

**Topic :-INVERSE TRIGONOMETRIC FUNCTIONS**

1. If  $\theta = \tan^{-1} a, \phi = \tan^{-1} b$  and  $ab = -1$ , then  $(\theta - \phi)$  is equal to
 

a) 0      b)  $\frac{\pi}{4}$       c)  $\frac{\pi}{2}$       d) None of these
2. If the  $(\cos^{-1} x) = \sin(\cot^{-1} \frac{1}{2})$ , then  $x$  is equal to
 

a)  $\pm \frac{5}{3}$       b)  $\pm \frac{\sqrt{5}}{3}$       c)  $\pm \frac{5}{\sqrt{3}}$       d) None of these
3. If  $\sin^{-1} x + \sin^{-1} y + \sin^{-1} z = \pi$ , then  $x^4 + y^4 + z^4 + 4x^2y^2z^2 = k(x^2y^2 + y^2z^2 + z^2x^2)$  Where  $k$  is equal to
 

a) 1      b) 2      c) 4      d) none of these
4.  $\tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right) - \tan^{-1}\left(\frac{2x}{1-x^2}\right)$  is equal to
 

a) 0      b) 1      c)  $\tan^{-1} x$       d)  $\tan^{-1} 2x$
5. If  $\cos^{-1}\sqrt{p} + \cos^{-1}\sqrt{1-p} + \cos^{-1}\sqrt{1-q} = \frac{3\pi}{4}$ , then the value of  $q$  is
 

a) 1      b)  $\frac{1}{\sqrt{2}}$       c)  $\frac{1}{3}$       d)  $\frac{1}{2}$
6. If  $\alpha, \beta$  are the roots of the equation  $6x^2 - 5x + 1 = 0$ , then the value of  $\tan^{-1} \alpha + \tan^{-1} \beta$  is
 

a) 0      b)  $\pi/4$       c) 1      d)  $\pi/2$
7. If  $\alpha = \sin^{-1}\frac{4}{5} + \sin^{-1}\frac{1}{3}$  and  $\beta = \cos^{-1}\frac{4}{5} + \cos^{-1}\frac{1}{3}$ , then
 

a)  $\alpha < \beta$       b)  $\alpha = \beta$       c)  $\alpha > \beta$       d) None of these
8. Solution set of  $[\sin^{-1} x] > [\cos^{-1} x]$ , where  $[.]$  denote the greatest integer function, is
 

a)  $[\frac{1}{\sqrt{2}}, 1]$       b)  $(\cos 1, \sin 1)$       c)  $[\sin 1, 1]$       d) None of these
9. The value of  $\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3$ , is
 

a) 0      b) 1      c)  $\pi$       d)  $-\pi$
10. The greatest and the least values of  $(\sin^{-1} x)^3 + (\cos^{-1} x)^3$  are respectively
 

a)  $-\frac{\pi}{2}, \frac{\pi}{2}$       b)  $-\frac{\pi^3}{8}, \frac{\pi^3}{8}$       c)  $\frac{\pi^3}{32}, \frac{7\pi^3}{8}$       d) None of these

11. If  $\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{3}{4}\right) - \tan^{-1}\left(\frac{x}{3}\right) = 0$ , then  $x$  is equal to  
 a)  $\frac{7}{3}$       b) 3      c)  $\frac{11}{3}$       d)  $\frac{13}{3}$
12.  $\cos[\tan^{-1}\{\sin(\cot^{-1}x)\}]$  is equal to  
 a)  $\sqrt{\frac{x^2+2}{x^2+3}}$       b)  $\sqrt{\frac{x^2+2}{x^2+1}}$       c)  $\sqrt{\frac{x^2+1}{x^2+2}}$       d) None of these
13.  $\tan^{-1}\frac{x}{y} - \tan^{-1}\frac{x-y}{x+y}$  is equal to  
 (where  $x < y > 0$ )  
 a)  $-\frac{\pi}{4}$       b)  $\frac{\pi}{4}$       c)  $\frac{3\pi}{4}$       d) None of these
14. If  $\tan^{-1} 2$  and  $\tan^{-1} 3$  are two angles of a triangle, then the third angle is  
 a)  $\frac{\pi}{2}$       b)  $\frac{\pi}{3}$       c)  $\frac{\pi}{4}$       d)  $\frac{\pi}{6}$
15. If  $\theta$  and  $\phi$  are the roots of the equation  $8x^2 + 22x + 5 = 0$ , then  
 a) Both  $\sin^{-1}\theta$  and  $\sin^{-1}\phi$  are equal  
 b) Both  $\sec^{-1}\theta$  and  $\sec^{-1}\phi$  are equal  
 c) Both  $\tan^{-1}\theta$  and  $\tan^{-1}\phi$  are equal  
 d) None of the above
16. If  $x_1, x_2, x_3, x_4$  are the roots of the equation  $x^4 - x^3 \sin 2\beta - x \cos \beta - \sin \beta = 0$ , then  
 $\tan^{-1}x_1 + \tan^{-1}x_2 + \tan^{-1}x_3 + \tan^{-1}x_4$  is equal to  
 a)  $\beta$       b)  $\frac{\pi}{2} - \beta$       c)  $\pi - \beta$       d)  $-\beta$
17. The value of  $\cos(2 \cos^{-1}x + \sin^{-1}x)$  at  $x = \frac{1}{5}$  is  
 a) 1      b) 3      c) 0      d)  $-\frac{2\sqrt{6}}{5}$
18. Solution of the equation  $\cot^{-1}x + \sin^{-1}\frac{1}{\sqrt{5}} = \frac{\pi}{4}$  is  
 a)  $x = 3$       b)  $x = \frac{1}{\sqrt{5}}$       c)  $x = 0$       d) None of these
19. Let  $\cos(2 \tan^{-1}x) = \frac{1}{2}$ , then the value of  $x$  is  
 a)  $\sqrt{3}$       b)  $\frac{1}{\sqrt{3}}$       c)  $1 - \sqrt{3}$       d)  $1 - \frac{1}{\sqrt{3}}$
20. If  $\sin^{-1}\frac{1}{3} + \sin^{-1}\frac{2}{3} = \sin^{-1}x$ , then the value of  $x$  is  
 a) 0      b)  $\frac{(\sqrt{5} - 4\sqrt{2})}{9}$       c)  $\frac{(\sqrt{5} + 4\sqrt{2})}{9}$       d)  $\frac{\pi}{2}$