

Topic :-INVERSE TRIGONOMETRICE FUNCTIONS

1. If a, b, c be positive real number and the value of

$$\theta = \tan^{-1} \sqrt{\frac{a(a+b+c)}{bc}} + \tan^{-1} \sqrt{\frac{b(a+b+c)}{ca}} + \tan^{-1} \sqrt{\frac{c(c+b+c)}{ab}}$$

Then $\tan \theta$ is equal to

- a) 0 b) 1 c) $\frac{a+b+c}{abc}$ d) None of these
2. If $\sin^{-1} x + \sin^{-1} y = \frac{\pi}{2}$, then $\cos^{-1} x + \cos^{-1} y$ is equal to
- a) $\frac{\pi}{2}$ b) $\frac{\pi}{4}$ c) π d) $\frac{3\pi}{4}$

3. $\tan^{-1} \frac{c_1 x - y}{c_1 y + x} + \tan^{-1} \frac{c_2 - c_1}{1 + c_2 c_1} + \tan^{-1} \frac{c_3 - c_2}{1 + c_3 c_2} + \dots + \tan^{-1} \frac{1}{c_n}$ is equal to

- a) $\tan^{-1} \frac{y}{x}$ b) $\tan^{-1} yx$ c) $\tan^{-1} \frac{x}{y}$ d) $\tan^{-1}(x - y)$

4. The value of $\cos \{ \tan^{-1}(\tan 2) \}$, is

- a) $\frac{1}{\sqrt{5}}$ b) $-\frac{1}{\sqrt{5}}$ c) $\cos 2$ d) $-\cos 2$

5. If $\tan^{-1} \frac{x-1}{x+2} + \tan^{-1} \frac{x+1}{x+2} = \frac{\pi}{4}$, then x is equal to

- a) $\frac{1}{\sqrt{2}}$ b) $-\frac{1}{\sqrt{2}}$ c) $\pm \sqrt{\frac{5}{2}}$ d) $\pm \frac{1}{2}$

6. The sum of series

$$\tan^{-1} \frac{1}{1+1+1^2} + \tan^{-1} \frac{1}{1+2+2^2} + \tan^{-1} \frac{1}{1+3+3^2} + \dots$$

is equal to

- a) $\frac{\pi}{4}$ b) $\frac{\pi}{2}$ c) $\frac{\pi}{3}$ d) $\frac{\pi}{6}$

7. The value of 'a' for which $ax^2 + \sin^{-1}(x^2 - 2x + 2) + \cos^{-1}(x^2 - 2x + 2) = 0$ has a real solution, is

- a) $-\frac{2}{\pi}$ b) $\frac{2}{\pi}$ c) $-\frac{\pi}{2}$ d) $\frac{\pi}{2}$

8. If $\tan^{-1} x - \tan^{-1} y = \tan^{-1} A$, then A is equal to

- a) $x - y$ b) $x + y$ c) $\frac{x-y}{1+xy}$ d) $\frac{x+y}{1-xy}$

9. If $\tan^{-1}\left(\frac{a}{x}\right) + \tan^{-1}\left(\frac{b}{x}\right) = \frac{\pi}{2}$, then x is equal to
 a) \sqrt{ab} b) $\sqrt{2ab}$ c) $2ab$ d) ab
10. $\cos^{-1}\frac{1}{2} + 2 \sin^{-1}\frac{1}{2}$ is equal to
 a) $\frac{\pi}{4}$ b) $\frac{\pi}{6}$ c) $\frac{\pi}{3}$ d) $\frac{2\pi}{3}$
11. $4\tan^{-1}\frac{1}{5} - \tan^{-1}\frac{1}{239}$ is equal to
 a) π b) $\pi/2$ c) $\pi/3$ d) $\pi/4$
12. If $2\sin^{-1}x = \sin^{-1}(2x\sqrt{1-x^2})$, then x is equal to
 a) $[-1, 1]$ b) $\left[-\frac{1}{\sqrt{2}}, 1\right]$ c) $\left[-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right]$ d) None of these
13. The value of $\cot\left(\operatorname{cosec}^{-1}\frac{5}{3} + \tan^{-1}\frac{2}{3}\right)$, is
 a) $\frac{4}{17}$ b) $\frac{5}{17}$ c) $\frac{6}{17}$ d) $\frac{3}{17}$
14. Two angles of a triangle are $\cot^{-1}2$ and $\cot^{-1}3$. Then, the third angle is
 a) $\frac{\pi}{4}$ b) $\frac{3\pi}{4}$ c) $\frac{\pi}{6}$ d) $\frac{\pi}{3}$
15. If $e^{[\sin^2\alpha + \sin^4\alpha + \sin^6\alpha + \dots] \log_e 2}$ is a root of equation $x^2 - 9x + 8 = 0$, where $0 < \alpha < \frac{\pi}{2}$, then the principle value of $\sin^{-1}\sin\left(\frac{2\pi}{3}\right)$ is
 a) α b) 2α c) $-\alpha$ d) -2α
16. If $\frac{1}{2} \leq x \leq 1$, then $\cos^{-1}(4x^3 - 3x)$ equals
 a) $3\cos^{-1}x$ b) $2\pi - 3\cos^{-1}x$ c) $-2\pi - 3\cos^{-1}x$ d) None of these
17. If $\sin^{-1}(2x\sqrt{1-x^2}) - 2\sin^{-1}x = 0$, then x belongs to the interval
 a) $[-1, 1]$ b) $[-1/\sqrt{2}, 1/\sqrt{2}]$ c) $[-1, -1/\sqrt{2}]$ d) $[1/\sqrt{2}, 1]$
18. Solution set of $[\sin^{-1}x] > [\cos^{-1}x]$, where $[.]$ denote the greatest integer function, is
 a) $\left[\frac{1}{\sqrt{2}}, 1\right]$ b) $(\cos 1, \sin 1)$ c) $[\sin 1, 1]$ d) None of these
19. If $[\sin^{-1}\cos^{-1}\sin^{-1}x] = 1$, where $[.]$ denotes the greatest integer function, then x belongs to the interval
 a) $[\tan \sin \cos 1, \tan \sin \cos \sin 1]$ b) $(\tan \sin \cos 1, \tan \sin \cos \sin 1)$
 c) $[-1, 1]$ d) $[\sin \cos \tan 1, \sin \cos \sin \tan 1]$
20. The solution of $\tan^{-1}x + 2 \cot^{-1}x = \frac{2\pi}{3}$ is
 a) $-\frac{1}{\sqrt{3}}$ b) $\frac{1}{\sqrt{3}}$ c) $-\sqrt{3}$ d) $\sqrt{3}$

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