{-2}$

13. (B)

Sol. Friction force between wedge and block is internal i.e. will not change motion of COM. Friction force on the wedge by ground is external and causes COM to move towards right. Gravitational force (mg) on block brings it downward hence COM comes down.

14. (D)

Sol. Here : Mass of the body $m_1 = m$
Velocity of the first body $u_1 = 312 \text{ m/sec}$
Mass of second body at rest $m_2 = 2m$
Velocity of second body $u_2 = 0$
After combination total mass of the body
 $M = m + 2m = 3m$
Now from the law of conservation of momentum
 $Mv = m_1u_1 + m_2u_2$
(where $M = m + 2m = 3m$)
 $3mv = m \times 3 + 2m \times 0$
 $v = 1 \text{ km/hr}$

15. (C)

Sol. use $m_1v_1 = m_2v_2 = P$
F.E. $= \frac{1}{2}mv_1^2 + \frac{1}{2}m_2v_2^2$
 $= \frac{1}{2}m_1\left(\frac{P}{m_1}\right)^2 + \frac{1}{2}m_2\left(\frac{P}{m_2}\right)^2 = \frac{1}{2}\frac{P^2(m_2+m_1)}{m_1m_2}$.

16. (B)

Sol. $\frac{k_1}{k_2} = \frac{1}{2} \frac{P^2 / (m)}{P^2 / 2(4m)} = 4/1$

17. (D)

Sol. Velocity of man w.r.t. train is zero so kinetic energy of man w.r.t. train = 0

18. (C)

Sol. $\vec{p}_1 + \vec{p}_2 = 0 \Rightarrow \vec{p}_1 = -\vec{p}_2$
 $\Rightarrow |\vec{p}_1| = |\vec{p}_2|$

19. (B)

Sol. When the centre of mass remains at rest, it is possible that different individual forces do individual works though the net resultant force is zero. As work is a scalar quantity, they gets added up.

Also, $\Sigma F_{ext} = 0 \Rightarrow a_{CM} = 0$.

20. (D)

Sol. $\Delta P = P_f - P_i = (-Mv) - (Mv) = -2Mv$

21. (A)

22. (C)

Sol. by energy conservation $\frac{1}{2}mv^2 = \frac{1}{2}(2m)$
 $\left(\frac{v}{2}\right)^2 + \frac{1}{2}kx^2$
 $\Rightarrow x = \sqrt{2mK}$

23. (A)

Sol. Area of F-t curve = A = Impulse.
Impulse = $dP = A = mv - 0$

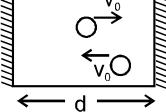
$$\therefore v = \frac{A}{M}$$

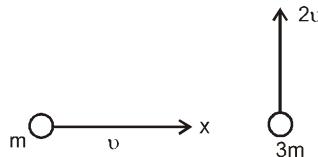
24. (C)

Sol. Impulse $= \int F dt$
= Area under curve
 $= \frac{1}{2}(2)(2) = 2 \text{ kg-m/sec.}$

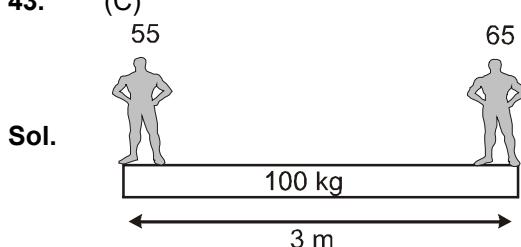
25. (C)

Sol. $| (m_1\vec{v}'_1 + m_2\vec{v}'_2) - (m_1\vec{v}_1 + m_2\vec{v}_2) | =$
| Change in momentum of the two particles |
= | External force on the system | \times time interval
 $= (m_1 + m_2) g(2t_0)$
 $= 2(m_1 + m_2) gt_0$

26.	(B)
Sol.	$t = \frac{2d}{v_0}$ (time for successive collision)
	$N \times t = dP = mv_0 - (-mv_0)$
	$N \times \frac{2d}{v_0} = 2mv_0$
	
