

JEE MAIN ANSWER KEY & SOLUTIONS

SUBJECT :- MATHEMATICS
CLASS :- 11th
CHAPTER :- STATISTICS

PAPER CODE :- CWT-12

ANSWER KEY

1. (D)	2. (A)	3. (A)	4. (C)	5. (C)	6. (A)	7. (A)
8. (D)	9. (C)	10. (B)	11. (B)	12. (B)	13. (B)	14. (A)
15. (C)	16. (D)	17. (A)	18. (A)	19. (C)	20. (C)	21. 50
22. 21	23. 22	24. 2	25. 31	26. 24	27. 4	28. 1
29. 7	30. 12					

SOLUTIONS

1. (D)
Sol. $\frac{w_1 + w_2 + \dots + w_9}{9} = x \dots(1)$

$\frac{(w_1 + w_2 + \dots + w_9) + w_{10}}{10} = x + \frac{1}{20}x \dots(2)$

From equation (1) & (2)

$w_{10} = \frac{3}{2}x$

Now $\frac{(w_1 + w_2 + \dots + w_9) + w_{10} + w_{11}}{11} = x$

....(3)

From equation (1), (2) and (3)

$w_{11} = \frac{x}{2}$

2. (A)

Sol. Mean = $\frac{\sum_{i=1}^n A + iB}{n} = \frac{A \cdot n + B \cdot \frac{n(n+1)}{2}}{n}$

Mean = $A + B \cdot \frac{(n+1)}{2}$

3. (A)

Sol. $\alpha - \frac{7}{2}, \alpha - 3, \alpha - \frac{5}{2}, \alpha - 2, \alpha - \frac{1}{2}, \alpha + \frac{1}{2}, \alpha + 4, \alpha + 5 (\alpha > 0)$

median = $\frac{\alpha - 2 + \alpha - \frac{1}{2}}{2} = \alpha - \frac{5}{4}$

4. (C)

Sol. Geometric mean

$\frac{M(x_1, x_2, x_3, \dots, x_n)}{M(y_1, y_2, y_3, \dots, y_n)} = \frac{(x_1 \cdot x_2 \cdot x_3 \cdot \dots \cdot x_n)^{\frac{1}{n}}}{(y_1 \cdot y_2 \cdot y_3 \cdot \dots \cdot y_n)^{\frac{1}{n}}}$

$= \left(\frac{x_1}{y_1} \cdot \frac{x_2}{y_2} \cdot \dots \cdot \frac{x_n}{y_n} \right)^{\frac{1}{n}} = M \left(\frac{x_1}{y_1}, \frac{x_2}{y_2}, \frac{x_3}{y_3}, \dots, \frac{x_n}{y_n} \right)$

⇒ While in case of 1 & 2 it is not true always

5. (C)
Sol. Mean of variate 1.2.3, 2.3.4, 3.4.5,, n.(n + 1).(n + 2)
 For sum of series

$T_r = \frac{r(r+1)(r+2)}{4} [(r+3) - (r-1)]$

$\Rightarrow S = \sum_{r=1}^n T_r = \frac{n(n+1)(n+2)(n+3)}{4}$

Mean = $\frac{s}{n} = \frac{(n+1)(n+2)(n+3)}{4}$

6. (A)

Sol. Coefficient of range

$= \frac{\text{difference of extreme values}}{\text{sum of extreme values}} = \frac{10 - 2}{10 + 2} = \frac{2}{3}$

7. (A)

Sol. 34, 38, 42, 44, 46, 48, 54, 55, 63, 70

median = $\frac{46 + 48}{2} = 47$

$\sum |x_i - M| = 13 + 9 + 5 + 3 + 1 + 1 + 7 + 8 + 16 + 23 = 86$

so mean deviation about median = $\frac{86}{10} = 8.6$

8. (D)

Sol. $\bar{x} = \frac{1}{2n+1} [a + (a + d) + \dots + (a + 2nd)]$

$= \frac{1}{2n+1} [(2n+1)a + d(1+2+\dots+2n)]$

$= a + d \cdot \frac{2n}{2} \cdot \frac{(1+2n)}{2n+1} = a + nd$

M.D. from mean = $\frac{1}{2n+1} 2|d|(1+2+\dots+n)$

$= \frac{n(n+1)|d|}{(2n+1)}$

9. (C)

