

## JEE MAIN ANSWER KEY &amp; SOLUTIONS

SUBJECT :- PHYSICS

CLASS :- 12<sup>th</sup>

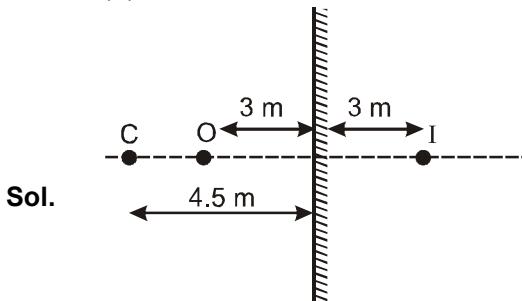
CHAPTER :- RAY OPTICS

PAPER CODE :- CWT-7

ANSWER KEY											
1.	(D)	2.	(A)	3.	(D)	4.	(B)	5.	(B)	6.	(B)
8.	(C)	9.	(C)	10.	(D)	11.	(C)	12.	(A)	13.	(A)
15.	(A)	16.	(D)	17.	(B)	18.	(A)	19.	(C)	20.	(C)
22.	18	23.	16	24.	2	25.	2	26.	225	27.	3
29.	27	30.	400							28.	30

## SOLUTIONS

1. (D)



From diagram distance of camera from image =  
 $4.5 + 3 = 7.5 \text{ m.}$

2. (A)

$$\text{Sol. } m = \frac{v}{u} = \frac{f}{f+u}$$

$$n = \frac{f}{f+u}$$

$$u = \frac{f(1-n)}{n}$$

$$\text{Distance} = \frac{-f(1-n)}{n} = \frac{f(n-1)}{n}$$

3. (D)

Sol. For air

$$\frac{1}{f} = (n_{\text{rel}} - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{10} = (1.52 - 1) \frac{2}{R}$$

$$R = 10 \times 2 \times .52$$

For liquid

$$\frac{1}{f} = \left( \frac{1.52}{1.68} - 1 \right) \frac{2}{R}$$

$$\frac{1}{f} = - \frac{.16}{1.68} \times \frac{2}{10 \times 2 \times .52}$$

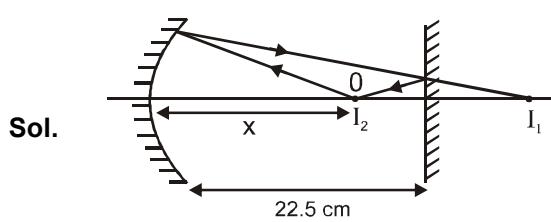
$$f = -54.60 \text{ cm}$$



P

Ans.

4. (B)



$I_1$  is the image formed by concave mirror.

For reflection by concave mirror

$$u = -x, \quad v = -(45 - x), \quad f = -10 \text{ cm},$$

$$\frac{1}{-10} = \frac{1}{-(45-x)} + \frac{1}{-x}$$

$$\frac{1}{10} = \frac{x+45-x}{x(45-x)}$$

$$\Rightarrow x^2 - 45x + 450 = 0$$

$$\Rightarrow x = 15 \text{ cm, } 30 \text{ cm}$$

but  $x = 30 \text{ cm}$  is not acceptable because  
 $x < 22.5 \text{ cm.}$

5. (B)

$$\text{Sol. } P = P_1 + P_2$$

$$2 = 5 + P_2$$

$$P_2 = -3 \text{ D}$$

$$\frac{\omega_1}{\omega_2} = -\frac{f_1}{f_2} = -\frac{P_2}{P_1} = \frac{3}{5}$$

6. (B)

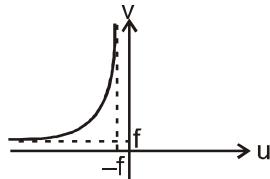
Sol. For a convex lens

$$u = -\text{ve } f = +\text{ve}$$

If  $v = \infty$ ,  $u = f$  and if  $u = -\infty$ ,  $v = f$ .

