CLASS : XITH DATE :

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Solutions

PRACTICE PROBLEM

SUBJECT : PHYSICS DPP NO. : 10

Topic :- SYSTEM OF PARTICLES AND ROTATIONAL MOTION

1

M.I. of the plate about an axis perpendicular to its plane and passing through its centre

 $I_0 = \frac{ma^2}{6}$

By parallel axes theorem

$$I_A = I_0 + m \left(\frac{a}{\sqrt{2}}\right)^2 = \frac{2}{3}ma^2$$

а

2

Moment of inertia of a disc

$$I = \frac{1}{2}MR^2$$

Disc is melted and recasted into a solid sphere.

∴ Volume of sphere=Volume of disc

$$\frac{\frac{4}{3}\pi R_1^3 = \pi R^2 \times \frac{R}{6}}{\frac{4}{3}R_1^3 = \frac{R^3}{6}}$$
$$R_1^3 = \frac{R^3}{8} \implies R_1 = \frac{R}{2}$$

∴ Moment of inertia of sphere

$$I' = \frac{2}{5}MR_1^2 = \frac{2}{5}M\left(\frac{R}{2}\right)^2 = \frac{2}{5}\frac{MR^2}{4} = \frac{1}{5}\left(\frac{1}{2}MR^2\right) = \frac{I}{5}$$
(c)

For solid cylinder, $\theta = 30^{\circ}$, $K^2 = \frac{1}{2}R^2$ For hollow cylinder, $\theta = ?$, $K^2 = R^2$

Using we find,

$$\frac{\left(1+\frac{1}{2}\right)}{\sin 30^{\circ}} = \frac{1+1}{\sin \theta}$$

3

$$\therefore \sin \theta = \frac{2}{3} = 0.6667$$
$$\theta = 42^{\circ}$$

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(c)

We can assume that three particles of equal mass *m* are placed at the corners of triangle $\vec{r}_1 = 0\hat{i} + 0\hat{j}$, $\vec{r}_2 = b\hat{i} + 0\hat{j}$

and
$$\vec{r}_{3} = 0\hat{i} + h\hat{j}$$

 $\therefore \vec{r}_{cm} = \frac{m_{1}\vec{r}_{1} + m_{2}\vec{r}_{2} + m_{3}\vec{r}_{3}}{m_{1} + m_{2} + m_{3}}$
(0,h)
(0,h)
(0,0)
(b,0)
(b,0)

$$=\frac{b}{3}\hat{i}+\frac{h}{3}\hat{j}$$

(d)

(b)

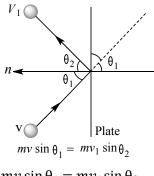
i.e. coordinates of centre of mass is $\left(\frac{b}{3}, \frac{h}{3}\right)$

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When a heavy body with velocity u collides with a lighter body at rest, then the heavier body remains moving in the same direction with almost same velocity. The lighter body moves in the same direction with a nearly velocity of 2u

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Since, no force is present along the surface of plane so, momentum conservation principle for ball is applicable along the surface of plate.



 $mv\sin\theta_1 = mv_1\sin\theta_2$

Or
$$v\sin\theta_1 = v_1\sin\theta_2$$

$$e = \frac{v_1 \cos \theta_2}{v \cos \theta_1} = \frac{v_1 \cos \theta_2}{v \cos \theta}$$

$$\therefore v_1 \cos \theta_2 = ev \cos \theta$$

$$\therefore \frac{v_1 \sin \theta_2}{v_1 \cos \theta_2} = \frac{v \sin \theta}{ev \cos \theta} = \frac{\tan \theta}{e}$$

$$\therefore \tan \theta = \frac{\tan \theta}{e}$$
$$\therefore \theta_2 = \tan^{-1} \left(\frac{\tan \theta}{e} \right)$$

7

(d)

(d)

(b)

We know that angular momentum of spin $= I\omega$ By the conservation of angular momentum

$$\frac{\frac{2}{5}MR^2 \cdot \frac{2\pi}{T} = \frac{2}{5}M\left(\frac{R}{4}\right)^2 \cdot \frac{2\pi}{T'}}{T' = \frac{T}{16} = \frac{24}{16} = 1.5h$$

8

Melting of ice produces water which will spread over larger distance away from the axis of rotation. This increases the moment of inertia so angular velocity decreases

9

(c)
Hence,
$$m_1 = 10 \text{ kg}, m_2 = 4 \text{ kg}$$

 $v_1 = 14 \text{ms}^{-1}, v_2 = 0$
 $v_{\text{CM}} = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2}$
 $v_{\text{CM}} = \frac{10 \times 14 + 4 \times 0}{10 + 4} = 10 \text{ms}^{-1}$

10

Let centre of mass of lead sphere after hollowing be at point O_2 , where $OO_2 = x$