Sol. Coefficient of variation = $0.58 = \frac{\sigma}{\bar{x}}$
 $\sigma(\text{S.D.}) = .58 \times 4 = 2.32$

10. (B)

Sol. $\sum_{i=1}^{10} (x_i - 50)^2 = 250$

$$\sigma = \sqrt{\frac{\sum_{i=1}^{10} (x_i - 50)^2}{10}} = 5$$

coeff. of variation = $\frac{\sigma}{\bar{x}} \times 100 = 10\%$

11. (B)

Sol. 28, 29, 30, 31, 32

Mean = 30

\Rightarrow variance = σ^2

$$= \frac{(30-28)^2 + (30-29)^2 + (30-30)^2 + (30-31)^2 + (30-32)^2}{5}$$

$$\sigma^2 = 2 \Rightarrow \text{S.D.} = +\sqrt{\sigma^2} = \sqrt{2}$$

12. (B)

Sol. $\frac{{}^{2n+1}C_0 + \dots + {}^{2n+1}C_n}{n+1} = \frac{2^{2n}}{n+1}$

13. (B)

Sol. $\bar{x} = \frac{0 \cdot {}^nC_0 + 1 \cdot {}^nC_1 + 2 \cdot {}^nC_2 + \dots + n \cdot {}^nC_n}{{}^nC_0 + {}^nC_1 + {}^nC_2 + \dots + {}^nC_n}$

$$= \frac{n \cdot 2^{n-1}}{2^n} = \frac{n}{2}$$

14. (A)

x_i	f_i	$f_i x_i$	$f_i x_i^2$
0	1	0	0
1	9	9	9
2	7	14	28
3	5	15	45
4	3	12	48
	$\sum f_i = 25$	$\sum f_i x_i = 50$	$\sum f_i x_i^2 = 130$

Sol.

$$\sigma^2 = \left[\frac{\sum f_i x_i^2}{\sum f_i} - \left(\frac{\sum f_i x_i}{\sum f_i} \right)^2 \right]$$

$$= \left[\frac{130}{25} - \left(\frac{50}{25} \right)^2 \right] = 1.2$$

so variance of A = $1.2 < 1.25 =$ variance of B
 so more consistent team = A

15. (C)

Sol. $\frac{\sum x_i}{200} = 25, \quad \frac{\sum y_i}{300} = 10$

$$\Rightarrow \sum x_i = 5000, \quad \sum y_i = 3000$$

$$\sigma_x = 3 \quad \text{and} \quad \sigma_y = 4$$

$$\Rightarrow \frac{\sum x_i^2}{200} - (25)^2 = 9 \quad \text{and} \quad \frac{\sum y_i^2}{300} - (10)^2 = 16$$

$$\Rightarrow \sum x_i^2 = 126800 \quad \text{and} \quad \sum y_i^2 = 34800$$

$$\therefore \sigma = \frac{\sum z_i^2}{n} - \left(\frac{\sum z_i}{n} \right)^2$$

$$= \frac{\sum (x_i^2 + y_i^2)}{500} - \left(\frac{\sum x_i + \sum y_i}{500} \right)^2$$

$$= \frac{161600}{500} - \left(\frac{8000}{500} \right)^2 = 67.2$$

16. (D)

Sol. $(\bar{x}) = 60, \quad (\bar{y}) = 40$
 $(\sigma_x^2) = 16, \quad (\sigma_y^2) = 36$

$$\sigma_x^2 = \frac{\sum x_1^2}{10} - (\bar{x})^2, \quad \sigma_y^2 = \frac{\sum y^2}{10} - (\bar{y})^2$$

$$\sum x_1^2 = 160 + (60)^2 - 10 \quad \sum y_1^2 = 360 + (40)^2 - 10$$

$$\sigma^2(\text{overall}) = \frac{\sum x_1^2 + \sum y_1^2}{20} - \left(\frac{10\bar{x} + 10\bar{y}}{20} \right)^2$$

$$= \frac{520 + 52000}{20} - (50)^2$$

$$\sigma^2 = 2626 - 2500 = 126$$

$$\text{S.D.} = +\sqrt{\sigma^2} = 11.2$$

17. (A)

