

DPP

DAILY PRACTICE PROBLEMS

CLASS : XITH
DATE :

Solutions

SUBJECT : PHYSICS
DPP NO. : 5

Topic :- WAVES

1

(a)

$$\text{Loudness, } L = 10 \log_{10} \frac{I}{I_0}$$

$$60 = 10 \log_{10} \frac{I_1}{I_0}$$

$$\Rightarrow \frac{I_1}{I_0} = 10^6 \quad \dots (i)$$

$$\text{similarly, } 30 = 10 \log_{10} \frac{I_2}{I_0}$$

$$\frac{I_2}{I_0} = 10^3 \quad \dots (ii)$$

Dividing Eq. (i) by Eq. (ii), we get

$$\frac{I_1}{I_2} = 1000$$

2

(a)

Path difference for a given phase difference δ is given by

$$\Delta x = \frac{\lambda}{2\pi} \delta$$

$$\text{Given that } \delta = 60^\circ = \frac{\pi}{3}$$

$$\Delta x = \frac{\lambda}{2\pi} \times \frac{\pi}{3} \therefore \Delta x = \frac{\lambda}{6}$$

3

(a)

Velocity of propagation

$$x = \frac{\text{Coefficient of } t}{\text{coefficient of } x} = \frac{2\pi/0.01}{2\pi/0.3} = 30 \text{ms}^{-1}$$

4

(b)

$$\text{If } \rho_H = 1, \text{ then } \rho_{\text{mix}} = \frac{4 \times 1 + 1 \times 16}{(4+1)} = 4$$

$$\frac{v_{\text{mix}}}{v_H} = \sqrt{\frac{\rho_H}{\rho_{\text{mix}}}} = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

$$v_{\text{mix}} = \frac{v_H}{2} = \frac{1224}{2} = 612 \text{ms}^{-1}$$

6 **(b)**

$$\text{Frequency} = \frac{\text{velocity}}{\text{Wavelength}}$$

$$\therefore f_1 = \frac{v}{\lambda_1} = \frac{330}{5} = 66 \text{Hz}$$

$$\text{And } f_2 = \frac{v}{\lambda_2} = \frac{330}{5.5} = 60 \text{Hz}$$

Number of beats per second

$$= f_1 - f_2 = 66 - 60 = 6$$

7 **(d)**

Given,

Progressive wave $y = a \sin(kx - \omega t)$

When reflected by right wall

Progressive wave $y' = a \sin[k(-x) - \omega t]$

Or $y' = a \sin[-(kx + \omega t)]$

Or $y' = a \sin(kx + \omega t)$

9 **(b)**

For hearing beats, difference of frequencies should be less than 10 Hz

10 **(b)**

In close organ pipe

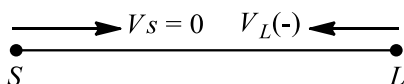
$$v = \frac{v}{4l}$$

So,

$$l = \frac{v}{4v}$$

11 **(a)**

Here, $v_s = 0$ and v_L is negative where v_s is velocity of source and v_L is velocity of listener (aeroplane)



If apparent frequency is v' and v is actual frequency, then

$$v' = \frac{v - (-v_L)}{v} v = \frac{v + v_L}{v} v$$

i. e., $v' > v$

So, apparent frequency will increase, it means apparent wavelength will decrease.

12 (b)

As is clear from figure of question

$$l = \frac{\lambda_p}{4}, \lambda = 4l, n_p = \frac{v}{\lambda_p} = \frac{v}{4l}$$

$$l = \frac{\lambda_q}{2}, \lambda_q = 2l, n_q = \frac{v}{\lambda_q} = \frac{v}{2l}$$

$$l = \lambda_r, \lambda_r = l, n_r = \frac{v}{\lambda_r} = \frac{v}{l}$$

$$l = \frac{3\lambda_s}{4}, \lambda_s = \frac{4l}{3}, n_s = \frac{v}{\lambda_s} = \frac{3v}{4l}$$

$$\therefore n_p : n_q : n_r : n_s = \frac{v}{4l} : \frac{v}{2l} : \frac{v}{l} : \frac{3v}{4l} = 1 : 2 : 3 : 4$$

13 (b)

At $t=0$ and $t=2s$, the shape of $y-x$ graphs are same.

