

ANSWER KEY											
1.	(B)	2.	(C)	3.	(B)	4.	(B)	5.	(B)	6.	(C)
8.	(D)	9.	(D)	10.	(A)	11.	(B)	12.	(D)	13.	(B)
15.	(C)	16.	(B)	17.	(A)	18.	(B)	19.	(D)	20.	(A)
22.	(B)	23.	(D)	24.	(B)	25.	(D)	26.	(B)	27.	(C)
29.	(D)	30.	(D)	31.	(B)	32.	(A)	33.	(B)	34.	(C)
36.	(C)	37.	(C)	38.	(B)	39.	(D)	40.	(D)	41.	(B)
43.	(B)	44.	(C)	45.	(D)	46.	(A)	47.	(A)	48.	(B)
50.	(D)										

**SOLUTIONS**

**SECTION-A**

1. (B)

**Sol.** Power =  $I^2 R = \left( \frac{I_p}{\sqrt{2}} \right)^2 R = \frac{I_p^2 R}{2}$

2. (C)

**Sol.**  $\nu = \frac{\omega}{2\pi} = \frac{120 \times 7}{2 \times 22} = 19 \text{ Hz}$

$V_{\text{r.m.s.}} = \frac{240}{\sqrt{2}} = 120\sqrt{2} \text{ V}$

3. (B)

**Sol.** In *dc* ammeter, a coil is free to rotate in the magnetic field of a fixed magnet. If an alternating current is passed through such a coil, the torque will reverse its direction each time the current changes direction and the average value of the torque will be zero.

4. (B)

**Sol.**  $i_{\text{r.m.s.}} = \frac{i_o}{\sqrt{2}} = \frac{4}{\sqrt{2}} = 2\sqrt{2} \text{ ampere}$

5. (B)

**Sol.**  $V_0 = \sqrt{2} V_{\text{rms}} = 10\sqrt{2}$

6. (C)

**Sol.**  $V_{\text{rms}} = \frac{200}{\sqrt{2}}, i_{\text{rms}} = \frac{1}{\sqrt{2}}$

$\therefore P = V_{\text{rms}} i_{\text{rms}} \cos \phi = \frac{200}{\sqrt{2}} \cdot \frac{1}{\sqrt{2}} \cos \frac{\pi}{3} = 50 \text{ watt}$

7. (C)

**Sol.**  $i_{\text{rms}} = \sqrt{\frac{i_1^2 + i_2^2}{2}} = \frac{1}{\sqrt{2}}(i_1^2 + i_2^2)^{1/2}$

8. (D)

**Sol.**  $P = Vi \cos \phi$

Phase difference  $\phi = \frac{\pi}{2} \Rightarrow P = \text{zero}$

9. (D)

**Sol.**  $P = V_{\text{rms}} I_{\text{rms}} \cos \phi$ ; since  $\phi = 90^\circ$ . So  $P = 0$

10. (A)

11. (B)

**Sol.**  $Z = \sqrt{R^2 + X_L^2}, X_L = \omega L \text{ and } \omega = 2\pi f$   
 $\therefore Z = \sqrt{R^2 + 4\pi^2 f^2 L^2}$

12. (D)

**Sol.** For the first circuit  $i = \frac{V}{Z} = \frac{V}{\sqrt{R^2 + \omega^2 L^2}}$   
 $\therefore$  Increase in  $\omega$  will cause a decrease in  $i$ .  
For the second circuit  $i = \frac{V}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}}$   
 $\therefore$  Increase in  $\omega$  will cause an increase in  $i$ .

13. (B)

14. (C)

15. (C)

**Sol.**  $Z = \sqrt{R^2 + (X_L - X_C)^2}$   
 $= \sqrt{100^2 + \left( 0.5 \times 100\pi - \frac{1}{10 \times 10^{-6} \times 100\pi} \right)^2}$   
 $= 189.72\Omega$

16. (B)

**Sol.** In non resonant circuits

impedance  $Z = \frac{1}{\sqrt{\frac{1}{R^2} + \left( \omega C - \frac{1}{\omega L} \right)^2}}$ , with rise

in frequency  $Z$  decreases i.e. current increases so circuit behaves as capacitive circuit.

17. (A)

**Sol.** In *LCR* circuit; in the condition of resonance  $X_L = X_C$  i.e. circuit behaves as resistive circuit. In resistive circuit power factor is maximum.

