

Topic :-DIFFERENTIATION

1. If $y = \sec^{-1} \frac{x+1}{x-1} + \sin^{-1} \frac{x-1}{x+1}$, then $\frac{dy}{dx}$ is

a) 1 b) 0 c) $\frac{x-1}{x+1}$ d) $\frac{x+1}{x-1}$

2. Let $g(x) = \log f(x)$, where $f(x)$ is a twice differentiable positive function on $(0, \infty)$ such that $f(x+1) = xf(x)$. Then, for $N = 1, 2, 3, \dots$, $g''\left(N + \frac{1}{2}\right) - g''\left(\frac{1}{2}\right)$ is equal to

a) $-4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2} \right\}$ b) $4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N-1)^2} \right\}$
 c) $-4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$ d) $4 \left\{ 1 + \frac{1}{9} + \frac{1}{25} + \dots + \frac{1}{(2N+1)^2} \right\}$

3. If $y = \log_{x^2+4} (7x^2 - 5x + 1)$, then $\frac{dy}{dx}$ is equal to

a) $\log_e (x^2 + 4) \cdot \left\{ \frac{14x-5}{7x^2-5x+1} - \frac{2xy}{x^2+4} \right\}$
 b) $\frac{1}{\log_e (x^2 + 4)} \left\{ \frac{14x-5}{7x^2-5x+1} - \frac{2xy}{x^2+4} \right\}$
 c) $\log_e (7x^2 - 5x + 1) \left\{ \frac{2x}{x^2+4} - \frac{(14x-5)y}{7x^2-5x+1} \right\}$
 d) $\frac{1}{\log_e (7x^2 - 5x + 1)} \left\{ \frac{2x}{x^2+4} - \frac{(14x-5)y}{7x^2-5x+1} \right\}$

4. If $\sin y = e^{-x \cos y} = e$, then $\frac{dy}{dx}$ at $(1, \pi)$ is equal to

a) $\sin y$ b) $-x \cos y$ c) e d) $\sin y - x \cos y$

5. If $y = \tan^{-1} \left(\frac{\sqrt{1+x^2}-1}{x} \right)$, then $y'(0)$ is

a) $\frac{1}{2}$ b) 0 c) 1 d) -1

6. Differential coefficient of $\sqrt{\sec \sqrt{x}}$ is

a) $\frac{1}{4\sqrt{x}} \sec \sqrt{x} \sin \sqrt{x}$ b) $\frac{1}{4\sqrt{x}} (\sec \sqrt{x})^{3/2} \cdot \sin \sqrt{x}$
 c) $\frac{1}{2} \sqrt{x} \sec \sqrt{x} \sin \sqrt{x}$ d) $\frac{1}{2} \sqrt{x} (\sec \sqrt{x})^{3/2} \cdot \sin \sqrt{x}$

7. If $f(x) = \sin x$ and $g(x) = \sin x$, then $g'(1)$ equals

a) 0 b) $-\cos 1$ c) $\cos 1$ d) None of these

8. The derivative of $y = x^{\ln x}$ is
 a) $x^{\ln x} \ln x$ b) $x^{\ln x - 1} \ln x$ c) $2x^{\ln x - 1} \ln x$ d) $x^{\ln x - 2}$
9. If $x = e^t \sin t$, $y = e^t \cos t$, then $\frac{d^2y}{dx^2}$ at $x = \pi$ is
 a) $2e^\pi$ b) $\frac{1}{2}e^\pi$ c) $\frac{1}{2e^\pi}$ d) $\frac{2}{e^\pi}$
10. If $f'(x) = \sin(\log x)$ and $y = f\left(\frac{2x+3}{3-2x}\right)$, then $\frac{dy}{dx}$ equals
 a) $\sin(\log x) \cdot \frac{1}{x \log x}$
 b) $\frac{12}{(3-2x)^2} \sin\left\{\log\left(\frac{2x+3}{3-2x}\right)\right\}$
 c) $\sin\left\{\log\left(\frac{2x+3}{3-2x}\right)\right\}$
 d) None of these
11. If $r = [2\phi + \cos^2(2\phi + \pi/4)]^{1/2}$, then what is the value of the derivative of $dr/d\phi$ at $\phi = \pi/4$?
 a) $2\left(\frac{1}{\pi+1}\right)^{1/2}$ b) $2\left(\frac{2}{\pi+1}\right)^2$ c) $\left(\frac{2}{\pi+1}\right)^{1/2}$ d) $2\left(\frac{2}{\pi+1}\right)^{1/2}$
12. For $|x| < 1$, let $y = 1 + x + x^2 \dots$ to ∞ , then $\frac{dy}{dx}$ equal to
 a) $\frac{x}{y}$ b) $\frac{x^2}{y^2}$ c) $\frac{x}{y^2}$ d) $xy^2 + y$
13. If $f(x+y) = 2f(x)f(y)$, $f'(5) = 1024(\log 2)$ and $f(2) = 8$, then the value of $f'(3)$ is
 a) $64(\log 2)$ b) $128(\log 2)$ c) 256 d) $256(\log 2)$
14. The value of differentiation of e^{x^2} with respect to e^{2x-1} at $x = 1$ is
 a) e b) 0 c) e^{-1} d) 1
15. Let $x = \log_e t$, $t > 0$ and $y + 1 = t^2$. Then, $\frac{d^2x}{dy^2}$ is equal to
 a) $4e^{2x}$ b) $-\frac{1}{2}e^{-4x}$ c) $-\frac{3}{4}e^{5x}$ d) $4e^x$
16. If $y = \cot^{-1}(\cos 2x)^{1/2}$, then the value of $\frac{dy}{dx}$ at $x = \frac{\pi}{6}$ will be
 a) $\left(\frac{2}{3}\right)^{1/2}$ b) $\left(\frac{1}{3}\right)^{1/2}$ c) $(3)^{1/2}$ d) $(6)^{1/2}$
17. If $P(x)$ is a polynomial such that $P(x^2 + 1) = \{P(x)\}^2 + 1$ and $P(0) = 0$, then $P'(0)$ is equal to
 a) -1 b) 0 c) 1 d) None of these
18. If $y = (\cos x^2)^2$, then $\frac{dy}{dx}$ is equal to
 a) $-4x \sin 2x^2$ b) $-x \sin x^2$ c) $-2x \sin 2x^2$ d) $-x \cos 2x^2$
19. Let $f(x) = 2^{2x-1}$ and $g(x) = -2^x + 2x \log 2$. Then the set of points satisfying $f'(x) > g'(x)$, is

a) $(0, 1)$

b) $[0, 1)$

c) $(0, \infty)$

d) $[0, \infty)$

20. $\frac{d}{dx} \left\{ \begin{array}{l} \tan^{-1} \left(\frac{2x}{1-x^2} \right) + \tan^{-1} \left(\frac{3x-x^3}{1-3x^2} \right) \\ - \tan^{-1} \left(\frac{4x-4x^3}{1-6x^2+x^4} \right) \end{array} \right\}$ is equal to

a) $\frac{1}{\sqrt{1-x^2}}$

b) $-\frac{1}{\sqrt{1-x^2}}$

c) $\frac{1}{1+x^2}$

d) $-\frac{1}{1+x^2}$

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