

Topic :- WAVE OPTICS

1 (b)

Fringe shift is given by $x = \frac{(\mu - 1)t\beta}{\lambda}$

For first plate, $x = \frac{(\mu_1 - 1)t\beta}{\lambda}$

For second plate $\frac{3}{2}x = \frac{(\mu_2 - 1)t\beta}{\lambda}$

$$\Rightarrow \left(\frac{\mu_2 - 1}{\mu_1 - 1}\right) = \frac{3}{2} \Rightarrow \left(\frac{\mu_2 - 1}{1.5 - 1}\right) = \frac{3}{2}$$

$$\Rightarrow \mu_2 = 1.75$$

2 (d)

$$y_1 = a \sin \omega t, y_2 = a \cos \omega t = a \sin \left(\omega t + \frac{\pi}{2}\right)$$

3 (d)

$$\phi = \frac{\lambda}{6} = \frac{360^\circ}{6} = 60^\circ$$

$$\begin{aligned} I &= I_0 \cos^2 \theta \\ &= I_0 \cos^2 60^\circ \\ &= \frac{3}{4} \times I_0 \\ \frac{I}{I_0} &= \frac{3}{4} \end{aligned}$$

5 (d)

Let n th minima of 400 nm coincides with m th minima of 560 nm, then

$$(2n - 1)\left(\frac{400}{2}\right) = (2m - 1)\left(\frac{560}{2}\right)$$

$$\text{Or } \frac{2n - 1}{2m - 1} = \frac{7}{2} = \frac{14}{10} = \dots$$

ie. 4th minima of 400 nm coincides with 3rd minima of 560 nm.

Location of this minima is,

$$Y_1 = \frac{(2 \times 4 - 1)(1000)(400 \times 10^{-6})}{2 \times 0.4} = 14 \text{ mm}$$

Next 11th minima of 400 nm will coincide with 8th minima of 560 nm. Location of this minima is ,

$$Y_2 = \frac{(2 \times 11 - 1) (1000) (400 \times 10^{-6})}{2 \times 0.1} = 42 \text{ mm}$$

$$\therefore \text{Required distance} = Y_2 - Y_1 = 28 \text{ mm}$$

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(a)

Amplitude A_1 and A_2 are added as vector. Angle between these vectors is the phase difference $(\beta_1 - \beta_2)$ between them

$$\therefore R = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos(\beta_1 - \beta_2)}$$

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(c)

The interference fringes for two slits are hyperbolic

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(d)

Momentum transferred in one second

$$p = \frac{2U}{c} = \frac{2S_{av}A}{c} = \frac{2 \times 6 \times 40 \times 10^{-4}}{3 \times 10^8} \\ = 1.6 \times 10^{-10} \text{ kg} - \text{m/s}^2$$

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(d)

Diffraction shows the wave nature of light and photoelectric effect shows particle nature of light

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(d)

Phase difference, $\phi = \frac{2\pi}{\lambda} \times \text{path difference}$

$$\phi = \frac{2\pi}{\lambda} \times \frac{\lambda}{6} = \frac{\pi}{3} = 60^\circ$$

Intensity, $I = I_0 \cos^2\left(\frac{\phi}{2}\right)$

$$\frac{I}{I_0} = \cos^2(30^\circ) = \left(\frac{\sqrt{3}}{2}\right)^2 = 0.75$$

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(a)

At any point along the path 1, path difference between the waves is 0

Hence maxima is obtained all along the path 1

At any point along the path 2, path difference is 1.5λ which is odd multiple of $\frac{\lambda}{2}$, so minima is obtained all along the path 2

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(c)

Let a_1 and a_2 be amplitudes of the two waves.

For maximum intensity

$$I_{\max} = (a_1 + a_2)^2$$

For minimum intensity

$$I_{\min} = (a_1 - a_2)^2$$

$$\text{Given, } \frac{I_{\max}}{I_{\min}} = \frac{25}{1} = \frac{(a_1 + a_2)^2}{(a_1 - a_2)^2}$$

$$\Rightarrow \frac{a_1 + a_2}{a_1 - a_2} = \frac{5}{1}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{3}{2}$$

(law of componendo and dividendo)

Also, Intensity \propto (amplitude)²

$$\therefore \frac{I_1}{I_2} = \left(\frac{a_1}{a_2}\right)^2 = \frac{9}{4}$$

15 **(a)**

Total phase difference

= Initial phase difference + Phase difference due to path

$$= 66^\circ + \frac{360^\circ}{\lambda} \times \Delta x = 66^\circ + \frac{360^\circ}{\lambda} \times \frac{\lambda}{4} = 66^\circ + 90 = 156^\circ$$

16 **(a)**

Photoelectric effect verifies particle nature of light. Reflection and refraction verify both particle nature and wave nature of light

18 **(a)**

$$\text{The speed of light } C = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = \frac{1}{\sqrt{2 \times 8}} = \frac{1}{4} = 0.25$$

19 **(c)**

$$\text{Path difference, } x = (SS_1 + S_1O) - (SS_2 + S_2O)$$

If $x = n\lambda$, the central fringe at O will be bright. If $x = (2n - 1)\lambda/2$, the central fringe at O will be dark.

20 **(c)**

$$\text{Critical angle, } C = \sin^{-1}(0.6)$$

$$\sin(C) = 0.6$$

$$\mu = \frac{1}{\sin C} = \frac{1}{0.6}$$

$$\text{Polarizing angle } i_p = \tan^{-1}(\mu) = \tan^{-1}\left(\frac{1}{0.6}\right)$$

$$= \tan^{-1}(1.6667)$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	B	D	D	D	D	A	C	D	D	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	B	C	C	A	A	C	A	C	C

PE