

DPP

DAILY PRACTICE PROBLEMS

CLASS : XITH
DATE :

Solutions

SUBJECT : PHYSICS
DPP NO. : 6

Topic :- WORK ENERGY AND POWER

1 (b)

$$\text{Kinetic energy, } K = \frac{P^2}{2m}$$

Where P is the momentum and m is the mass. When momentum is increased by 20%, then

$$P' = P + \frac{20}{100}P = 1.2P$$

$$\therefore K' = \frac{(1.2P)^2}{2m} = \frac{1.44P^2}{2m} = 1.44K$$

$$K' = K + 0.44K \Rightarrow \frac{K' - K}{K} = 0.44$$

Percentage increase in kinetic energy is

$$\frac{K' - K}{K} \times 100 = 0.44 \times 100 = 44\%$$

2 (c)

$$\text{Loss of kinetic energy} = \frac{1}{2} \frac{m_1 m_2}{m_1 + m_2} (v_1 - v_2)^2$$

$$= \frac{1}{2} \times \frac{M \times M}{M + M} (V_1 - V_2)^2$$

$$= \frac{M \cdot M}{2(2M)} (V_1 - V_2)^2$$

$$= \frac{M}{4} (V_1 - V_2)^2$$

3 (a)

No work is done while covering the horizontal distance because $\vec{F} \cdot \vec{s} = 0$ ($\therefore \theta = 90^\circ$)

But work is done during vertical displacement which is given by

$$F_h = 60 \times 5 = 300 \text{ J}$$

4 (c)

$$P = \frac{mgh}{t} = \frac{80 \times 10 \times 1.5}{2}$$

$$= 600 \text{ W} = 0.6 \text{ kW}$$

5 (c)

The displacement of body is

$$\begin{aligned}\vec{AB} &= \vec{r}_B - \vec{r}_A \\ &= (3\hat{i} + 2\hat{j} + 5\hat{k}) - (2\hat{i} + 3\hat{j} + 4\hat{k}) \\ &= \hat{i} + \hat{j} + \hat{k} \\ \therefore W &= \vec{F} \cdot \vec{AB} = (2\hat{i} - 4\hat{j}) \cdot (\hat{i} + \hat{j} + \hat{k}) \\ &= 2 - 4 = -2 \text{ J}\end{aligned}$$

6

(b)

Let the constant acceleration of body of mass m is a ,

From equation of motion

$$v_1 = 0 + at_1$$

$$\text{Or } a = \frac{v_1}{t_1} \quad \dots(\text{i})$$

At an instant t , the velocity v of the body

$$v = 0 + at$$

$$v = \frac{v_1}{t_1}t \quad \dots(\text{ii})$$

Therefore, instantaneous power

$$\begin{aligned}p &= Fv = mav \\ &= m\left(\frac{v_1}{t_1}\right) \times \left(\frac{v_1}{t_1} \cdot t\right) \quad [\text{From Eqs.(i) and (ii)}]\end{aligned}$$

$$= \frac{mv_1^2 t}{t_1^2}$$

7

(d)

Due to the same mass of A and B as well as due to elastic collision velocities of spheres get interchanged after the collision

8

(a)

$$\begin{aligned}\text{Power} &= Fv = v\left(\frac{m}{t}\right)v = v^2(\rho Av) \\ &= \rho Av^3 = (100)(2)^3 = 800 \text{ W}\end{aligned}$$

9

(b)

Impulse = change in momentum

$$mv_2 - mv_1 = 0.1 \times 40 - 0.1 \times (-30)$$

10

(d)

$$\text{Kinetic energy of particle } k = \frac{p_1^2}{2m}$$

$$p_1^2 = 2mk'$$

When kinetic energy = $2k$

$$p_2^2 = 2m \times 2k, p_2^2 = 2p_1^2, p_2 = \sqrt{2}p_1$$

11

(b)

