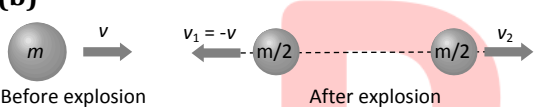


Topic :- WORK ENERGY AND POWER

- 1 (a)
Spring constant $k = \frac{F}{x} = \text{Slope of curve}$
 $\therefore k = \frac{4 - 1}{30} = \frac{3}{30} = 0.1 \text{ kg/cm}$

- 2 (b)
- 
- Before explosion: A mass m moves with velocity v to the right.
- After explosion: Two fragments of mass $m/2$ are shown. The left fragment moves with velocity $v_1 = -v$ to the left. The right fragment moves with velocity v_2 to the right.
- Let the initial mass of body = m
Initial linear momentum = mv ... (i)
When it breaks into equal masses then one of the fragment retrace back with same velocity
 \therefore Final linear momentum = $\frac{m}{2}(-v) + \frac{m}{2}(v_2)$... (ii)
By the conservation of linear momentum
 $\Rightarrow mv = \frac{-mv}{2} + \frac{mv_2}{2}$
 $\Rightarrow v_2 = 3v$
i.e., other fragment moves with velocity $3v$ in forward direction

- 3 (a)
Effective height through which man moves up
 $= 1 - h$

- 4 (d)
Work done (W) = Area under curve of $F-x$ graph
 $= \text{Area of triangle } OAB = \frac{1}{2} \times 5 \times 1 = 2.5 \text{ J}$

- 5 (c)
According to work-energy theorem,
 $W = \Delta K = 0$
(\because Initial and final speeds are zero)
 \therefore work done by friction + work done by gravity = 0
 $-(\mu mg \cos \phi) \frac{l}{2} + mgl \sin \phi = 0$

$$\text{or } \frac{\mu}{2} \cos \phi = \sin \phi$$

$$\therefore \mu = 2 \tan \phi$$

6

(c)

$$\text{Force produced by the engine } F = \frac{P}{v} = \frac{30 \times 10^3}{30} = 10^3 N$$

$$\begin{aligned} \text{Acceleration} &= \frac{\text{Forward force by engine} - \text{resistive force}}{\text{mas of car}} \\ &= \frac{1000 - 750}{1250} = \frac{250}{1250} = \frac{1}{5} \text{ m/s}^2 \end{aligned}$$

9

(c)

The work done in stretching a sprig by a length x ,

$$W_1 = \frac{1}{2} kx^2 \quad \dots(i)$$

The work done in stretching the spring by a further length x .

$$W_2 = \frac{1}{2} k(2x)^2 - \frac{1}{2} kx^2$$

$$\text{Or } W_2 = \frac{1}{2} k \times 4x^2 - \frac{1}{2} kx^2$$

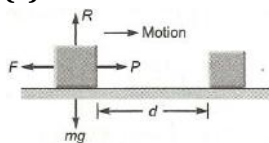
$$\text{Or } W_2 = 3 \times \frac{1}{2} kx^2 \quad \dots(ii)$$

From Esq. (i) and (ii) we have

$$W_2 = 3W_1$$

10

(c)



As shown a block of mass M is lying over rough horizontal surface. Let μ be the coefficient of kinetic friction between the two surfaces in contact. The force of friction between the block and horizontal surface is given by

$$F = \mu R = \mu M g \quad (\because R = M g)$$

To move the block without acceleration, the force (P) required will be just equal to the force of friction, ie,

$$P = F = \mu R$$

If d is the distance moved, then work done is given by

$$W = P \times d = \mu R d$$

11

(a)

Kinetic energy of the block is

$$K = \frac{1}{2} m v^2$$

This kinetic energy is equal to the work done by the block before coming to rest. The work done in compressing the spring through a distance x from its normal length is

$$W = \frac{1}{2} k x^2$$

$$\therefore \frac{1}{2} m v^2 = \frac{1}{2} k x^2$$

$$\Rightarrow x = v \sqrt{\frac{m}{k}}$$

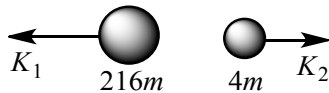
Given, $v = 4 \text{ m/s}, m = 16 \text{ kg}, k = 100 \text{ N/m}$

$$\therefore x = 4 \times \sqrt{\frac{16}{100}} = 1.6 \text{ m}$$

12 (b)

Given that,

$$K_1 + K_2 = 5.5 \text{ MeV} \dots(i)$$



From conservation of linear Momentum

$$\text{Or } \sqrt{2K_1(216m)} = \sqrt{2k_2(4m)}$$

$$\text{Or } k_2 = 54 K_1 \dots(ii)$$

Solving Eq.(i) & (ii), we get

$$k_2 = KE \text{ of } \alpha \text{-particle} = 5.4 \text{ MeV.}$$

13 (d)

