CLASS : XITh
DATE :

## Solutions

## Topic :-WAVES

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(a)

Here, $\frac{c t}{\lambda}$ is dimensionless and unit of $c t$ is same as that of $x$. Also unit of $\lambda$ is same as that of $A$, which is also the unit of $x$
(a)
$\mathrm{Y}=2 \cos 2 \pi(330 t-x)$
$\omega=2 \pi \times 330$
$T=\frac{1}{330} s$
(c)

Resonance occurs when amplitude is maximumie, when the denominator of this equation is minimum.
(d)

Number of waves per minute $=54$
$\therefore$ Number of waves per second $=54 / 60$
Now $v=n \lambda \Rightarrow n=\frac{54}{60} \times 10=9 \mathrm{~m} / \mathrm{s}$
(a)
$v_{\text {max }}=a \omega=3 \times 10=30$
6 (c)
Resultant amplitude
$A_{R}=2 A \cos \left(\frac{\theta}{2}\right)=2 \times(2 a) \cos \left(\frac{\theta}{2}\right)=4 a \cos \left(\frac{\theta}{2}\right)$
(b)

Let the base frequency be $n$ for closed pipe then notes are $n, 3 n, 5 n \ldots$...
$\therefore$ note $3 n=255 \Rightarrow n=85$, note $5 n=85 \times 5=425$ note $7 n=7 \times 85=595$
(b)
$y_{1}=10^{-6} \sin [100 t+(x / 50)+0.5]$
$y_{2}=10^{-6} \sin \left[100 t+\left(\frac{x}{50}\right)+\left(\frac{\pi}{2}\right)\right]$
Phase difference $\phi$
$=[100 t+(x / 50)+1.57]-[100 t+(x / 50)+0.5]$
$=1.07$ radians
(d)

In $n$ is frequency of first fork, then frequency of the last $(10$ th fork $)=n+4(10-1)=2 n$
$\therefore n=36$ and $2 n=72$
(a)

Phase difference is $2 \pi$ means constrictive interference so resultant amplitude will be maximum
(a)

At nodes pressure change (strain) is maximum
(d)

According to Laplace, the speed of sound in gas is given by
$v=\sqrt{\frac{\gamma R T}{M}}$,
Where $\gamma$ is ratio of specific heats, $M$ the molecular
weight, R the gas constant and T the temperature,
$\therefore \frac{v_{o}}{v_{H}}=\sqrt{\frac{M_{H}}{M_{o}}}$
$\therefore \frac{v_{O}}{v_{H}}=\sqrt{\frac{1}{16}}=\frac{1}{4}$
$\therefore \quad v_{O}: v_{H}=1: 4$
(a)

Here, $u_{s}=50 \mathrm{~ms}^{-1}, v_{L}=0, v=350 \mathrm{~ms}^{-1}$
When source is moving towards observer,
$v^{\prime}=1000$
$v^{\prime}=\frac{u \times v}{u-u_{s}}$
$v=\frac{\left(u-u_{s}\right) v^{\prime}}{u}$
$=\frac{(350-50) 1000}{350}=\frac{6000}{7} \mathrm{~Hz}$
When source is moving away from observer,
$v^{\prime}=\frac{u \times v}{u+v_{s}}$
$=\frac{350}{(350+50)} \times \frac{6000}{7}$
$=750 \mathrm{~Hz}$

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(d)

Frequency is decreasing (becomes half), it means source is going away from the observe.
In this case frequency observed by the observer is
$n^{\prime}=n\left(\frac{v}{v+v_{S}}\right) \Rightarrow \frac{n}{2}=n\left(\frac{v}{v+v_{S}}\right) \Rightarrow v_{S}=v$
(a)

From $n=\frac{1}{l D} \sqrt{\frac{T}{\pi \rho}}$
When radius of string is doubled, Diameter $D$ becomes twice. As $T$ and $\rho$ are same, $n$ becomes $1 / 2$, ie, $n / 2$.
(d)

Here, $A_{1}=A, A_{2}=A, \phi=120^{\circ}$
The amplitude of the resultant wave is
$A_{R}=\sqrt{A_{1}^{2}+A_{2}^{2}+2 A_{1} A_{2} \cos \phi}$
$=\sqrt{A^{2}+A^{2}+2 A A \cos 120^{\circ}}$
$=\sqrt{A^{2}+A^{2}-A^{2}} \quad\left[\because \cos 120^{\circ}=-\frac{1}{2}\right]$
$\therefore A_{R}=A$
(c)

According to the question frequencies of first and last tuning forks are $2 n$ and $n$ respectively.
Hence frequency is given arrangement are as follows

$\Rightarrow 2 n-24 \times 3=n \Rightarrow n=72 \mathrm{~Hz}$
So, frequency of $21^{\text {st }}$ tuning fork
$n_{21}=(2 \times 72-20 \times 3)=84 \mathrm{~Hz}$
(c)
$\frac{I_{1}}{I_{2}}=\frac{4}{1}=\frac{a^{2}}{b^{2}}: \frac{a}{b}=\frac{2}{1}$
$\therefore \frac{I_{\text {max }}}{I_{\text {min }}}=\frac{(a+b)^{2}}{(a-b)^{2}}=\frac{(2+1)^{2}}{(2-1)^{2}}=9$
Now, $L_{1}-L_{2}=10 \log \frac{I_{\text {max }}}{I_{0}}-10 \log \frac{I_{\text {mim }}}{I_{0}}$
$=10 \log \frac{I_{\max }}{I_{\text {min }}}=10 \log 9$
$L_{1}-L_{2}=10 \log 3^{2}=20 \log 3$


| ANSWER-KEY |  |  |  |  |  |  |  |  |  |  |  |  |
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| Q. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |  |
| A. | A | A | C | D | A | C | D | B | B | B |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| Q. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |  |  |
| A. | D | A | A | D | A | D | A | D | C | C |  |  |
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