

CLASS : XIIth
DATE :

SUBJECT : MATHS
DPP NO. : 10

Topic :-INVERSE TRIGONOMETRIC FUNCTIONS

1. If $a < \frac{1}{32}$, then the number of solutions of $(\sin^{-1} x)^3 + (\cos^{-1} x)^3 = a \pi^3$, is
a) 0 b) 1 c) 2 d) Infinite

2. If $\sqrt{3} + i = (a + ib)(c + id)$, then $\tan^{-1}\left(\frac{b}{a}\right) + \tan^{-1}\left(\frac{d}{c}\right)$ has the value
a) $\frac{\pi}{3} + 2n\pi, n \in I$ b) $n\pi + \frac{\pi}{6}, n \in I$ c) $n\pi - \frac{\pi}{3}, n \in I$ d) $2n\pi - \frac{\pi}{3}, n \in I$

3. If $\tan^{-1}\frac{1-x}{1+x} = \frac{1}{2}\tan^{-1}x$, then the value of x is
a) $\frac{1}{2}$ b) $\frac{1}{\sqrt{3}}$ c) $\sqrt{3}$ d) 2

4. The sum of the infinite series $\cot^{-1} 2 + \cot^{-1} 8 + \cot^{-1} 18 + \cot^{-1} 32 + \dots$ is
a) π b) $\frac{\pi}{2}$ c) $\frac{\pi}{4}$ d) None of these

5. If $y = \cos^{-1}(\cos 10)$, then y is equal to
a) 10 b) $4\pi - 10$ c) $2\pi + 10$ d) $2\pi - 10$

6. The principle value of $\sin^{-1} \tan\left(\frac{-5\pi}{4}\right)$ is
a) $\frac{\pi}{4}$ b) $-\frac{\pi}{4}$ c) $\frac{\pi}{2}$ d) $-\frac{\pi}{2}$

7. The value of $\sum_{r=0}^{\infty} \tan^{-1}\left(\frac{1}{1+r+r^2}\right)$ is equal to
a) $\frac{\pi}{2}$ b) $\frac{3\pi}{4}$ c) $\frac{\pi}{4}$ d) None of these

8. If $-1 \leq x \leq -\frac{1}{2}$, then $\cos^{-1}(4x^3 - 3x)$ equals
a) $3\cos^{-1}x$ b) $2\pi - 3\cos^{-1}x$ c) $-2\pi + 3\cos^{-1}x$ d) None of these

9. If $\tan^{-1}x - \tan^{-1}y = \tan^{-1}A$, then A is equal to
a) $x - y$ b) $x + y$ c) $\frac{x-y}{1+xy}$ d) $\frac{x+y}{1-xy}$

10. If $2\tan^{-1}(\cos x) = \tan^{-1}(2 \operatorname{cosec} x)$, then the value of x is
a) $\frac{3\pi}{4}$ b) $\frac{\pi}{4}$ c) $\frac{\pi}{3}$ d) None of these

11. The number of real solution of $\tan^{-1} \sqrt{x(x+1)} + \sin^{-1} \sqrt{x^2+x+1} = \frac{\pi}{2}$ is
 a) 0 b) 1 c) 2 d) ∞

12. $\cos \left\{ \cos^{-1} \left(-\frac{1}{7} \right) + \sin^{-1} \left(-\frac{1}{7} \right) \right\} =$
 a) $-\frac{1}{3}$ b) 0 c) $\frac{1}{3}$ d) $\frac{4}{9}$

13. The number of triplets (x, y, z) satisfying $\sin^{-1} x + \cos^{-1} y + \sin^{-1} z = 2\pi$, is
 a) 0 b) 2 c) 1 d) Infinite

14. If $\sin^{-1}(1-x) - 2\sin^{-1}x = \frac{\pi}{2}$, then x equals
 a) $0, -\frac{1}{2}$ b) $0, \frac{1}{2}$ c) 0 d) None of these

15. $\cos^{-1} \left(\frac{15}{17} \right) + 2\tan^{-1} \left(\frac{1}{5} \right) =$
 a) $\frac{\pi}{2}$ b) $\cos^{-1} \left(\frac{171}{221} \right)$ c) $\frac{\pi}{4}$ d) None of these

16. If $x < 0$, then $\tan^{-1} \left(\frac{1}{x} \right)$ equals
 a) $\cot^{-1} x$ b) $-\cot^{-1} x$ c) $-\pi + \cot^{-1} x$ d) $-\pi - \cot^{-1} x$

17. If $\cos^{-1} \sqrt{p} + \cos^{-1} \sqrt{1-p} + \cos^{-1} \sqrt{1-q} = \frac{3\pi}{4}$, then the value of q is
 a) 1 b) $\frac{1}{\sqrt{2}}$ c) $\frac{1}{3}$ d) $\frac{1}{2}$

18. $\tan^{-1} \frac{m}{n} - \tan^{-1} \frac{m-n}{m+n}$ is equal to
 a) $\tan^{-1} \frac{n}{m}$ b) $\tan^{-1} \frac{m+n}{m-n}$ c) $\frac{\pi}{4}$ d) $\tan^{-1} \left(\frac{1}{2} \right)$

19. The value of $\sin \left[\frac{\pi}{2} - \sin^{-1} \left(-\frac{\sqrt{3}}{2} \right) \right]$ is
 a) $\frac{\sqrt{3}}{2}$ b) $-\frac{\sqrt{3}}{2}$ c) $\frac{1}{2}$ d) $-\frac{1}{2}$

20. If $\cos^{-1} x > \sin^{-1} x$, then
 a) $x < 0$ b) $-1 < x < 0$ c) $0 \leq x < \frac{1}{\sqrt{2}}$ d) $-1 \leq x < \frac{1}{\sqrt{2}}$