

Topic :-DIFFERENTIAL EQUATIONS

1. The function $f(\theta) = \frac{d}{d\theta} \int_0^\theta \frac{dx}{1 - \cos\theta \cos x}$ satisfies the differential equation
 - a) $\frac{df}{d\theta} + 2f(\theta) = 0$
 - b) $\frac{df}{d\theta} - 2f(\theta) = 0$
 - c) $\frac{df}{d\theta} - 2f(\theta) = \tan\theta$
 - d) $\frac{df}{d\theta} + 2f(\theta)\cot\theta = 0$

2. The solution of $\frac{dy}{dx} = \left(\frac{y}{x}\right)^{1/3}$, is
 - a) $x^{2/3} + y^{2/3} = C$
 - b) $x^{1/3} + y^{1/3} = C$
 - c) $y^{2/3} - x^{2/3} = C$
 - d) $y^{1/3} - x^{1/3} = C$

3. If $x \sin\left(\frac{y}{x}\right) dy = \left[y \sin\left(\frac{y}{x}\right) - y\right] dx$ and $y(1) = \frac{\pi}{2}$, then the value of $\cos\left(\frac{y}{x}\right)$ is equal to
 - a) x
 - b) $\frac{1}{x}$
 - c) $\log x$
 - d) e^x

4. The solution of the differential equation $\frac{dy}{dx} = \frac{y}{x} + \frac{\phi\left(\frac{y}{x}\right)}{\phi\left(\frac{y}{x}\right)}$ is
 - a) $x \phi\left(\frac{y}{x}\right) = k$
 - b) $\phi\left(\frac{y}{x}\right) = kx$
 - c) $y \phi\left(\frac{y}{x}\right) = k$
 - d) $\phi\left(\frac{y}{x}\right) = ky$

5. If $\frac{dy}{dx} = \frac{xy}{x^2 + y^2}$, $y(1) = 1$, then one of the values of x_0 satisfying $y(x_0) = e$ is given by
 - a) $e\sqrt{2}$
 - b) $e\sqrt{3}$
 - c) $e\sqrt{5}$
 - d) $e/\sqrt{2}$

6. Solution of $\frac{dy}{dx} = 3^{x+y}$ is
 - a) $3^{x+y} = c$
 - b) $3^x + 3^y = c$
 - c) $3^{x-y} = c$
 - d) $3^x + 3^{-y} = c$

7. Order of the differential equation of the family of all concentric circles centred at (h,k) is
 - a) 1
 - b) 2
 - c) 3
 - d) 4

8. The solution of $\frac{dy}{dx} = \cos(x+y) + \sin(x+y)$ is
 - a) $\log\left[1 + \tan\left(\frac{x+y}{2}\right)\right] + c = 0$
 - b) $\log\left[1 + \tan\left(\frac{x+y}{2}\right)\right] = x + c$
 - c) $\log\left[1 - \tan\left(\frac{x+y}{2}\right)\right] = x + c$
 - d) None of these

9. The general solution of the differential equation $\frac{dy}{dx} = \frac{(1+y^2)}{xy(1+x^2)}$ is

a) $(1 + x^2)(1 + y^2) = c$
 c) $(1 - x^2)(1 - y^2) = c$

b) $(1 + x^2)(1 + y^2) = cx^2$
 d) $(1 + x^2)(1 + y^2) = cy^2$

10. The general solution of $\frac{dy}{dx} = \frac{2x-y}{x+2y}$ is

a) $x^2 - xy + y^2 = c$ b) $x^2 - xy - y^2 = c$ c) $x^2 + xy - y^2 = c$ d) $x^2 + xy^2 = c$

11. The differential equation representing the family of curves $y^2 = 2c(x + c^{2/3})$, where c is a positive parameter, is of

a) Order 3, degree 3 b) Order 2, degree 4 c) Order 1, degree 5 d) Order 5, degree 1

12. The solution of the differential equation $\frac{dx}{x} + \frac{dy}{y} = 0$ is

a) $xy = c$ b) $x + y = c$ c) $\log x \log y = c$ d) $x^2 + y^2 = c$

13. If $y = (x + \sqrt{1+x})^n$, then $(1 + x^2)\frac{d^2y}{dx^2} + x\frac{dy}{dx}$ is

a) n^2y b) $-n^2y$ c) $-y$ d) $2x^2y$

14. The order of the differential equation whose general solution is given by $y = (c_1 + c_2)\cos(x + c_3) - c_4e^{x+c_5}$ where c_1, c_2, c_3, c_4 and c_5 are arbitrary constants is

a) 5 b) 6 c) 3 d) 2

15. The differential equation obtained by eliminating arbitrary constants from $y = ae^{bx}$ is

a) $y\frac{d^2y}{dx^2} + \frac{dy}{dx} = 0$ b) $y\frac{d^2y}{dx^2} - \frac{dy}{dx} = 0$ c) $y\frac{d^2y}{dx^2} - \left(\frac{dy}{dx}\right)^2 = 0$ d) $y\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 0$

16. The differential equation of all non-horizontal lines in a plane is

a) $\frac{d^2y}{dx^2} = 0$ b) $\frac{dx}{dy} = 0$ c) $\frac{dy}{dx} = 0$ d) $\frac{d^2x}{dy^2} = 0$

17. The degree of the differential equation satisfying $\sqrt{1-x^2} + \sqrt{1-y^2} = a(x-y)$ is

a) 1 b) 2 c) 3 d) None of these

18. The solution of the differential equation $\frac{dy}{dx} = e^{y+x} + e^{y-x}$ is

a) $e^{-y} = e^x - e^{-x} + c$ b) $e^{-y} = e^{-x} - e^x + c$ c) $e^{-y} = e^x + e^{-x} + c$ d) $e^{-y} + e^x + e^{-x} = c$

19. The integrating factor of the differential equation $\frac{dy}{dx} + \frac{1}{x}y = 3x$ is

a) x b) $\ln x$ c) 0 d) ∞

20. The solution of the differential equation $\sec^2 x \tan y dx + \sec^2 y \tan x dy = 0$ is

a) $\tan y \tan x = c$ b) $\frac{\tan y}{\tan x} = c$ c) $\frac{\tan^2 x}{\tan y} = c$ d) None of these