

DPP

DAILY PRACTICE PROBLEMS

CLASS : XITH
DATE :

Solutions

SUBJECT : PHYSICS
DPP NO. : 10

Topic :- WAVES

1 (c)

For an organ pipe open at one end,

$$\text{Frequency of 1st overtone } n_1 = \frac{3v}{4l_1}$$

For the organ pipe open at both ends,

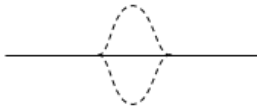
$$\text{Frequency of 3rd harmonic, } n_2 = \frac{3v}{2l_2}$$

As $n_1 = n_2$

$$\therefore \frac{3v}{4l_1} = \frac{3v}{2l_2} \text{ or } \frac{l_1}{l_2} = \frac{2}{4} = \frac{1}{2}$$

2 (c)

After two seconds each wave travel a distance of $2.5 \times 2 = 5 \text{ cm}$ *i. e.* the two pulses will meet in mutually opposite phase and hence the amplitude of resultant will be zero.



3 (b)

$$\frac{I_1}{I_2} = \frac{a_1^2}{a_2^2} \Rightarrow \frac{I_1}{I_2} = \frac{25}{100} = \frac{1}{4}$$

4 (a)

Frequency

$$v = \frac{1}{2l} \sqrt{\left(\frac{T}{m}\right)}$$

$$\therefore v + \frac{3}{2} = \frac{1}{2l} \sqrt{\left(\frac{101 T}{100 m}\right)}$$

$$= 1.005 \times \frac{1}{2l} \sqrt{\left(\frac{T}{m}\right)}$$

$$\Rightarrow v + 1.5 = 1.005v$$

$$\Rightarrow v = 300 \text{ Hz}$$

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(c)

$$\text{Reverberation time, } T = \frac{0.61V}{aS}$$

$$\Rightarrow \frac{T_1}{T_2} = \left(\frac{V_1}{V_2}\right) \left(\frac{S_2}{S_1}\right) = \left(\frac{V}{8V}\right) \left(\frac{4S}{S}\right) = \frac{1}{2}$$

$$\Rightarrow T_2 = 2T_1 = 2 \times 1 = 2 \text{ sec. } [\because T_1 = 1 \text{ sec}]$$

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(b)

$$\text{As } \frac{v}{4l_1} = \frac{3v}{2l_2}$$

$$\therefore \frac{l_1}{l_2} = \frac{2}{12} = \frac{1}{6}$$

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(d)

It is known that Doppler's effect depends on velocity not on distance. When the source is approaching the stationary observer, the apparent frequency heard by the observer is

$$n' = \frac{v \times n}{v - v_s} = \text{constant}$$

But $n' > n$.

When the source has crossed the observer, apparent frequency heard by the observer is

$$n'' = \frac{v \times n}{v + v_s} = \text{another constant}$$

But $n'' < n$. option (d) is correct.

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(b)

Sound heard directly

$$v_1 = v_o \left(\frac{v}{v - v_s}\right)$$

$$\therefore 970 = 1000 \left(\frac{330}{330 + v_s}\right)$$

$$\text{Or } v_s = 10.2 \text{ ms}^{-1}$$

The frequency of reflected sound is given by

$$v_2 = v_o \left(\frac{v}{v - v_s} \right) = 1000 \left(\frac{330}{330 - 10.2} \right)$$
$$= \frac{1000 \times 330}{319.8} \approx 1032 \text{ Hz}$$

9 **(c)**

A pulse of a wave train when travels along a stretched string and reaches the fixed end of the string, then it will be reflected back to the same medium and the reflected ray suffers a phase change of π with the incident wave but wave velocity after reflection does not change.

10 **(a)**

Given, $y(x,t) = 0.005 \cos(ax - \beta t)$

$$\frac{2\pi}{\lambda} = a \quad \text{and} \quad \frac{2\pi}{T} = \beta$$

So,

$$a = \frac{2\pi}{0.08} = 25\pi \quad \text{and} \quad \beta = \frac{2\pi}{2} = \pi$$

11 **(a)**

Length of air column in resonance is odd integer multiple of

$$\frac{\lambda}{4}$$

And prongs of tuning fork are kept in a vertical plane.

