

Topic :- WAVE OPTICS

1 (d)

By using $f_p = \frac{r^2}{(2p-1)\lambda}$

For first HPZ $r = \sqrt{f_p \lambda} = \sqrt{0.6 \times 6000 \times 10^{-10}}$
 $= 6 \times 10^{-4} m$

2 (d)

For liquid A

$L_1 = 20 \text{ cm}, \theta_1 = 38^\circ, \text{concentration} = C_1$

Specific rotation $a_1 = \frac{\theta_1}{L_1 C_1} = \frac{38^\circ}{20 \times C_1}$

Similarly, for liquid B

$L_2 = 30 \text{ cm}, \theta_2 = -24^\circ, \text{concentration} = C_2$

Specific rotation $a_2 = \frac{\theta_2}{L_2 C_2} = \frac{-24^\circ}{30 \times C_2}$

The mixture has 1 part of liquid A and 2 parts of liquid B,

$\therefore C'_1 : C'_2 = 1 : 2$

$\theta = \{a_1 C'_1 + a_2 C'_2\} l$

$= \left\{ \frac{38^\circ}{20 \times C_1} \times \frac{C_1}{3} + \frac{(-24^\circ)}{30 \times C_2} \times \frac{2C_2}{3} \right\} \times 30$

$= 19^\circ - 16^\circ = 3^\circ$

Thus, the optical rotation of mixture is $+3^\circ$ in right had direction.

3 (b)

$c = \frac{E}{B} \Rightarrow B = \frac{E}{c} = \frac{18}{3 \times 10^8} = 6 \times 10^{-8} T$

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(a)

For an electromagnetic wave

$$\text{Velocity } c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = 3 \times 10^8 \text{ ms}^{-1}$$

Air acts almost as vacuum

$$\therefore a = 3 \text{ approximately}$$

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(c)

$$\text{Here, } \sin \theta = \frac{y}{D}$$

$$\text{So, } \Delta\theta = \frac{\Delta y}{D}$$

Angular fringe width $\theta_0 = \Delta\theta$ (width $\Delta y = \beta$)

$$\theta_0 = \frac{\beta}{D} = \frac{D\lambda}{d} \times \frac{1}{D} = \frac{\lambda}{d}$$

$$\theta_0 = 1^\circ = \pi/180 \text{ rad}$$

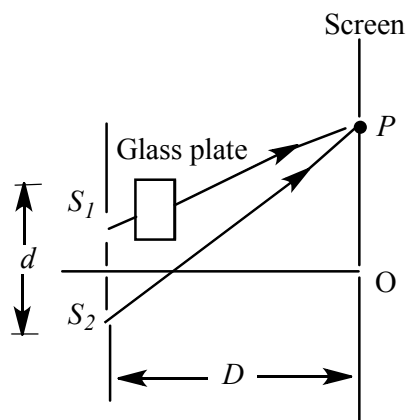
$$\text{And } \lambda = 6 \times 10^{-7} \text{ m}$$

$$d = \frac{\lambda}{\theta_0} = \frac{180}{\pi} \times 6 \times 10^{-7}$$

$$= 3.44 \times 10^{-5} \text{ m}$$

$$= 0.03 \text{ mm}$$

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(b)When a thin glass plate of thickness t is placed over one of the slits, then lateral displacement is given by

$$x = \frac{(\mu - 1)tD}{d}$$

Given, $\mu = 1.5$, $t = 0.06 \text{ mm} = 6 \times 10^{-5} \text{ m}$

$D = 2 \text{ m}$, $d = 1 \text{ mm} = 1 \times 10^{-3} \text{ m}$

Putting the values in the above relation, we get

$$x = \frac{(1.5 - 1) \times 6 \times 10^{-5} \times 2}{1 \times 10^{-3}}$$
$$= 0.5 \times 12 \times 10^{-2} = 0.06 \text{ m} = 6 \text{ cm}$$

7 **(d)**

To see interference, we need two sources with the same frequency and with a constant phase difference. In the given waves,

$$X_1 = a_1 \sin \omega t$$

And $X_4 = a_1 \sin(\omega t + \delta)$

Have a constant phase difference δ , so interference is possible between them.

