

Topic :-Application of Derivatives

- If $x = t^2$ and $y = 2t$, then equation of the normal at $t = 1$, is
a) $x + y - 3 = 0$ b) $x + y - 1 = 0$ c) $x + y + 1 = 0$ d) $x + y + 3 = 0$
- The side of an equilateral triangle is ' a ' units and is increasing at the rate of λ units/sec. The rate of increase of its area is
a) $\frac{2}{\sqrt{3}} \lambda a$ b) $\sqrt{3} \lambda a$ c) $\frac{\sqrt{3}}{2} \lambda a$ d) None of these
- If a and b are positive numbers such that $a > b$, then the minimum value of $a \sec \theta - b \tan \theta$ ($0 < \theta < \frac{\pi}{2}$) is
a) $\frac{1}{\sqrt{a^2 - b^2}}$ b) $\frac{1}{\sqrt{a^2 + b^2}}$ c) $\sqrt{a^2 + b^2}$ d) $\sqrt{a^2 - b^2}$
- If $y = x^n$, then the ratio of relative errors in y and x is
a) 1 : 1 b) 2 : 1 c) 1 : n d) n : 1
- How many real solutions does the equation $x^7 + 14x^5 + 16x^3 + 30x - 560 = 0$ have?
a) 5 b) 7 c) 1 d) 3
- The function $f(x) = x^3 + ax^2 + bx + c, a^2 \leq 3b$ has
a) One maximum value b) One minimum value
c) No extreme value d) One maximum and one minimum value
- The fixed point P on the curve $y = x^2 - 4x + 5$ such that the tangent at P is perpendicular to the line $x + 2y - 7 = 0$ is given by
a) (3, 2) b) (1, 2) c) (2, 1) d) None of these
- If the area of the triangle, included between the axes and any tangent to the curve $xy^n = a^{n+1}$ is constant, then the value of n is
a) -1 b) -2 c) 1 d) 2

9. The radius of a circular plate is increasing at the rate of 0.01 cm/s when the radius is 12 cm. Then, The rate at which the area increase, is
 a) 0.24π sq cm/s b) 60π sq cm/s c) 24π sq cm/s d) 1.2π sq cm/s
10. If $g(x) = \min(x, x^2)$ where x is real number, then
 a) $g(x)$ is an increasing function
 b) $g(x)$ is a decreasing function
 c) $g(x)$ is a constant function
 d) $g(x)$ is a continuous function except at $x = 0$
11. The angle between the curves $y = a^x$ and $y = b^x$ is equal to
 a) $\tan^{-1} \left(\left| \frac{a-b}{1+ab} \right| \right)$ b) $\tan^{-1} \left(\left| \frac{a+b}{1-ab} \right| \right)$
 c) $\tan^{-1} \left(\left| \frac{\log b + \log a}{1 + \log a \log b} \right| \right)$ d) $\tan^{-1} \left(\left| \frac{\log a - \log b}{1 + \log a \log b} \right| \right)$
12. The function which is neither decreasing nor increasing in $\left(\frac{\pi}{2}, \frac{3\pi}{2} \right)$, is
 a) $\operatorname{cosec} x$ b) $\tan x$ c) x^2 d) $|x - 1|$
13. On the interval $[0, 1]$ the function $x^{25}(1-x)^{75}$ takes its maximum value at the point
 a) 0 b) $\frac{1}{4}$ c) $\frac{1}{2}$ d) $\frac{1}{3}$
14. A function f is defined by $f(x) = e^x \sin x$ in $[0, \pi]$. Which of the following is not correct?
 a) f is continuous in $[0, \pi]$ b) f is differentiable in $[0, \pi]$
 c) $f(0) = f(\pi)$ d) Rolle's theorem is not true in $[0, \pi]$
15. If $xy = c^2$, then minimum value of $ax + by$ is
 a) $c\sqrt{ab}$ b) $2c\sqrt{ab}$ c) $-c\sqrt{ab}$ d) $-2c\sqrt{ab}$
16. If $x - 2y = 4$, the minimum value of xy is
 a) -2 b) 0 c) 0 d) -3
17. The function $f(x) = (9 - x^2)^2$ increasing in
 a) $(-3, 0) \cup (3, \infty)$ b) $(-\infty, -3) \cup (3, \infty)$ c) $(-\infty, -3) \cup (0, 3)$ d) $(-3, 3)$
18. The real number x when added to its inverse gives the minimum value of the sum at x equals to
 a) 2 b) 1 c) -1 d) -2
19. The points on the curve $12y = x^3$ whose ordinate and abscissa change at the same rate, are
 a) $(-2, -2/3), (2, 2/3)$ b) $(-2/3, -2), (2/3, 2)$ c) $(-2, -2/3)$ only d) $(2/3, 2)$ only

20. Let $P(2, 2)$ and $Q(1/2, -1)$ be two points on the parabola $y^2 = 2x$. The coordinates of the point R on the parabola $y^2 = 2x$, where the tangent to the curve is parallel to the chord PQ , are
- a) $(2, -1)$ b) $(1/8, 1/2)$ c) $(\sqrt{2}, 1)$ d) $(-\sqrt{2}, 1)$

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