	$\therefore N = \frac{mv_0^2}{d}$
27.	(A)
28.	(D)
29.	(A)
Sol.	$v_1 = \frac{(m_1 - em_2)u_1}{m_1 + m_2} + \frac{m_2(1+e)u_2}{m_1 + m_2}$ $= \frac{(m - e2m)u_1}{m + 2m} + \frac{2m(1+e) \times 0}{m + 2m} = 0$ $\Rightarrow 0 = m - e2m \Rightarrow e = 1/2$
30.	(B)
31.	(C)
32.	(D)
Sol.	$0.5 \times v_p + m \times 0 = 5.05 v$ $\therefore \frac{v_f}{v_i} = \frac{0.05}{5} = 10^{-2}$ $\Rightarrow \frac{\frac{1}{2}m(v_f)^2}{\frac{1}{2}m(v_i)^2} = (10^{-2})^2 = 10^{-4}$
33.	(D)
Sol.	Kinetic energy remains conserved in elastic collision
34.	(A)
Sol.	$e = \frac{\text{velocity of separation}}{\text{velocity of approach}} = 1$ for elastic collision.
35.	(D)
Sol.	In an inelastic collision, the particles do not regain their shape and size completely after collision. Some fraction of mechanical energy is retained by the colliding particles in the form of deformation potential energy. Thus, the kinetic energy of particles no longer remains conserved. However, in the absence of external forces, law of conservation of linear momentum still holds good.

SECTION-B	
36.	(B)
Sol.	According to Newton's Law
	$e = \frac{\vec{v}_2 - \vec{v}_1}{\vec{u}_1 - \vec{u}_2}$
	For elastic collision coefficient of restitution
	$\vec{v}_2 - \vec{v}_1 = \vec{u}_1 - \vec{u}_2$
	Statement - 1 is correct Linear momentum is conserved in both elastic & non elastic collision but it's not the explanation of statement -1 so it is not the correct explanation of the statement A.
37.	(D)
Sol.	$F = \mu \frac{dm}{dt} \Rightarrow 210 = 300 \times \frac{dm}{dt}$ $\Rightarrow \frac{dm}{dt} = 0.7 \text{ kg/s.}$
38.	(B)
Sol.	Let Initial thrust of the blast be F then $F - mg = ma$
	$F = m(g + a) = 3.5 \times 10^4 \times (10 + 10)$ $= 7 \times 10^5 \text{ N}$
39.	(B)
Sol.	As no external force is acting on the system, the centre of mass must be at rest i.e. $v_{CM} = 0$.
40.	(A)
Sol.	
	From momentum conservation
	$m\hat{i} + 3m(2v)\hat{j} = (4m)\vec{v}$
	$\vec{v} = \frac{v}{4}\hat{i} + \frac{6}{4}v\hat{j}$
	$= \frac{v}{4}\hat{i} + \frac{3}{2}v\hat{j}$
41.	(D)
Sol.	From momentum conservation
	$mu + 0 = 0 + (4m)V_2 \Rightarrow V_2 = \frac{u}{4}$
	$e = \frac{V_2}{u} = \frac{u_4}{u} = \frac{1}{4} = 0.25$
42.	(C)
Sol.	Statement-2 contradicts Newton's third law and hence is false.

43. (C)



Sol.

There is no external force so com will not shift

44. (A)

$$\text{Sol. } v_{\text{cm}} = \frac{1 \times 2 + \frac{1}{2} \times 6}{1 + 1/2} = \frac{10}{3} \text{ m/sec.}$$

45. (A)

Sol. vector sum of internal forces on system is zero.

46. (A)

47. (D)

Sol. by conservation of linear momentum $P_i = P_f$

$$\Rightarrow mu = \frac{m}{4} \times 0 + \frac{3m}{4} \times V$$

$$\Rightarrow V = \frac{4u}{3}$$

48. (A)

Sol. Impulse = change in momentum = $2 mv$
 $= 2 \times 0.06 \times 4 = 0.48 \text{ kg m/s. Ans.}$

49. (A)

Sol. Momentum conservation
 $5 \times 10 + 20 \times 0 = 5 \times 0 + 20 \times v \Rightarrow v = 2.5 \text{ m/s}$

50. (C)

$$\text{Sol. } m_G = \frac{m_B v_B}{v_G} = \frac{50 \times 10^{-3} \times 30}{1} = 1.5 \text{ kg}$$

P E