18. (B)

Sol.  $\cos \phi = \frac{R}{Z} = \frac{R}{(R^2 + \omega L^2)^{1/2}}$

19. (D)

20. (A)

21. (A)

Sol. Capacitance of wire

$$C = 0.014 \times 10^{-6} \times 200 = 2.8 \times 10^{-6} F = 2.8 \mu F$$

For impedance of the circuit to be minimum

$$X_L = X_C \Rightarrow 2\pi f L = \frac{1}{2\pi f C}$$

$$\Rightarrow L = \frac{1}{4\pi^2 f^2 C} = \frac{1}{4(3.14)^2 \times (5 \times 10^3)^2 \times 2.8 \times 10^{-6}} \\ = 0.35 \times 10^{-3} H = 0.35 mH$$

22. (B)

Sol. 1. rms value =  $\frac{x_0}{\sqrt{2}}$

2.

$$x_0 \sin \omega t \cos \omega t = \frac{x_0}{2} \sin 2\omega t \Rightarrow \text{rms value} = \frac{x_0}{2\sqrt{2}}$$

3.

$$x_0 \sin \omega t + x_0 \cos \omega t \Rightarrow \text{rms value} = \sqrt{\left(\frac{x_0}{\sqrt{2}}\right)^2 + \left(\frac{x_0}{\sqrt{2}}\right)^2}$$

$$= \sqrt{x_0^2} = x_0$$

23. (D)

Sol. As explained in solution (A) for frequency  $0 - f_r$ ,  $Z$  decreases hence  $(i = V/Z)$ , increases and for frequency  $f_r \rightarrow \infty$ ,  $Z$  increases hence  $i$  decreases.

24. (B)

Sol. The phase angle for the *LCR* circuit is given by

$$\tan \phi = \frac{X_L - X_C}{R} = \frac{\omega L - 1/\omega C}{R}$$

Where  $X_L$ ,  $X_C$  are inductive reactance and capacitive reactance respectively when  $X_L > X_C$  then  $\tan \phi$  is positive i.e.  $\phi$  is positive (between 0 and  $\pi/2$ ). Hence emf leads the current.

25. (D)

Sol.  $P = I_{\text{rms}} V_{\text{rms}} \cos \frac{\pi}{2} = 0$

26. (B)

Sol.  $Z = 100 \Omega$  at  $f = 50 \text{ Hz}$   
 $2\pi f \times L = X_L$

$$\frac{f_1}{f_2} = \frac{X_{L_1}}{X_{L_2}}$$

$$\frac{50}{150} = \frac{100}{X_{L_2}}$$

$$X_{L_2} = 300 \Omega$$

27. (C)

Sol. The current lags the EMF by  $\pi/2$ , so the circuit should contain only an inductor.

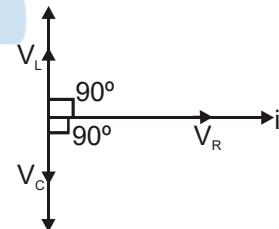
28. (B)

Sol.  $i_{\text{rms}} = \frac{V_{\text{rms}}}{\sqrt{R^2 + \frac{1}{\omega^2 C^2}}}$

when  $\omega$  increases,  $i_{\text{rms}}$  increases so the bulb glows brighter

29. (D)

Sol. In an *LCR* series a.c. circuit, the voltage across inductor  $L$  leads the current by  $90^\circ$  and the voltage across capacitor  $C$  lags behind the current by  $90^\circ$



Hence, the voltage across LC combination will be zero.

30. (D)

Sol. When all (*L,C,R*) are connected then net phase difference =  $60^\circ - 60^\circ = 0^\circ$ . So, there will be resonance.

$$I = \frac{V}{R} = 2 \text{ A}$$

$$P = I^2 R = 400 \text{ watt.}$$

31. (B)

Sol.  $\cos \phi = \frac{R}{Z}$

$$Z_1 = 2R, Z_2 = 4R$$

% change in impedance = 100%

**32. (A)**

**Sol.**  $V = 220 \text{ V}$ ,  $i = 5 \text{ mA}$

Loss of power = 0

because power factor = 0

$$R = 0$$

**33. (B)**

**Sol.**  $P = V_{\text{rms}} \cdot I_{\text{rms}} \cdot \cos\phi$

at maximum power  $\cos\phi = 1$

but at half power  $\cos\phi = \frac{1}{2}$

$$V_{\text{rms}} \times I_{\text{rms}} \times \frac{1}{2} = P$$

$$V_{\text{rms}} \times I_{\text{rms}} \times \frac{1}{2} = \frac{V_{\text{rms}}}{\sqrt{2}} \times I$$

$$I = \frac{I_{\text{rms}}}{\sqrt{2}}$$

$$I = \frac{I_{\text{rms}}}{\sqrt{2}}$$

**34. (C)**

$$\text{Sol. } P = \frac{V^2}{R}$$

$$R = \frac{10 \times 10}{20} = 5\Omega$$

for AC source

$P = 10 \text{ watt}$

$$\therefore P = V_{\text{rms}} \cdot \frac{V_{\text{rms}}}{Z} \times \frac{R}{Z}$$