Mass of spherical hollow
$$m = \frac{\frac{4}{3}\pi (\frac{R}{2})^2 M}{(\frac{4}{2}\pi R^3)} = \frac{M}{8}$$
 and
 $x = OO_1 = \frac{R}{2}$

$$\therefore x = \frac{M \times 0 - \left(\frac{M}{8}\right) \times \frac{R}{2}}{M - \frac{M}{8}} = \frac{\frac{MR}{16}}{\frac{7M}{8}} = -\frac{R}{14}$$

$$\therefore \text{ shift } = \frac{\pi}{14}$$
 (d)

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Angular momentum is given by

$$J = I\omega = \left(\frac{2MR^2}{5}\right)\omega$$
$$= \frac{2MR^2}{5} \times \frac{2\pi}{T} = \frac{4\pi MR^2}{5T}$$

12 **(a)**

Acceleration of each mass $= a = \left(\frac{m_1 \cdot m_2}{m_1 + m_2}\right)g$

Now acceleration of centre of mass of the system

$$A_{cm} = \frac{m_1 a_1 + m_1 a_2}{m_1 + m_2}$$

As both masses move with same acceleration but in opposite direction so $\overrightarrow{a_1} = -\overrightarrow{a_2} = a$ (let)

$$a \downarrow \boxed{m_2} a \uparrow$$

$$\therefore A_{cm} = \frac{m_1 a \cdot m_2 a}{m_1 + m_2}$$

$$= \left(\frac{m_1 \cdot m_2}{m_1 + m_2}\right) \times \left(\frac{m_1 \cdot m_2}{m_1 + m_2}\right) \times g = \left(\frac{m_1 \cdot m_2}{m_1 + m_2}\right)^2 \times g$$

13

(c)

If speed of man relative to plank be v, then it can be shown easily that speed of man relative to ground

$$v_{\rm mg} = v \frac{M}{\left(M + \frac{M}{3}\right)} = \frac{3}{4} v$$

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∴ Distance covered by man relative to ground

$$= L \frac{v_{\rm mg}}{v} = \frac{L}{v} \frac{3}{4} v = \frac{3L}{4}$$
(b)

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M.I. of disc
$$= \frac{1}{2}MR^2 = \frac{1}{2}M\left(\frac{M}{\pi t\rho}\right) = \frac{1}{2}\frac{M^2}{2\pi t\rho}$$

 $\left(As \ \rho = \frac{M}{\pi R^2 t} \text{ There fore } R^2 = \frac{M}{\pi t\rho}\right)$

If mass and thickness are same then, $I \propto \frac{1}{\rho}$

$$\therefore \frac{I_1}{I_2} = \frac{\rho_2}{\rho_1} = \frac{3}{1}$$

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(a)

(c)

If M = M' then bullet will transfer whole of its velocity (and consequently 100% of its KE) to block and will itself come to rest as per theory of collision.

Acceleration
$$a = \frac{v_{-}u_{-}}{t}$$

Or $a = \frac{v_{-}v_{0}}{t}$

Or
$$g = \frac{v \cdot v_0}{t}$$

 $\therefore v = 0$
Speed before first bounce
 $v_0 = -5ms^{-1}$
 $\therefore t = \frac{v_0 \cdot v_0}{s} = \frac{(-5)}{10} = \frac{5}{10} = 0.5 s$
(a)
 $m = 0.6 kg$
 $\sqrt{1-1}$
Mass per unit length $= \frac{0.6}{100} kgcm^{-1}$
Mass of part AB, $m_1 = \frac{0.6}{100} kgcm^{-1}$
Mass of part AB, $m_1 = \frac{0.6}{100} \times 20 = \frac{0.6}{5} kg$
Moment of inertia $= \frac{0.6 \times 4}{5} = \frac{2.4}{5} kg$
 $l = m_1(\frac{4g}{2})^2 + m_2(\frac{4g}{2})^2$
 $= \frac{0.6}{5} \times (\frac{2}{0} \times 10^2)^2 + \frac{24}{5} \times (\frac{60}{2} \times 10^2)^2$
 $= \frac{0.6}{5} \times (\frac{2}{0} \times 10^2)^2 + \frac{24}{5} \times (4 \times 10^{-1})^2$
 $= \frac{0.6}{5} \times 10^2 + \frac{2.4}{5} \times 16 \times 10^2$
 $= (\frac{0.6 + 3.4}{5}) \times 10^2$
 $= 7.8 \times 10^2 kg.m^2 = 0.078 kg.m^2$
(a)
 $P = \sqrt{p_x^2 + p_y^2}$
 $= \sqrt{(2 \cos t)^2 + (2 \sin t)^2} = 2$
If *m* be the mass of the body, then kinetic energy
 $= \frac{p_z^2}{2m} = \frac{(2)^2}{2m} = \frac{2}{m}$
Since kinetic energy does not change with time, both work done and power are zero
Now Power = F v \cos \theta = 0
As $F \neq 0, v \neq 0$
 $\therefore \cos \theta = 0$
Or $\theta = 90^\circ$
As direction of β is same that $\vec{v}(: \vec{v} = m\vec{v})$ hence angle between \vec{F} and \vec{p} is equal to 90°

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ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
А.	С	С	С	С	D	В	D	D	С	В
Q.	11	12	13	14	15	16	17	18	19	20
А.	D	А	С	В	А	D	С	В	А	A