We have  $v = +\text{ve}$  and  $u = -\text{ve}$

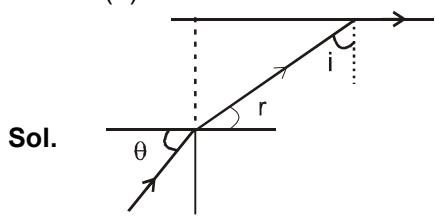
and  $u$  and  $v$  are symmetrical. Hence graph is shown,



7. (B)

Sol. Larger aperture increases the amount of light gathered by the telescope increasing the resolution.

8. (C)



Sol.

$$\sin \theta = \frac{2}{\sqrt{3}} \quad \sin r = \frac{2}{\sqrt{3}} \cos i \quad \dots \text{(i)}$$

$$\text{and } \frac{2}{\sqrt{3}} \sin i = \sin 90^\circ \Rightarrow i = 60^\circ \quad \dots \text{(ii)}$$

$$\text{From (i) and (ii)} \quad \sin \theta = \frac{1}{\sqrt{3}}$$

9. (C)

$$\text{Sol. } \theta = \frac{10}{x}, \quad \theta_1 = \frac{10}{x}(20)$$

Now 20 times nearer

10. (D)

Sol. When  $i = 35^\circ$  and  $e = 79^\circ$  then  $\delta = 40^\circ$

$$\delta = i + e - A$$

$$40^\circ = 35 + 79 - A$$

$$A = 74^\circ$$

Since  $i \neq e$  so  $\delta_{\min}$  will be less than  $40^\circ$

$$n = \frac{\sin\left(\frac{\delta_{\min} + A}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$$n = \frac{\sin\left(\frac{40^\circ + 74^\circ}{2}\right)}{\sin\left(\frac{74^\circ}{2}\right)} = \frac{\sin(57^\circ)}{\sin(37^\circ)} = \frac{0.84}{0.60} = 1.4$$

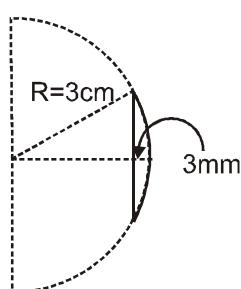
Since  $\delta_{\min}$  will be less than  $40^\circ$  so

n will be less than 1.4

so the closest answer will be 1.5

11. (C)

$$\text{Sol. } n = \frac{3}{2}$$



$$3^2 + (R - 3\text{mm})^2 = R^2$$

$$\Rightarrow 3^2 + R^2 - 2R(3\text{mm}) + (3\text{mm})^2 = R^2$$

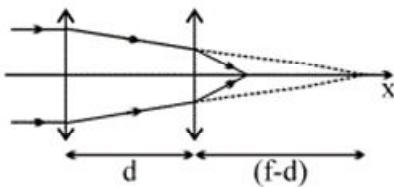
$$\Rightarrow R \approx 15 \text{ cm}$$

$$\frac{1}{f} = \left(\frac{3}{2} - 1\right)\left(\frac{1}{15}\right) \Rightarrow f = 30\text{cm}$$

12. Sol.

(A)

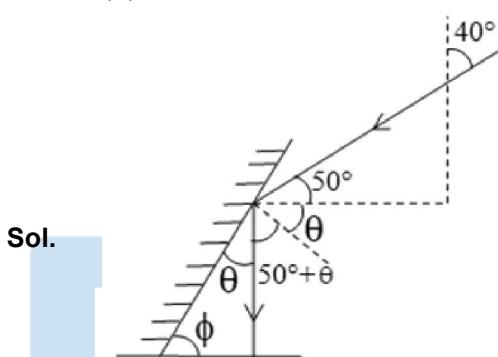
For second lens,



$$\Rightarrow v = \frac{f(f-d)}{2f-d}$$

$$\Rightarrow x = d + v = d + \frac{f(f-d)}{2f-d}$$

13. (A)



Sol.

$$50 + 2\theta = 90, \\ \theta = 20^\circ \\ \phi = 90 - q \\ \phi = 70^\circ$$

14. (D)

Sol. Using Newton formula

$$ab = f^2 \Rightarrow f = \sqrt{ab}$$

15. (A)