14 (d)

$$Y = 10 \sin \left[\frac{2\pi}{45} t + a \right]$$

If $t=0, y=5 \text{ cm}$

$$5 = 10(\sin a)$$

$$\sin a = \frac{1}{2}$$

$$a = \frac{\pi}{6}$$

If $t=7.5 \text{ s}$

Then total phase =

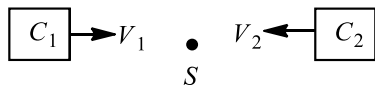
$$\frac{2\pi}{45} \times \frac{15}{2} + \frac{\pi}{6} = \frac{\pi}{3} + \frac{\pi}{6} = \frac{\pi}{2}$$

15 (a)

$$n = \frac{v}{\lambda} \propto v \Rightarrow \frac{n_{MW}}{n_{US}} \approx \frac{3 \times 10^8}{3 \times 10^2} \approx 10^6 : 1$$

16 (a)

Firstly, car will be treated as an observer which is approaching the source. Then, it will be treated as a source, which is moving in the direction of sound.



Hence,

$$f_1 = f_o \left(\frac{v + v_1}{v - v_1} \right)$$

$$f_2 = f_o \left(\frac{v + v_2}{v - v_2} \right)$$

$$\begin{aligned} \therefore f_1 - f_2 &= \left(\frac{1.2}{100}\right) f_o \\ &= f_o \left[\frac{v + v}{v + v_1} - \frac{v + v_2}{v - v_2} \right] \end{aligned}$$

Or

$$\left(\frac{1.2}{100}\right) f_o = \frac{2v(v_1 - v_2)}{(v - v_1)(v - v_2)}, f_o$$

as v_1 and v_2 are very very less than v .

We can write, $(v - v_1)$ or $(v - v_2) \approx v$.

$$\therefore \left(\frac{1.2}{100}\right) f_o = \frac{2(v_1 - v_2)}{v} f_o$$

$$\begin{aligned} \text{Or } (v_1 - v_2) &= \frac{v \times 1.2}{200} \\ &= \frac{300 \times 1.2}{200} = 1.98 \text{ms}^{-1} \\ &= 7.128 \text{kmh}^{-1} \end{aligned}$$

\therefore the nearest integer is 7.

17

(a)

$$y = y_1 + y_2 = a \sin(\omega t - kx) = a \sin(\omega t - kx)$$

$$y = 2a \sin \omega t \cos kx$$

Clearly it is equation of standing wave for position of nodes $y=0$.

$$i. e., x = (2n + 1) \frac{\lambda}{4}$$

$$\Rightarrow \left(n + \frac{1}{2}\right) \lambda = 0, 1, 2, 3$$

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(b)

In case of interference of two waves resultant intensity

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

If ϕ varies randomly with time, so $(\cos \phi)_{av} = 0$

$$\Rightarrow I = I_1 + I_2$$

For n identical waves, $I = I_0 + I_0 + \dots = nI_0$

Here $I = 10I_0$

19

(a)

According to Doppler's effect, whenever there is a relative motion between a source of sound and listener, the apparent frequency of sound heard by the listener is different from the actual frequency of sound emitted by the source. Let S be source of sound and L the listener of sound. Let v be the actual frequency of sound emitted by the source and λ be the actual wavelength of the sound emitted.

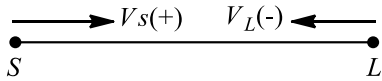
If v is velocity of sound in still air, then

$$\lambda = \frac{v}{V}$$

If velocity of listener is v_L and velocity of source is v_s , then apparent frequency of sound waves heard by the listener is

$$v' = \frac{v - v_L}{v - v_s} \times V$$

Here, both source and listener are approaching each other.



Then v_s is positive and v_L is negative.

$$\therefore v' = \frac{v - (-v_L)}{v - v_s} v = \left(\frac{v + v_L}{v - v_s} \right) v$$

i.e., $v' > v$

Also,

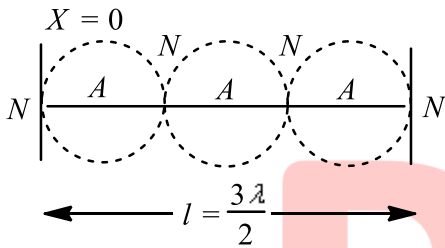
$$\lambda' < \lambda$$

So, listener listens more frequency and observes less wavelength.

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(c)

Third mode of vibration or second overtone has three loops.



It consist of 4 nodes and 3 antinodes.

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	A	A	B	C	B	D	D	B	B
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	B	B	D	A	A	A	B	A	C

PE