

## Topic :-MATRICES

1. If  $A$  and  $B$  are matrices such that  $AB$  and  $A + B$  both are defined, then
  - a)  $A$  and  $B$  can be any two matrices
  - b)  $A$  and  $B$  are square matrices not necessarily of the same order
  - c)  $A, B$  are square matrices of the same order
  - d) Number of columns of  $A$  is same as the number of rows of  $B$
  
2. Let  $a, b, c$  be any real numbers. Suppose that there are real numbers  $x, y, z$  not all zero such that  $x = cy + bz, y = az + cx,$  and  $z = bx + ay$  have non-zero solution. Then,  $a^2 + b^2 + c^2 + 2abc$  is equal to
  - a) 1
  - b) 2
  - c) -1
  - d) 0
  
3. If  $I_n$  is the identity matrix of order  $n$ , then rank of  $I_n$  is
  - a) 1
  - b)  $n$
  - c) 0
  - d) None of these
  
4. If the matrix  $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & \lambda \end{bmatrix}$  is singular, then  $\lambda$  is equal to
  - a) 3
  - b) 4
  - c) 2
  - d) 5
  
5. If  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ , then  $I + A + A^2 + A^3 + \dots \infty$  equals to
  - a)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
  - b)  $\begin{bmatrix} -1 & -2 \\ -3 & -4 \end{bmatrix}$
  - c)  $\begin{bmatrix} 1/2 & -1/3 \\ -1/2 & 0 \end{bmatrix}$
  - d)  $\begin{bmatrix} -1/4 & 1/3 \\ 1/2 & 0 \end{bmatrix}$
  
6. If  $A$  is a non-singular square matrix of order  $n$ , then the rank of  $A$  is
  - a) Equal to  $n$
  - b) Less than  $n$
  - c) Greater than  $n$
  - d) None of these
  
7. If  $A = \begin{bmatrix} 1 & -2 \\ 4 & 5 \end{bmatrix}$  and  $f(t) = t^2 - 3t + 7$ , then  $f(A) + \begin{bmatrix} 3 & 6 \\ -12 & -9 \end{bmatrix}$  is equal to
  - a)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
  - b)  $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$
  - c)  $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
  - d)  $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$
  
8. The system of linear equations
 
$$x + y + z = 2$$

$$2x + y - z = 3$$

$$3x + 2y + kz = 4$$
 has a unique solution if
  - a)  $k \neq 0$
  - b)  $-1 < k < 1$
  - c)  $-2 < k < 2$
  - d)  $k = 0$

9. The number of solutions of the system of equations  $2x + y - z = 7, x - 3y + 2z = 1, x + 4y - 3z = 5$  is
- a) 0                                  b) 1                                  c) 2                                  d) 3
10. If  $X = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$ , the value of  $X^n$  is equal to
- a)  $\begin{bmatrix} 3n & -4n \\ n & -n \end{bmatrix}$                           b)  $\begin{bmatrix} 2+n & 5-n \\ n & -n \end{bmatrix}$                           c)  $\begin{bmatrix} 3^n & (-4)^n \\ 1^n & (-1)^n \end{bmatrix}$                           d) None of these
11. If  $I_3$  is the identity matrix of order 3, then  $(I_3)^{-1} =$
- a) 0                                  b)  $3 I_3$                                   c)  $I_3$                                   d) Not necessarily exists
12. If  $A = [a_{ij}]$  is a square matrix of order  $n \times n$  and  $k$  is a scalar, then  $|kA| =$
- a)  $k^n|A|$                                   b)  $k|A|$                                   c)  $k^{n-1}|A|$                                   d) None of these
13. If  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ a & b & -1 \end{bmatrix}$ , then  $A^2$  is equal to
- a) Null matrix                          b) Unit matrix                          c)  $-A$                                   d)  $A$
14. If  $A = \begin{bmatrix} \alpha & 0 \\ 1 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 0 \\ 5 & 1 \end{bmatrix}$ , then value of  $\alpha$  for which  $A^2 = B$  is
- a) 1                                  b)  $-1$                                   c) 4                                  d) No real values
15. If  $A$  is a square matrix such that  $A (\text{adj } A) = \begin{bmatrix} 4 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ , then  $|\text{adj } A| =$
- a) 4                                  b) 16                                  c) 64                                  d) 256
16. If  $\omega$  is a complex cube root of unity and  $A = \begin{bmatrix} \omega & 0 \\ 0 & \omega \end{bmatrix}$ , then  $A^{50}$  is
- a)  $\omega^2 A$                                   b)  $\omega A$                                   c)  $A$                                   d) 0
17. If  $A = \begin{bmatrix} 1 & 2 & x \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & -2 & y \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  and  $AB = I_3$ , then  $x + y$  equals
- a) 0                                  b)  $-1$                                   c) 2                                  d) None of these
18. The adjoint of the matrix  $\begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$  is
- a)  $\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$                           b)  $\begin{bmatrix} \sin \theta & \cos \theta \\ \cos \theta & \sin \theta \end{bmatrix}$                           c)  $\begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$                           d)  $\begin{bmatrix} -\sin \theta & \cos \theta \\ \cos \theta & \sin \theta \end{bmatrix}$

19. The inverse matrix of  $A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$  is

a)  $\begin{bmatrix} \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} \\ -\frac{4}{5} & 3 & -1 \\ \frac{5}{2} & -\frac{3}{2} & \frac{1}{2} \end{bmatrix}$

b)  $\begin{bmatrix} \frac{1}{2} & -4 & \frac{5}{3} \\ 1 & -6 & \frac{2}{3} \\ 1 & 2 & -1 \end{bmatrix}$

c)  $\frac{1}{2} \begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \\ 4 & 2 & 3 \end{bmatrix}$

d)  $\frac{1}{2} \begin{bmatrix} 1 & -1 & -1 \\ -8 & 6 & -2 \\ 5 & -3 & 1 \end{bmatrix}$

20. If  $f(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$ , then  $\{f(\theta)^{-1}\}$  is equal to

a)  $f(-\theta)$

b)  $f(\theta)^{-1}$

c)  $f(2\theta)$

d) None of these

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