Work done in raising water = mgh

$$\therefore W = (\text{volume} \times \text{density}) gh = (9 \times 1000) \times 10 \times 10$$

$$\Rightarrow W = 9 \times 10^5 \text{ J}$$

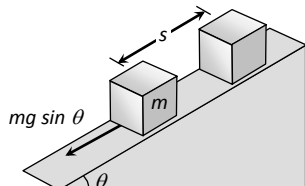
$$\therefore \text{Useful power} = \frac{\text{work}}{\text{time}} = \frac{9 \times 10^5}{5 \times 60} = 3 \text{ kW}$$

$$\therefore \text{Efficiency} = \frac{3}{10} = 30\%$$

14 (d)

As the body moves in the direction of force therefore work done by gravitational force will be positive

$$W = Fs = mgh = 10 \times 9.8 \times 10 = 980 \text{ J}$$



15 (a)

$$\text{Given that, } S = \frac{1}{3}t^2$$

$$v = \frac{dS}{dt} = \frac{2}{3}t; a = \frac{d^2S}{dt^2} = \frac{2}{3}$$

$$F = ma = 3 \times \frac{2}{3} = 2 \text{ N}; \text{ Work} = 2 \times \frac{1}{3}t^2$$

At $t=2$

$$\text{Work} = 2 \times \frac{1}{3} \times 2 \times 2 = \frac{8}{3} \text{ J}$$

16 (b)

In elastic collision

$$v_1 = \left(\frac{m_1 - m_2}{m_1 + m_2} \right) u_1 + \left(\frac{2m_2}{m_1 + m_2} \right) u_2$$

If the second ball is at rest, ie $u_2 = 0$, then

$$v_1 = \left(\frac{m_1 - m_2}{m_1 + m_2} \right) u_1$$

$$\frac{2}{3}u_1 = \left(\frac{m_1 - m_2}{m_1 + m_2} \right) u_1 \quad [\because v_1 = \frac{2}{3}u_1]$$

$$\text{Or } 2m_1 + 2m_2 = 3m_1 - 3m_2$$

$$\text{Or } m_1 = 5m_2$$

$$\text{Or } \frac{m_1}{m_2} = \frac{5}{1}$$

17

(a)

From Newton's second law,

$$F = \frac{dp}{dt}$$

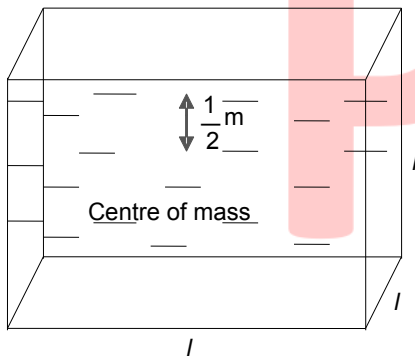
$$\text{If } F=0, \text{ then } \frac{dp}{dt} = 0$$

$$\Rightarrow p = \text{constant}$$

Thus, if total external force acting on the system is zero, then linear momentum of the system remains conserved.

18

(b)



$$V = l^3 = 1m^3$$

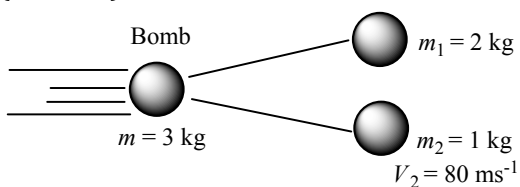
$$m = 1 \times 1000 = 1000\text{kg}$$

$$W = mgh = 1000 \times 10 \times \frac{1}{2} = 5000 \text{ J}$$

19

(d)

From law of conservation of momentum, when no external force acts upon a system of two (or more) bodies, then the total momentum of the system remains constant.



Momentum before explosion = momentum after explosion.

since bomb is at rest, its velocity is zero, hence,

$$mv = m_1v_1 + m_2v_2$$

$$3 \times 0 = 2v_1 + 1 \times 80$$

$$\text{or } v_1 = -\frac{80}{2} = -40\text{ms}^{-1}$$

Total energy imparted is

$$\text{KE} = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2$$

$$= \frac{1}{2} \times 2 \times (-40)^2 + \frac{1}{2} \times 1 \times (80)^2$$

$$= 1600 + 3200 = 4800\text{J}$$

$$= 4.8\text{kJ}$$

20

(a)

Let d_s be the distance travelled by the vehicle before it stops

Here, final velocity $v = 0$, initial velocity $= u$

Using equation of motion $v^2 = u^2 + 2aS$

$$\therefore 0^2 = u^2 + 2ad_s$$

$$\text{Or Stopping distance, } d_s = -\frac{u^2}{2a}$$

PE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	B	A	D	C	C	C	D	C	C
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	B	D	D	A	B	A	B	D	A

PE