

## Topic :- UNITS AND MEASUREMENTS

1 (b)

$$\text{Bulk modulus } K = \frac{\text{normal stress}}{\text{volumetric strain}}$$
$$= \frac{F/A}{-\Delta V/V}$$

$$= -\frac{FV}{A \Delta V}$$

Now,  $\frac{F}{A} = p$

$$\therefore K = \frac{pV}{\Delta V}$$

As volumetric strain is dimensionless.

$\therefore$  Dimensions of  $K$  = dimensions of normal stress

$$\Rightarrow [K] = [ML^{-1}T^{-2}]$$

2 (a)

$$R = \frac{V}{I} \Rightarrow \pm \frac{\Delta R}{R} = \pm \frac{\Delta V}{V} \pm \frac{\Delta I}{I}$$
$$= 3 + 3 = 6\%$$

4 (d)

$$n(xm)^2 = 1m^2 \text{ or } n = \frac{1}{x^2}$$

5 (d)

Given,  $v = at + bt^2$

Applying the law of homogeneity  $[v] = [bt^2]$

Or  $[LT^{-1}] = [bT^2]$

Or  $[b] = [LT^{-3}]$

6

**(a)**

$$V = \frac{W}{Q} = [ML^2T^{-2}Q^{-1}]$$

7

**(c)**

$$\text{Volume of sphere } (V) = \frac{4}{3}\pi r^3$$

$$\% \text{ error in volume} = 3 \times \frac{\Delta r}{r} \times 100 = \left(3 \times \frac{0.1}{5.3}\right) \times 100$$

8

**(d)**

$$\text{Given, } v = at + \frac{b}{t+c}$$

Since, LHS is equal to velocity, so  $at$  and  $\frac{b}{t+c}$  must have the dimensions of velocity.

$$\therefore at = v$$

$$\text{Or } a = \frac{v}{t} = \frac{[LT^{-1}]}{[T]} = [LT^{-2}]$$

Now,  $c = \text{time}$  ( $\because$  like quantities are added)

$$\therefore c = t = [T]$$

Now,

$$\frac{b}{t+c} = v$$

$$\therefore b = v \times \text{time} = [LT^{-1}][T] = [L]$$

10

**(a)**

$$\text{Dimensions of } E = [ML^2T^{-2}]$$

$$\text{Dimensions of } G = [M^{-1}L^3T^{-2}]$$

$$\text{Dimensions of } I = [MLT^{-1}]$$

$$\text{And dimension of } M = [M]$$

$$\therefore \text{Dimensions of } \frac{GIM^2}{E^2} = \frac{[M^{-1}L^3T^{-2}][MLT^{-1}][M^2]}{[ML^2T^{-2}]^2}$$

$$= [T]$$

= Dimensions of time

11

**(a)**

$$\text{Percentage error inside} = \frac{1}{2} \left[ \frac{0.2}{100} \times 100 \right] = 0.1$$

$$\text{Absolute error inside} = \frac{0.1}{100} \times 10 = 0.01$$

12 **(d)**

The second is the duration of 9192631770 period of the radiation corresponding to the transition between the two hyperfine levels of the ground state of cesium-133 atom. Therefore, 1 ns is  $10^{-9}$  s of Cs-clock of 9192631770 oscillations.

14 **(a)**

$$\text{Weight in air} = (5.00 \pm 0.05)N$$

$$\text{Weight in water} = (4.00 \pm 0.05)N$$

$$\text{Loss of weight in water} = (1.00 \pm 0.1)N$$

$$\text{Now relative density} = \frac{\text{weight in air}}{\text{weight loss in water}}$$

$$\text{i.e. } R.D = \frac{5.00 \pm 0.05}{1.00 \pm 0.1}$$

Now relative density with max permissible error

$$= \frac{5.00}{1.00} \pm \left( \frac{0.05}{5.00} + \frac{0.1}{1.00} \right) \times 100 = 5.0 \pm (1 + 10)\%$$

$$= 5.0 \pm 11\%$$

15 **(c)**

$$\text{Angular momentum} = [ML^2T^{-1}], \text{ Frequency} = [T^{-1}]$$

17 **(a)**

By the principle of dimensional homogeneity

$$[P] = \left[ \frac{a}{V^2} \right] \Rightarrow [a] = [P] \times [V^2] = [ML^{-1}T^{-2}][L^6]$$

$$= [ML^5T^{-2}]$$

18 **(a)**

$$[E] = [ML^2T^{-2}]$$

$$[M] = [M]$$

$$[L] = [ML^2T^{-1}]$$

$$[G] = [M^{-1}L^3T^{-2}]$$

$$\left[ \frac{EL^2}{M^5G^2} \right] = \frac{[ML^2T^{-2}][ML^2T^{-1}]^2}{[M]^5[M^{-1}L^3T^{-2}]^2}$$

$$= \frac{[ML^2T^{-2}][M^2L^4T^{-2}]}{[M^5][M^{-2}L^6T^{-4}]} = \frac{[M^3L^6T^{-4}]}{[M^3L^6T^{-4}]}$$

$$= [m^0L^0T^0] = \text{Angle}$$

19 **(c)**

$$[MT^{-3}] = \frac{[ML^2T^{-2}]}{[L^2][T]} = \text{energy / area} \times \text{time} = \text{dimensions of solar constant.}$$

20 **(b)**

We know that kinetic energy =  $\frac{1}{2}mv^2$

Required percentage error is  $2\% + 2 \times 3\%$  ie, 8%

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	B	A	A	D	D	A	C	D	D	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	D	A	A	C	C	A	A	C	B

PE