Sol.  $C < i_b$

here  $i_b$  is "Brewster's angle" and c is critical angle

$$\sin_c < \sin i_b \text{ since } \tan i_b = \mu_{0,\text{rel}} = \frac{1.5}{\mu}$$

$$\frac{1}{\mu} < \frac{1.5}{\sqrt{\mu^2 + (1.5)^2}} \therefore \sin i_b = \frac{1.5}{\sqrt{\mu^2 + (1.5)^2}}$$

$$\sqrt{\mu^2 + (1.5)^2} < 1.5 \times \mu$$

$$\mu^2 + (1.5)^2 < (\mu \times 1.5)^2$$

$$\mu < \frac{3}{\sqrt{5}}$$

Slab  $\mu = 1.5$

**16.** (D)

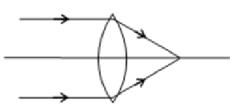
**Sol.** The limit of resolution,

$$\Delta\theta = 1.22\lambda/a = \left(1.22 \times 500 \times 10^{-9} / 200 \times 10^{-2}\right) \\ = 3.05 \times 10^{-7}$$

$$\Delta\theta = 305 \times 10^{-9} \text{ radian}$$

**17.**

(B)



**Sol.**



**18.**

(A)

$$\text{Sol. } f_\ell = \frac{R}{\mu - 1} = 120 \text{ cm}, f_m = R/2 = 30 \text{ cm},$$

$$P = P_L + P_M$$

$$-\frac{1}{f} = \frac{2}{f_\ell} - \frac{1}{f_m} = \frac{1}{60} + \frac{1}{30} = \frac{1}{20}$$

$$f = -20 \text{ cm}$$

**19.**

(C)

$$\text{Sol. } m = \frac{-2.4}{160} = \frac{v}{u}$$

$$v = \frac{-2.4u}{168} = \frac{-u}{70}$$

$$-\frac{70}{u} - \frac{1}{u} = \frac{1}{5.5}$$

$$u = -71 \times 5.5 \text{ cm} = -39 \text{ m}$$



**20.**

(C)

$$\text{Sol. } (1.34/v) - (1/\infty) = (1.34/-1)7.8$$

$$1.34/v = 0.34/7.8$$

$$v = (1.34 \times 7.8)/0.34$$

$$v = 30.7 \text{ mm} = 3.1 \text{ cm}$$

**21.**

8

$$\text{Sol. } \sin \theta = \frac{\frac{4}{3}}{n_{\text{glass}}}$$

$$n_{\text{glass}} = \frac{8}{3\sqrt{3}}$$

$$t = \frac{\frac{9\sqrt{3}}{10}}{\left(\frac{8}{3\sqrt{3}}\right)} = \frac{9\sqrt{3}}{9\sqrt{3} \times 10^8}$$

$$t = \frac{8 \times 10^{-8}}{10} = 8 \times 10^{-9} \text{ s}$$

**22.** 18

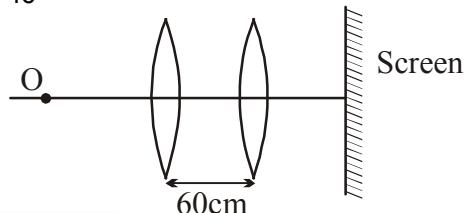
$$\text{Sol. } \frac{1}{15.5} = (1.504 - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f} = (1.434 - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{f}{15.5} = \frac{0.504}{0.434}$$

