

## Topic :- UNITS AND MEASUREMENTS

1 (c)

$$\text{From } h = ut + \frac{1}{2}gt^2$$

$$h = 0 + \frac{1}{2} \times 9.8 \times (2)^2 = 19.6 \text{ m}$$

$$\frac{\Delta h}{h} = \pm 2 \frac{\Delta t}{t} \quad [\because a = g = \text{constant}]$$

$$= \pm 2 \left( \frac{0.1}{2} \right) = \pm \frac{1}{10}$$

$$\therefore \Delta h = \pm \frac{h}{10} = \pm \frac{19.6}{10} = \pm 1.96 \text{ m}$$

2 (a)

$$\text{Given, } W = \frac{1}{2}kx^2$$

Writing the dimensions on both sides

$$[ML^2T^{-2}] = k[M^0L^2T^0]$$

$$\therefore \text{Dimensions of } k = [MT^{-2}] = [ML^0T^{-2}]$$

3 (a)

$$\text{Given, } m = 3.513 \text{ kg and } v = 5.00 \text{ ms}^{-1}$$

$$\text{So, momentum, } p = mv = 17.565$$

As the number of significant digits in  $m$  is 4 and  $v$  is 3, so,  $p$  must have 3 significant digits

$$p = 17.6 \text{ kgms}^{-1}$$

4 (d)

$$\text{Modulus of rigidity} = \frac{\text{Shear stress}}{\text{Shear strain}} = [ML^{-1}T^{-2}]$$

5 (c)

The unit of physical quantity obtained by the line integral of electric field is  $JC^{-1}$ .

6 **(b)**

$$F = \frac{Gm_1m_2}{d^2}$$

$$\Rightarrow G = \frac{Fd^2}{m_1m_2}$$

$$[G] = \frac{[\text{MLT}^{-2}][\text{L}^2]}{[\text{M}^2]} = [\text{M}^{-1}\text{L}^3\text{T}^2]$$

Moment of inertia  $I = mK^2 = [\text{ML}^2]$

7 **(c)**

$$\text{Stress} = \frac{\text{Force}}{\text{Area}} = \frac{N}{\text{m}^2}$$

8 **(a)**

$$n_1u_1 = n_2u_2$$

$$n_2 = \frac{n_1u_1}{u_2}$$

$$= \frac{170.474L}{M^3}$$

$$= \frac{170.474 \times 10^{-3}M^3}{M^3}$$

$$= 0.170474$$

PE

9 **(c)**

$$\text{Intensity } (I) = \frac{\text{Energy}}{\text{Area} \times \text{time}}$$

10 **(d)**

By the principle of dimensions homogeneity

$$F = at^{-1}$$

$$[\text{MLT}^{-2}] = a[\text{T}^{-1}]$$

$$a = [\text{MLT}^{-1}]$$

Similarly for  $b = [\text{MLT}^{-4}]$

11 **(a)**

Let radius of gyration  $[k] \propto [h]^x [c]^y [G]^z$

By substituting the dimension of  $[k] = [L]$

$$[h] = [\text{ML}^2\text{T}^{-1}]$$

$$[c] = [\text{LT}^{-1}]$$

$$[G] = [M^{-1}L^3T^{-2}]$$

And by comparing the power of both sides

We can get  $x = 1/2, y = -3/2, z = 1/2$

Therefore dimension of radius of gyration is

$$[h]^{1/2}[c]^{-3/2}[G]^{1/2}$$

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**(a)**

Here,

Mass of a body,  $M = 5.00 \pm 0.05 \text{ kg}$

Volume of a body,  $V = 1.00 \pm 0.05 \text{ m}^3$

$$\text{Density, } \rho = \frac{M}{V}$$

Relative error in density is

$$\frac{\Delta\rho}{\rho} = \frac{\Delta M}{M} + \frac{\Delta V}{V}$$

Percentage error in density is

$$\frac{\Delta\rho}{\rho} \times 100 = \frac{\Delta M}{M} \times 100 + \frac{\Delta V}{V} \times 100$$

$$= \left(\frac{0.05}{5} \times 100\right) + \left(\frac{0.05}{1} \times 100\right) = 1\% + 5\% = 6\%$$

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**(c)**

Stefan's law is  $E = \sigma(T^4) \Rightarrow \sigma = \frac{E}{T^4}$

where,  $E = \frac{\text{Energy}}{\text{Area} \times \text{Time}} = \frac{\text{Watt}}{\text{m}^2}$

$$\sigma = \frac{\text{Watt} \cdot \text{m}^{-2}}{\text{K}^4} = \text{Watt} \cdot \text{m}^{-2} \text{K}^{-4}$$

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**(a)**

$y = a \sin(\omega t + kx)$ .

Here,  $\omega t$  should be dimensionless

$$\therefore [\omega] = \left[\frac{1}{t}\right]$$

$$[\omega] = [M^0L^0T^{-1}]$$

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**(c)**

Percentage error in  $T = \frac{0.01}{1.26} \times 100 + \frac{0.01}{9.80} \times 100$

$$+ \frac{0.01}{1.45} \times 100$$

$$= 0.8 + 0.1 + 0.7 = 1.6$$

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**(a)**

$$\frac{R}{L} = \frac{V/I}{V \times T/I} = \frac{1}{T} = \text{Frequency}$$

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**(b)**

$$\text{Pressure} = \frac{\text{Force}}{\text{Area}} = \frac{\text{Energy}}{\text{Volume}} = ML^{-1}T^{-2}$$

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**(b)**

The dimension of frequency ( $f$ ) =  $[T^{-1}]$

$$\begin{aligned}\text{The dimension of } \left(\frac{R}{L}\right) &= \frac{[ML^2T^{-3}A^{-2}]}{[ML^2T^2A^{-2}]} \\ &= \left[\frac{1}{T}\right] \\ &= [T^{-1}]\end{aligned}$$

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**(a)**

Area of rectangle

$$A = lb$$

$$= 10.5 \times 2.1$$

$$= 22.05 \text{ cm}^2$$

Minimum possible measurement of scale = 0.1 cm

So, area measured by scale =  $22.0 \text{ cm}^2$

PE

<b>ANSWER-KEY</b>										
Q.	1	2	3	4	5	6	7	8	9	10
A.	C	A	A	D	C	B	C	A	C	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	A	C	A	C	A	B	B	B	A

PE