For $X_1 = a_1 \sin \omega t$

And $X_2 = a_2 \sin 2\omega t$

Frequency is not equal and there is no constant phase difference.

For $X_1 = a_1 \sin \omega t$

And $X_3 = a_1 \sin \omega_1 t$,

Frequency is different and there is no constant phase difference.

8 **(a)**

Intensity, $I_0 = I_1 + I_2 + 2\sqrt{I_1 I_2}$

If $I_1 = I_2 = I$ (Let)

Then $I_0 = 4I$

When one slit is covered then $I_2 = 0$

$$\therefore I_0 = I = \frac{I_0}{4}$$

10 **(a)**

For interference phase difference must be constant

11 **(d)**

$$\beta = \frac{\lambda D}{d} = \frac{600 \times 10^{-9} \times 2}{1 \times 10^{-3}} = 12 \times 10^{-4} \text{ m}$$

So, distance between the first dark fringes on either side of the central bright fringe

$$= 2\beta$$

$$= 2 \times 12 \times 10^{-4} \text{ m}$$

$$= 24 \times 10^{-4} \text{ m}$$

$$= 2.4 \text{ mm}$$

12 **(a)**

$$\omega = 6 \times 10^8$$

$$k = \frac{\omega}{v} = \frac{6 \times 10^8}{3 \times 10^8} = 2 \text{ m}^{-1}$$

13 **(d)**

If shift is equivalent to n fringes then

$$n = \frac{(\mu - 1)t}{\lambda} \Rightarrow n \propto t \Rightarrow \frac{t_2}{t_1} = \frac{n_2}{n_1} \Rightarrow t_2 = \frac{n_2}{n_1} \times t$$

$$t_2 = \frac{20}{30} \times 4.8 = 3.2 \text{ mm}$$

14 **(c)**

Doppler shift (Source moving towards observer)

$$\lambda' = \lambda \left(1 - \frac{V}{C}\right)$$

$$5400 \text{ \AA} = 6200 \text{ \AA} \left(1 - \frac{V}{C}\right)$$

$$V = \left[1 - \frac{54}{62}\right]C = 3.9 \times 10^7 \text{ approx}$$

15 **(b)**

The optical path between any two points is proportional to the time of travel.

The distance traversed by light in a medium of refractive index μ in time t is given by

$$d = vt \quad \dots\dots\dots(i)$$

Where v is velocity of light in the medium. The distance traversed by light in a vacuum in this time.

$$\Delta = ct$$

$$= c \cdot \frac{d}{v} \quad [From Eq.(i)]$$

$$= d \frac{c}{v} = \mu d \quad (ii)$$

$$\text{(Since, } \mu = \frac{c}{v} \text{)}$$

This distance is the equivalent distance in vacuum and is called optical path.

Here, optical path for first ray = $n_1 L_1$

Optical path for second ray = $n_2 L_2$

Path difference = $n_1 L_1 - n_2 L_2$

Now, phase difference

$$= \frac{2\pi}{\lambda} \times \text{path difference}$$

$$= \frac{2\pi}{\lambda} \times (n_1 L_1 - n_2 L_2)$$

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(c)

$$\beta = \frac{\beta}{\lambda} (\mu - 1)t$$

$$\Rightarrow t = \frac{\lambda}{(\mu - 1)} = \frac{\lambda}{(1.5 - 1)} = 2\lambda$$

17

(c)

The number of fringes on either side of centre C of screen is

$$n_1 = \left[\frac{AC}{\beta} \right] = \left[\frac{0.5}{0.021} \right] = [23.8] = 23$$

\therefore Total number of fringes

$$= 2n_1 + \text{fringe at centre}$$

$$= 2n_1 + 1 = 2 \times 23 + 1$$

$$= 46 + 1 = 47$$

In Young's experiment, the number of fringes should be odd.

18

(a)

When unpolarised light is made incident at polarizing angle, the reflected light is plane polarized in a direction perpendicular to the plane of incidence.

Therefore \vec{E} in reflected light will vibrate in vertical plane with respect to plane of incidence

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	D	D	B	A	C	B	D	A	A	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	D	A	D	C	B	C	C	A	B	B

P E