Gravitational potential energy of ball gets converted into elastic potential energy of the

$$\text{spring } mg(h + d) = \frac{1}{2}Kd^2$$

$$\text{Net work done} = mg(h + d) - \frac{1}{2}Kd^2 = 0$$

12

(a)

$$dW = Fdl$$

$$W = \int_0^l F dl \quad Y = \frac{FL}{dl}$$

$$\text{or } W = \int_0^l \frac{Yal}{L} dl \quad \text{or } F = \frac{Yal}{L}$$

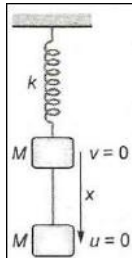
$$\text{or } W = \frac{Ya}{L} \int_0^l dl \quad \text{or } W = \frac{Ya}{L} \left(\frac{l^2}{2} \right)$$

$$\text{or } W = \frac{1Yal}{2L} l = \frac{1}{2} Fl$$

13

(b)

Let x be the maximum extension of the spring, figure. From conservation of mechanical energy; decreases in gravitational potential energy = increase in elastic potential energy



$$Mgx = \frac{1}{2} k x^2$$

$$x = \frac{2Mg}{k}$$

14

(b)

$$a = \frac{10 - 0}{5} \text{ ms}^{-2} = 2 \text{ ms}^{-2};$$

$$F = ma \text{ or } F = 1000 \times 2 \text{ N} = 2000 \text{ N}$$

$$\text{Average velocity} = \frac{0 + 10}{2} \text{ ms}^{-1} = 5 \text{ ms}^{-1}$$

$$\text{Average power} = 2000 \times 5 \text{ W} = 10^4 \text{ W}$$

$$\text{Required horse power is } \frac{10^4}{746}$$

15

(a)

Work done = area between the graph force displacement curve and displacement

$$W = \frac{1}{2} \times 6 \times 10 - 5 \times 4 + 5 \times 4 - 5 \times 2$$

$$W = 20 \text{ J}$$

According to work energy theorem

$$\Delta = K_E = W$$

$$K_{Ef} = W + \Delta K$$

$$= 20 + 25$$

$$= 45 \text{ J}$$

16

(b)



Initial condition

Final condition

By conservation of linear momentum

$$2m = mv_1 + 2mv_2 \Rightarrow v_1 + 2v_2 = 2$$

By definition of $e, e = \frac{1}{2} = \frac{v_2 - v_1}{2 - 0}$

$$\Rightarrow v_2 - v_1 = 1 \Rightarrow v_1 = 0 \text{ and } v_2 = 1 \text{ ms}^{-1}$$

17

(b)

Potential energy of water = kinetic energy at turbine

$$mgh = \frac{1}{2}mv^2 \Rightarrow v = \sqrt{2gh} = \sqrt{2 \times 9.8 \times 19.6} = 19.6 \text{ m/s}$$

18

(c)

$$U(x) = \frac{a}{x^{12}} - \frac{b}{x^6}$$

$$U(x = \infty) = 0$$

$$\text{As } F = -\frac{dU}{dx} = -\left[\frac{12a}{x^{13}} + \frac{6b}{x^7}\right]$$

At equilibrium, $F = 0$

$$X^6 = \frac{2a}{b}$$

$$\therefore U_{\text{at equilibrium}} = \frac{a}{\left(\frac{2a}{b}\right)^2} - \frac{b}{\left(\frac{2a}{b}\right)} = -\frac{b^2}{4a}$$

$$\therefore D = [U(x = \infty) - U_{\text{at equilibrium}}] = \frac{b^2}{4a}$$

20

(c)

$$m_1v_1 - m_2v_2 = (m_1 + m_2)v$$

$$\therefore 2 \times 3 - 1 \times 4 = (2 + 1)v$$

$$\text{Or } v = \frac{2}{3} \text{ ms}^{-1}$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	B	C	A	C	C	B	D	A	B	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	A	B	B	A	B	B	C	B	C

PE