12 **(b)**

$$\text{As } p\sqrt{T} = \text{constant} \quad \therefore \frac{T_2}{T_1} = \frac{p_1^2}{p_2^2} = \frac{4^2}{6^2}$$

$$T_2 = \frac{16}{36} T_1 = \frac{16}{36} \times 65 = 29$$

$$\therefore \text{Weight to be removed} = 65 - 29 = 36 \text{ g}$$

13 **(c)**

The amplitude of a plane progressive wave = a , that of a cylindrical progressive wave is a/\sqrt{r} .

14 **(a)**

The average power per unit area that is incident perpendicular to the direction of propagation is called the intensity, i.e.,

$$I = \frac{P}{4\pi r^2}$$

Or

$$I \propto \frac{1}{r^2}$$

Or

$$\frac{I_2}{I_1} = \left(\frac{r_1}{r_2} \right)^2$$

Here, $r_1 = 2m, r_2 = 3m$

$$\therefore \frac{I_1}{I_2} = \left(\frac{3}{2}\right)^2 = \frac{9}{4}$$

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(a)

Wavelength of closed organ pipe is

$$\lambda = \frac{4L}{(2n-1)}$$

Putting $n=1,2,3,\dots$ we find that

$$\lambda_1 = 4L, \frac{4L}{3}, \frac{4L}{5}, \dots$$

So frequency of vibration corresponding to modes

$n=1,2,3,\dots$ is

$$v_1 = \frac{v}{\lambda_1} = \frac{v}{4L} = v_1$$

$$v_2 = \frac{v}{\lambda_2} = \frac{v}{4L/3} = \frac{3v}{4L} = 3v_1$$

$$v_3 = \frac{v}{\lambda_3} = \frac{v}{4L/5} = \frac{5v}{4L} = 5v_1$$

$$\therefore v_1 : v_2 : v_3 \dots = 1 : 3 : 5 : \dots$$

So, only odd harmonics are present.

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(c)

The standard equation of wave is

$$Y = a \sin(\omega t - kx)$$

Where a is amplitude, ω the angular velocity and x the displacement at instant t .

Given equation is

$$Y = 0.1 \sin(100\pi t - kx)$$

Comparing Eq. (i) with Eq. (ii), we get

$$\therefore \text{Wave number} = \frac{\omega}{v} = \frac{100\pi}{100} = \pi \text{ m}^{-1}$$

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(a)

The velocity of wave

$$v = \frac{\omega(\text{Co-efficient of } t)}{k(\text{Co-efficient of } x)} = \frac{10}{1} = 10 \text{ m/s}$$

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(a)

Speed of wave on a string

$$v = \sqrt{\frac{T}{m}}$$

Or

$$v \propto \sqrt{T}$$

Or

$$\frac{v_2}{v_1} = \sqrt{\frac{T_2}{T_1}}$$

Or

$$T - \frac{2}{T_1} = \frac{v_2^2}{v_1^2}$$

Or

$$\frac{T_2 - T_1}{T_1} = \frac{v_2^2 - v_1^2}{v_1^2}$$

Initially, $T_1 = 120 \text{ N}$,

$$v_1 = 150 \text{ ms}^{-1}$$

$$v_2 = v_1 + \frac{20}{100} v_1$$

$$= v_1 + \frac{v_1}{5} = \frac{6v_1}{5}$$

$$= \frac{6}{5} \times 150 = 180 \text{ ms}^{-1}$$

So, from eq. (i), we get

$$\frac{T_2 - T_1}{T_1} = \frac{(180)^2 - (150)^2}{(150)^2}$$

$$= \frac{30 \times 330}{150 \times 150} = 0.44$$

Hence, % increases in tension

$$= \left(\frac{T_2 - T_1}{T_1} \right) \times 100 = 0.44 \times 100 = 44\%$$

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(c)

$$n \propto \sqrt{T} \Rightarrow \frac{\Delta n}{n} = \frac{\Delta T}{2T}$$

If tension increases by 2%, then frequency must increase by 1%.

If initial frequency $n_1 = n$ then final frequency $n_2 - n_1 = 5$

$$\Rightarrow \frac{101}{100} n - n = 5 \Rightarrow n = 500 \text{ Hz}$$

Short trick : If you can remember then apply following formula to solve such type of problems.

Initial frequency of each wire (n)

$$= \frac{(\text{Number of beats heard per sec}) \times 200}{(\text{per centage change in tension of the wire})}$$

$$\text{Here } n = \frac{5 \times 200}{2} = 500 \text{ Hz}$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	C	C	B	A	C	B	D	B	C	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	B	C	A	A	C	A	A	C	C

PE