Sol. Let x_n misread value (x_n) = 10 (x_n)_{actual} = 12

$$\sigma^2 = 3.3 \quad \bar{x} = 11.3$$

$$\Rightarrow \sum_{i=1}^{n-1} x_i = 113 - 10 = 103 = 10(\bar{x}) - 10$$

$$\sigma^2 = \frac{\sum_{i=1}^{n-1} x_i^2 + x_n^2}{10} - (\bar{x})^2$$

$$\sum_{i=1}^{n-1} x_i^2 = -67 + 10(\bar{x})^2 \quad \dots(1)$$

$$\Rightarrow (\sigma^2)_{\text{actual}} = \frac{\sum_{i=1}^n x_i^2 + (x_n)_{\text{actual}}^2}{10} - (\bar{x})_{\text{actual}}^2$$

$$= \frac{-67 + 10(\bar{x})^2 + 144}{10} - \left(\frac{10(\bar{x}) - 10 + 12}{10} \right)^2$$

$$= (\sigma^2)_{\text{actual}} = 3.14$$

18. (A)
Sol. $x_1, x_2, x_3, \dots, x_{2n}, x_{2n+1}, \dots, x_{4n}$
 mean $\bar{x} = \frac{x_1 + x_2 + \dots + x_{4n}}{4n}$
 median = $\frac{x_{2n} + x_{2n+1}}{2}$, which lies between x_{2n} and x_{2n+1}
 \Rightarrow observations below median are x_1, x_2, \dots, x_{2n}
 observations above median are x_{2n+1}, \dots, x_{4n}
 New mean =

$$\frac{(x_1+12)+(x_2+12)+\dots+(x_{2n}+12)+(x_{2n+1}-4)+\dots+(x_{4n}-4)}{4n}$$

$$= \frac{x_1 + x_2 + \dots + x_{4n} + 16n}{4n} = \bar{x} + 4.]$$

19. (C)
Sol. Let they number are a and b, then

$$\frac{1+2+6+a+b}{5} = 4$$

$$9 + a + b = 20$$

$$\Rightarrow a + b = 11 \quad \dots(i)$$

$$\text{variance, } \sigma^2 = \frac{\sum X^2}{N} - \bar{X}^2$$

$$(5.2) = \frac{1+4+36+a^2+b^2}{5} - 16$$

$$= \frac{41+a^2+b^2-80}{5}$$

$$a^2 + b^2 - 39 = 26$$

$$a^2 + b^2 = 65 \quad \dots(ii)$$

Equation (i) and (ii),
 $a = 4, b = 7$ **Ans.]**

20. (C)
Sol. Let the numbers x and y

$$\frac{1+2+6+x+y}{5} = 4 \Rightarrow x + y = 11$$

..... (1)

Variance = 5.2

$$\frac{1^2 + 2^2 + 6^2 + x^2 + y^2}{5} - (\text{mean})^2 = 5.2$$

$$41 + x^2 + y^2 - 80 = 26$$

$$x^2 + y^2 = 65 \quad \dots(2)$$

Solve (1) and (2) negative

$$x = 4, 7$$

$$y = 7, 4$$

21. 50

Sol. Mean of 21 observation $\bar{x} = 40$, so
 Sum of numbers = $21 \times 40 = 840$
 \Rightarrow As numbers greater than median increased by 21, so 10 observations will increase by 21.
 Now sum of all observations = $840 + 10 \times (21) = 1050$

$$\Rightarrow \text{So now new mean is} = \frac{1050}{21} = 50$$

22. 21

Sol. Mean - Mode = 63

As mode = 3 median - 2 mean

$$\Rightarrow \text{mean} - 63 = 3 \text{ median} - 2 \text{ mean}$$

$$\Rightarrow \text{mean} - \text{median} = 21$$

23. 22

Sol. $n = 88$

$$\text{Median} = \frac{44^{\text{th}} \text{ value} + 45^{\text{th}} \text{ value}}{2} = \frac{56 + 57}{2}$$

$$= 56.5$$

M.D.(median)

