

CLASS: XITH DATE:

Solutions

SUBJECT : PHYSICS

DPP NO.: 2

Topic:-.UNITS AND MEASUREMENTS

1 **(d)**

Given equation, $y = a\sin(bt \cdot cx)$

Comparing the given equation with general wave equation

$$y = a \sin\left(\frac{2\pi t}{T} - \frac{2\pi x}{\lambda}\right),\,$$

We get
$$b = \frac{2\pi}{T}$$
, $c = \frac{2\pi}{\lambda}$

Dimension of $\frac{b}{c}$

$$=\frac{2\pi/T}{2\pi/\lambda}=[LT^{-1}]$$
, and other three quantity is dimensionless

3 **(b**)

Units of a and PV^2 are same and equal to $dyne \times cm^4$

4 **(d**)

$$f = \frac{1}{2\pi\sqrt{LC}}$$

 $\therefore \left(\frac{C}{L}\right)$ does not represent the dimensions of frequency

5 **(c)**

$$P_1 = [ML^2T^{-1}]$$

$$D_2 = [(2M)(2L)^2(2T)^{-1}]$$

$$P_2 = 4[ML^2T^{-1}] = 4P_1$$

6 **(a**)

Time period of a simple pendulum

$$T = 2\pi \sqrt{\frac{L}{8}}$$

$$Or \ g = \frac{4\pi^2 L}{T^2} \qquad \dots (i)$$

Differentiating Eq. (i), we have

$$\frac{\Delta g}{g} = \frac{\Delta L}{L} + \frac{2\Delta T}{T} \qquad(ii)$$

Given, L=100 cm, T=2s,

$$\Delta T = \frac{0.1}{100} = 0.001s,$$

$$\Delta L = 1mm = 0.1 cm$$

Substituting the in Eq. (ii), we have

$$\therefore \left| \frac{\Delta g}{g} \right|_{\text{max}} = \frac{\Delta^L}{L} + \frac{2\Delta T}{T}$$

$$= \frac{0.1}{100} + 2 \times \frac{0.001}{2}$$

Thus, maximum percentage eror

$$\left| \frac{\Delta g}{g} \right|_{\text{max}} \times 100 = \left(\frac{0.1}{100} \times 100 \right) + \left(\frac{2 \times 0.001}{2} \times 100 \right)$$

$$= 0.1\% + 0.1\% = 0.2\%$$

7 **(d)**

Because temperature is a fundamental quantity

8 (a)

By submitting dimension of each quantity in R.H.S. of option (a) we get

$$\begin{bmatrix} \frac{mg}{\eta r} \end{bmatrix} = \begin{bmatrix} \frac{M \times LT^{-2}}{ML^{-1}T^{-1} \times L} \end{bmatrix} = [LT^{-1}]$$

This option gives the dimension of velocity

9 **(b)**

Percentage error in mass $=\frac{0.01}{23.42}\times 100 = 0.04$

Percentage error in volume $=\frac{0.1}{4.9} \times 100 = 2.04$

Adding up the percentage errors, we get nearly 2%.

10 **(d)**

Percentage error in A

$$= \left(2 \times 1 + 3 \times 3 + 1 \times 2 + \frac{1}{2} \times 2\right)\% = 14\%$$

11 **(d)**

According to Wien's law the product of wavelength corresponding to maximum intensity of radiation and temperature of body (in Kelvin) is constant ie, $\lambda_m T = b = \text{constant}$, where b is Wien's constant and has value 2.89×10^{-3} m - K.

$$Y = \frac{\text{Stress}}{\text{Strain}} = \frac{\text{Force/Area}}{\text{Dimensionless}} \Rightarrow Y \equiv \text{Pressure}$$

 $Coefficient\ o\ friction = \frac{Applied\ force}{Normal\ reactiom}$

$$=\frac{[MLT^{-2}]}{[MLT^{-2}]}$$
 = no dimensions

Unit =
$$\frac{N}{N}$$
 = no unit

$$[kx]$$
 = Dimension of ωt = (dimensionless)

Hence
$$K = \frac{1}{X} = \frac{1}{L} = [L^{-1}] : [K] = [L^{-1}]$$

Magnetic field =
$$\frac{Force}{Charge \times velocity}$$

$$= \frac{[MLT^{-2}]}{[AT][LT^{-1}]} = [MA^{-1}T^{-2}]$$

17 **(c**

Percentage error in measurement of a side

$$=\frac{0.01}{1.23}\times100$$

Percentage error in measurement of area

$$=2 \times \frac{0.01}{1.23} \times 100$$

18 **(a**)

Charge = current \times time

19 (c)

From the principle of dimensional homogenity $[v] = [at] \Rightarrow [a] = [LT^{-2}]$. Similarly [b] = [L] and [c] = [T]

20 **(d)**

$$U = \frac{A\sqrt{x}}{x+B}$$

Dimensions of U = dimensions of potential energy

$$= \left[ML^2T^{-2} \right]$$

From Eq. (i),

Dimensions of $B = \text{dimensions of } x = [M^0LT^0]$

\therefore Dimensions of A

$$= \frac{\text{dimensions of } U \times \text{dimensions of } (x + B)}{\text{dimension of } \sqrt{x}}$$
$$[ML^2T^{-2}][M^0LT^0]$$

$$=\frac{[ML^2T^{-2}][M^0LT^0]}{[M^0L^{1/2}T^0]}$$

$$= \left[ML^{5/2}T^{-2} \right]$$

Hence, dimensions of AB

$$= [ML^{5/2}T^{-2}][M^0LT^0]$$

$$= \left[ML^{7/2}T^{-2} \right]$$



ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	D	A	В	D	С	A	D	A	В	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	D	A	С	С	A	С	С	A	С	D