$$10 = 10 \times \frac{10R}{Z^2}$$

$$Z^2 = 10R$$

$$R^2 + X_L^2 = 10 \times R$$

$$25 + X_L^2 = 10 \times 5$$

$$X_L^2 = 25$$

$$X_L = \sqrt{25} = 5$$

$$\omega \times L = 5$$

$$f = \frac{5 \times 10^2}{2\pi} = \frac{250}{3.14} \approx 80 \text{ Hz}$$

**35. (C)**

**Sol.** Given :  $L = 10 \text{ H}$ ,  $f = 50 \text{ Hz}$ .

For maximum power

$$X_C = X_L$$

$$\frac{1}{\omega C} = L\omega$$

$$C = \frac{1}{\omega^2 L}$$

$$C = \frac{1}{4\pi^2 \times 50 \times 50 \times 10}$$

$$\therefore C = 0.1 \times 10^{-5} \text{ F} = 1 \mu\text{F}$$

## SECTION-B

**36. (C)**

**Sol.** In the condition of resonance

$$X_L = X_C$$

$$\text{or } \omega L = \frac{1}{\omega C}$$

.....(i)

Since, resonant frequency remains unchanged,

$$\text{so, } \sqrt{LC} = \text{constant}$$

$$\text{or } LC = \text{constant}$$

$$\therefore L_1 C_1 = L_2 C_2$$

$$\Rightarrow L \times C = L_2 \times 2C$$

$$\Rightarrow L_2 = \frac{L}{2}$$

**37. (C)**

**38. (B)**

**Sol.** Given :  $i_p = 4 \text{ A}$ ,  $N_p = 140$ ,

$$N_s = 280$$

From the formula

$$\frac{i_p}{i_s} = \frac{N_s}{N_p} \quad \text{or} \quad \frac{4}{i_s} = \frac{280}{140}$$

$$\text{So, } i_s = 2 \text{ A}$$

**39. (D)**

**Sol.**  $P_{\text{out}} = 100 \text{ watt}$

$$P_{\text{in}} = 200 \times 0.6 \text{ watt.}$$

$$= 120 \text{ watt}$$

$$\text{so } \eta = \frac{100}{120} \times 100\% = \frac{5}{6} \times 100\% = \frac{500}{6}\% = 83.33\%$$

**40. (D)**

**Sol.** The current takes  $\frac{T}{4} \text{ sec}$  to reach the peak

value.

In the given question

$$\frac{2\pi}{T} = 200\pi \Rightarrow T = \frac{1}{100} \text{ sec}$$

$$\therefore \text{Time to reach the peak value} = \frac{1}{400} \text{ sec}$$

**41. (B)**

$$\text{Sol. } E = E_0 \cos \omega t = E_0 \cos \frac{2\pi t}{T}$$

$$= 10 \cos \frac{2\pi \times 50 \times 1}{600} = 10 \cos \frac{\pi}{6} = 5\sqrt{3} \text{ volt.}$$

**42.** (D)

**Sol.**  $\because P = V_i \cos \phi$ ,  $\therefore P \propto \cos \phi$

**43.** (B)

**Sol.**  $P = \frac{V_{rms}^2}{R} = \frac{(30)^2}{10} = 90 \text{ W}$

**44.** (C)

**Sol.** Resonance frequency in *radian/second* is

$$\omega = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{8 \times 0.5 \times 10^{-6}}} = 500 \text{ rad/sec}$$

**45.** (D)

**Sol.**  $i = \frac{220}{\sqrt{(20)^2 + (2 \times \pi \times 50 \times 0.2)^2}} = \frac{220}{66} = 3.33 \text{ A}$

**46.** (A)

**Sol.** The voltage across a *L-R* combination is given by

$$V^2 = V_R^2 + V_L^2$$

$$V_L = \sqrt{V^2 - V_R^2} = \sqrt{400 - 144} = \sqrt{256} = 16 \text{ volt.}$$

P

**47.** (A)

**Sol.** Phase angle  $\tan \phi = \frac{\omega L}{R} = \frac{2\pi \times 200}{300} \times \frac{1}{\pi} = \frac{4}{3}$

$$\therefore \phi = \tan^{-1} \frac{4}{3}$$

**48.** (B)

**Sol.** Resonance frequency

$$\omega = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{8 \times 10^{-3} \times 20 \times 10^{-6}}} = 2500 \text{ rad/sec}$$

$$\text{Resonance current} = \frac{V}{R} = \frac{220}{44} = 5 \text{ A}$$

**49.** (C)

**Sol.**  $\cos \phi = \frac{R}{Z} = \frac{10}{20} = \frac{1}{2} \Rightarrow \phi = 60^\circ$

**50.** (D)

**Sol.** Impedance  $Z = \sqrt{R^2 + 4\pi^2\nu^2L^2}$

$$= \sqrt{(12)^2 + 4 \times (3.14)^2 \times (50)^2 \times (0.04)} = 17.37 \text{ A}$$

Now current  $i = \frac{V}{Z} = \frac{220}{17.37} = 12.7 \Omega$

E