$$= \frac{\sum_{i=1}^{88} |x_i - 56.5|}{88} = \frac{43.5 + 42.5 + \dots + 0.5 + 0.5 + \dots + 43.5}{88}$$

$$= \frac{1 + 3 + 5 + \dots + 85 + 87}{88} = 22$$

24. 2

Sol. Mean = $\frac{-1+0+4}{3} = 1$

Hence M.D. (about mean)

$$\frac{|-1-1| + |0-1| + |4-1|}{3} = 2$$

25. 31

Sol. $\sum_{i=1}^{20} (x_i - 30) = 20 \Rightarrow \sum_{i=1}^{20} x_i - 20 \times 30 = 20$

$$\sum_{i=1}^{20} x_i = 600 + 20 = 620$$

$$\text{Mean} = \frac{620}{20} = 31 \text{ Ans.}$$

26. 24

Sol. Let two observations are x and y

$$\text{then } \frac{x+y+2+4+10+12+14}{7} = 8$$

$$x+y+42 = 56 \Rightarrow x+y = 14 \quad \dots(A)$$

$$\text{and } \frac{x^2+y^2+4+16+100+144+196}{7}$$

$$- \frac{(x+y+42)^2}{49} = 16$$

$$\Rightarrow \frac{x^2+y^2+460}{7} = 16+64 = 80$$

$$\Rightarrow x^2+y^2 = 560 - 460 = 100 \quad \dots(B)$$

\(\therefore\) on solving (A) & (B) we get $x = 6, y = 8$

27. 4

Sol. $\sigma_x = 3 \Rightarrow \frac{\sum x_i^2}{100} - (\bar{x})^2 = 9$

$$\Rightarrow \sum x_i^2 = 23400$$

$$\sum z_i = 250 \times 15.6 = 3900$$

$$\therefore \sum y_i = \sum z_i - \sum x_i = 3900 - 1500 = 2400$$

$$\sigma_z^2 = 13.44 \Rightarrow \frac{\sum x_i^2 + \sum y_i^2}{250}$$

$$- (15.6)^2 = 13.44 \Rightarrow \sum y_i^2$$

$$= 40800 \Rightarrow \sigma_y$$

$$= \sqrt{\frac{\sum y_i^2}{150} - \left(\frac{\sum y_i}{150}\right)^2} = \sqrt{\frac{40800}{150} - \left(\frac{2400}{150}\right)^2}$$

$$= 4$$

28. 1

Sol. Mean $(\bar{x}) = 4$, variance = 5.2

$$a_1, a_2, a_3 = 1, 2, 3.$$

Let x_1, x_2 are remaining values

$$\text{Mean } \bar{x} = \frac{a_1+a_2+a_3+x_1+x_2}{5}$$

$$\Rightarrow x_1+x_2 = 11 \quad \dots(1)$$

$$\text{variance } \sigma^2 = 5.2 = \frac{a_1^2+a_2^2+a_3^2+x_1^2+x_2^2}{5}$$

$$- (\bar{x})^2 \Rightarrow x_1^2+x_2^2 = 65 \quad \dots(2)$$

$$\Rightarrow |x_1-x_2| = 3$$

$$\Rightarrow \text{So } \lambda = 11 \Rightarrow 10 - x^2 - 2x = \lambda$$

$$\Rightarrow (x+1)^2 = 0 \quad \text{one solution}$$

29. 7

Sol. $\sum x_i = 14$

$$\sum x_i^2 = \left(\sum x_i\right)^2 - 2\sum x_1x_2$$

$$= 196 - 2 \cdot 70 = 56$$

$$\sigma^2 = \frac{1}{n} \left(\sum_{i=1}^n x_i^2\right) - \frac{1}{n^2} \left(\sum_{i=1}^n x_i\right)^2$$

$$\Rightarrow 4n^2 - 56n + (14)^2 = 0$$

$$\Rightarrow 4(n-7)^2 = 0$$

$$\Rightarrow n = 7 \quad \text{Ans.]}$$

30. 12

Sol. $\sigma^2 = \frac{\sum x^2}{n} - (\bar{x})^2$

$$\sigma^2 = \frac{1560}{10} - (\sqrt{12})^2 = 144 \Rightarrow \text{S.D.} = \sqrt{\sigma^2}$$

$$= 12$$