## **JEE MAIN ANSWER KEY & SOLUTIONS**



**14.** (C)  
\n**Sol.** Temperature of junction A is T<sub>A</sub>  
\n
$$
\frac{KA(T - T_A)}{\ell} = \frac{KA(T_A - 0)}{\ell}
$$
\n
$$
\Rightarrow T - T_A = T_A
$$
\n
$$
\Rightarrow T_A = \frac{T}{2}
$$

$$
15.
$$

**15.** (B)

**Sol.** 



- **16.** (C)
- **Sol.** Thermal expansion in isotropic bodies is independent of shape size & availability of cavity.
- **17.** (A)
- **Sol.**   $L - x$  $T-T$ x  $T_1 - T_2 - T - T_2$  $\overline{a}$  $\frac{-T}{\cdot} = \frac{T - T}{\cdot}$  $\Rightarrow$  T<sub>1</sub>L – T<sub>1</sub>x + Tx – TL = Tx – T<sub>2</sub>x  $TL = (T_2 - T_1)x + T_1L$
- **18.** (B)
- **Sol.** Amount of steam required to convert all the ice in water at 100ºC is 3  $\frac{10}{2}$  gm.
- **19.** (A)
- **Sol.** The conductivity more in Cu.

**20.** (C)

**Sol.** Resistance of inner cylinder R<sub>1</sub> = 
$$
\frac{\ell}{k_1 \pi R^2}
$$

 Resistance of outer cylinder  $\overline{a}$ 

$$
R_2 = \frac{\epsilon}{k_2(4\pi R^2 - \pi R^2)}
$$

As inner & outer cylinder in parallel

$$
R_{eq} = \frac{R_1 R_2}{R_1 + R_2}
$$

21. 41  
\n**Sol.** Neglecting other heat losses  
\nHeat lost by water = Heat gained by  
\nthermometer  
\n
$$
\therefore m_1 s_1 (\theta_1 - 40^\circ) = m_2 s_2 (40^\circ - 10^\circ)
$$
  
\n $m_1 = \text{mass of water}$   
\n $m_2 = \text{mass of thermometer}$   
\n $s_1 = \text{specific heat of water}$   
\n $s_2 = \text{specific heat of thermometer}$   
\n $\Rightarrow \theta_1 = 40.6^\circ \text{C}$   
\n $\approx 41^\circ \text{C}$   
\n22. 2  
\n**Sol.**  $x = \ell_0 \alpha t$   
\n $x = 2$   
\n23. 8  
\n**Sol.**  $-\frac{dT}{dt} = \frac{K}{100 \times S_w} (T - T_0)$   
\n $\int_{40}^{35} \frac{-dT}{T - T_0} = \int_{0}^{5} \frac{K}{100 \times S_w} dt$   
\n $\int_{40}^{35} \frac{-dT}{(T - T_0)} = \int_{0}^{5} \frac{dt}{100 \times \rho_t s_\ell}$   
\n $\frac{SK}{100S_w} = \frac{2K}{100 \times \rho_s}$   
\n $\rho_\ell = \frac{4}{5} \text{ g/cm}^3 = \frac{4 \times 10^{-3} \text{ kg}}{5 \times 10^{-6} \text{ m}^3} = \frac{4}{5} \times 10^3$   
\n $= \frac{40}{5} \times 10^2 = 800 \text{kg/m}^3$   
\n24. 1  
\n**Sol.**  $\frac{40 - T}{R_H / 2} = \frac{T - 20}{R_H / 2} + \frac{T - 0}{R_H / 4}$   
\n $T = 15^\circ \text{C}$   
\n $\frac{T - 0}{R_H / 4} = i_H \Rightarrow i_H = 6 \text{ J/s}$   
\n $\frac{H}{R_H / 4} = i_H \Rightarrow i_H = 6 \text{ J/s}$   
\n $\frac{100 - 70}{T_0 \text{C}} = \frac{K}{70^\circ \text{C}} = \frac{100 \text{ C}}{100^\circ$ 

$$
= \frac{100 - T}{R_1}
$$
  
\n
$$
\Rightarrow \frac{100 - T}{T} = \frac{R_1}{R_2} = \frac{K_2}{K_1} = 7/3
$$
  
\n
$$
\Rightarrow 300 - 3T = 7T \Rightarrow T = 30^{\circ} \text{C} \text{ Ans.}
$$

**26.** 3

**Sol.** R =

 $\overline{KA}$ 

 $\ell$ 

 When heat is transferred from first vessel to second, temperature of first vessel decreases while that of second vessel increases. Due to both there reasons, difference between temperature of vessels decreases.

Let at an instant t, the temperature difference between two vessels be  $\theta$ .

$$
H = \frac{\theta}{R} = \frac{KA\theta}{\ell}
$$
  
dQ = Hdt =  $\frac{KA\theta}{\ell}$  dt ....(i)

 Since gases are contained in two vessels, therefore, processes on gases in two vessels are isochoric.

Hence, decrease in temperature of gas in first vessel,

$$
\Delta\theta_1 = \frac{dQ}{nC_v} = \frac{dQ}{2 \times \frac{5R}{2}} = \frac{dQ}{5R}
$$

 Increase in temperature of gas in second vessel is

$$
\Delta\theta_2 = \frac{dQ}{4 \times \frac{3R}{2}} = \frac{dQ}{6R}
$$

∴ Decrease in temperature difference  $(-d\theta) = \Delta\theta_1 + \Delta\theta_2$ 

$$
-\mathbf{d}\theta = \frac{\mathbf{d}Q}{R} \times \frac{11}{30}
$$
  
or 
$$
-\int_{50}^{25} \frac{\mathbf{d}\theta}{\theta} = \frac{KA \times 11}{30\ell R} \int_{0}^{t} dt
$$

 $t = 3$  seconds.

**27.** 8  
**Sol.** 
$$
m = \frac{64}{8} = 8
$$
 gm

$$
28. \qquad 3
$$

**Sol.** Let T = 100<sup>o</sup> C  
\n& T<sub>0</sub> = 50<sup>o</sup>C  
\nHeat = (T – T<sub>0</sub>) 
$$
\frac{A}{\ell}
$$
 (K<sub>S</sub> + K<sub>B</sub>) × 10 × 60  
\n= (100 – 50) ×  $\left(\frac{0.2 \times 10^{-4}}{31 \times 10^{-2}}\right)$  × (46 + 109)  
\n× 10 × 60  
\n= 300 J

**29.** 2  
\n**Sol.** 
$$
\frac{d\theta}{dt} = \frac{100 - \theta}{R_{eq}}
$$
;  $T_B = 40^{\circ}C$ ,  $T_D = 60^{\circ}C$ 

$$
30. 10
$$

$$
\text{Sol.} \quad \xrightarrow{\text{100°C i,} \quad \downarrow \quad i_2} 0^{\circ}\text{C}
$$

 $200^{\circ}$ C

$$
i_1 = \frac{dQ_1}{dt} = \frac{(200 - 100)kA}{x}
$$

$$
= L_v \frac{dm_{\text{stream}}}{dt}
$$

$$
i_2 = \frac{dQ_2}{dt} = \frac{(200 - 0)kA}{(\ell - x)} = L_f \frac{dm_{\text{fusion}}}{dt}
$$

According to problem,

$$
\frac{dm_{\text{steam}}}{dt} = \frac{dm_{\text{fusion}}}{dt}
$$
\n
$$
\frac{100kA}{x L_v} = \frac{200kA}{(\ell - x)L_f}
$$
\n
$$
\Rightarrow x = \frac{2\ell}{29} = 0.1 \text{ m} = 10 \text{ cm}
$$