$$f = 15.5 \times \frac{252}{217} = 18 \text{ cm}$$

**23.** 16



**Sol.**

$$D = 1 \text{ m} \quad d = 0.60 \text{ m}$$

$$f = \frac{D^2 - d^2}{4D} = \frac{1 - (0.6)^2}{4 \times 1} = 16 \text{ cm}$$

$$f = 16 \text{ cm}$$

**24.** 2

$$\text{Sol. } \frac{1.5}{v_1} - \frac{1}{-6} = \frac{1.5 - 1}{R}$$

$$\frac{1.5}{v_1} = \frac{1}{2R} - \frac{1}{6} = \frac{3-R}{6R}$$

$$v_1 = \frac{9R}{3-R}$$

$$u_2 = \frac{9R}{3-R} - R = \frac{6R + R^2}{3-R}$$

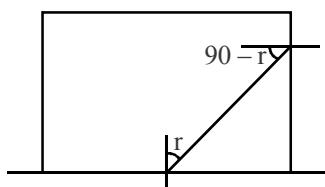
$$\frac{R^2}{1.5} = \frac{32}{3}$$

$$R^2 + 22R - 48 = 0$$

$$R = -\frac{-22 \pm \sqrt{484 + 192}}{2} = 2 \text{ cm}$$

**25.** 2

**Sol.**  $i \sin i = n \sin r$



$$\sin(90^\circ - r) \geq \frac{1}{n}$$

$$\sqrt{1 - \frac{\sin^2 i}{n^2}} \geq \frac{1}{n^2}$$

$$n^2 - 1 \geq \sin^2 i$$

$$n_{\max} = \sqrt{1+1} = \sqrt{2}$$

**26.** 225

$$\text{Sol. } 1^{\text{st}} \text{ refraction: } \frac{1.5}{v_1} - 0 = \frac{0.5}{15}$$

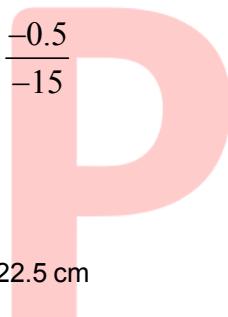
$$v_1 = 45 \text{ cm}$$

$$2^{\text{nd}} \text{ refraction: } \frac{1}{v_2} - \frac{1.5}{15} = \frac{-0.5}{-15}$$

$$\Rightarrow \frac{1}{v_2} = \frac{1}{30} + \frac{1}{10}$$

$$\Rightarrow v_2 = +7.5 \text{ cm}$$

$$\Rightarrow \text{Distance from center} = 22.5 \text{ cm} \\ = 225 \text{ mm}$$



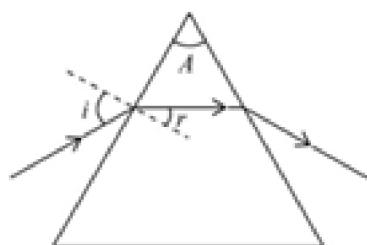
**27.** 3

$$\text{Sol. } \frac{V_{b/f}}{4} = \frac{-8}{4} + \frac{(-v)}{1}$$

$$\Rightarrow \frac{-12}{3} = \frac{-8}{4} + \frac{(-v)}{1}$$

$$\Rightarrow v = 3 \text{ m/s}$$

**28.** 30



**Sol.**

The formula for the refractive index can be given as:

$$n = \frac{\sin i}{\sin r}$$

As the transparent liquid is filled in an equilateral hollow prism, the angle of refraction can be calculated as:

$$r = \frac{A}{2}$$

$$r = \frac{60^\circ}{2}$$

$$R = 30^\circ$$

Substitute the known value of  $n$  and  $r$  in the refractive index formula.

$$\sqrt{2} = \frac{\sin i}{\sin(30^\circ)}$$

$$\sqrt{2} \left( \frac{1}{2} \right) \times \left( \frac{\sqrt{2}}{\sqrt{2}} \right) = \sin i$$

$$\frac{1}{\sqrt{2}} = \sin i$$

$$i = 45^\circ$$

Hence, the angle of minimum deviation for the liquid will be,

$$\delta_{\min} = 2i - A$$

$$= 2(45^\circ) - (60^\circ)$$

$$= 90^\circ - 60^\circ$$

$$= 30^\circ$$

Therefore, the correct answer is 30.

**29.** 27

$$\text{Sol. } 1.5 \sin 60^\circ = n \sin 90^\circ$$

$$1.5 \times \frac{\sqrt{3}}{2} = \frac{\sqrt{x}}{4}$$

$$x = 27$$

**30.** 400

**Sol.** The object after 10 second will be at  $u = -80$  cm.

$$\text{So, } \frac{1}{v} - \frac{1}{80} = -\frac{1}{100}$$

$$\Rightarrow v = \frac{8000}{+20} = 400 \text{ cm}$$