

Topic :- RAY OPTICS AND OPTICAL INSTRUMENTS

1

(a)

$$\text{Shift} = t\left(1 - \frac{1}{\mu}\right)$$

$$1 = 3\left(1 - \frac{1}{\mu}\right) \text{ or } \frac{1}{3} = 1 - \frac{1}{\mu}$$

$$\text{Or } \frac{1}{\mu} = 1 - \frac{1}{3} = \frac{2}{3} \text{ or } \mu = \frac{3}{2} = 1.5$$

2

(a)

$$A(\mu_v - \mu_r) + A'(\mu'_v - \mu'_r) = 0^\circ \Rightarrow A' = 5^\circ$$

3

(d)

$$P_1 = \frac{100}{20} = 5 \text{ D}, P_2 = \frac{100}{25} = 4 \text{ D}$$

$$\text{Effective power } P = P_1 + P_2 \\ = 5 + 4 = 9 \text{ D}$$

4

(b)

Lens-maker's formula is given by

$$\frac{1}{f} = (\mu_g - 1)\left(\frac{1}{R_1} - \frac{1}{R_2}\right) \quad \dots(i)$$

If the lens is immersed in a liquid of refractive index μ_1 then

$$\frac{1}{f_1} = (\mu_g - \mu_1)\left(\frac{1}{R_1} - \frac{1}{R_2}\right) \quad \dots(ii)$$

Here, μ_g is refractive index of glass w.r.t liquid

Dividing Eq. (i) by Eq. (ii), we have

$$\frac{f_1}{f} = \frac{(\mu_g - 1)}{(\mu_g - \mu_1)}$$

$$\Rightarrow \frac{f_1}{f} = \left(\frac{1.5 - 1}{1.25 - 1}\right)$$

$$\Rightarrow \frac{f_1}{f} = \frac{0.5 \times 1.25}{0.25} = 2.5$$

Hence, focal length increases by a factor of 2.5.

5

(d)

$$v = -15\text{cm}, u = -300\text{cm}$$

$$\text{From lens formula } \frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\Rightarrow \frac{1}{f} = \frac{1}{-15} - \frac{1}{-300} = \frac{-19}{300}$$

$$\Rightarrow f = \frac{-300}{19} = -15.8\text{ cm}$$

$$\text{and power } P = \frac{100}{f_{\text{in cm}}} = \frac{-100 \times 19}{300}$$

$$= -6.33\text{ D}$$

6

(b)

$$E_0 = \frac{I}{r^2} = \frac{I}{(4)^2} = \frac{I}{16}$$

$$E_p = \frac{I \cos \theta}{r'^2} = \frac{I \times (415)}{(5)^2}$$

$$= \frac{4I}{125}$$

$$\therefore \frac{E_0}{E_p} = \frac{I}{16} \times \frac{125}{4I} = \frac{125}{64}$$

9

(a)

$$\mu = \frac{h}{h'} \Rightarrow h' = \frac{8}{4/3} = 6\text{ m}$$

10

(a)

As there is no deflection between medium 1 and 2. Therefore, $\mu_1 = \mu_2$

11

(d)

$$\frac{I'}{I} = \frac{40 \times 40}{50 \times 50} = \frac{16}{25}$$

$$1 - \frac{I'}{I} = 1 - \frac{16}{25} = \frac{9}{25}$$

$$\text{or } \frac{I-I'}{I} \times 100 = \frac{9}{25} \times 100 = 36\%$$

12

(b)

According to Cartesian sign convention

$$u = -40\text{ cm}, R = -20\text{ cm}$$

$$\mu_1 = 1, \mu_2 = 1.33$$

Applying equation for refraction through spherical surface, we get

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

$$\frac{1.33}{v} - \frac{1}{-40} = \frac{1.33}{-20}$$

After solving, $v = -32\text{ cm}$

$$\text{The magnification is } m = \frac{h_2}{h_1} = \frac{\mu_1 v}{\mu_2 u}$$

$$\therefore \frac{h_2}{1} = -\frac{1(32)}{1.33(-40)}$$

Or $h_2 = 0.6 \text{ cm}$

The positive sign shows that the image is erect

13 **(c)**

Power of spectacles, $P = 2 \text{ D}$

Since, power is positive so lens used is convex which is used for the purpose of removing hypermetropia.

14 **(a)**

Refractive index of diamond is

$$\mu = \frac{\text{velocity of light in air}}{\text{velocity of light in diamond}}$$

$$2 = \frac{3.0 \times 10^{10}}{\text{velocity of light in diamond}}$$

So, velocity of light in diamond is

$$= \frac{3.0 \times 10^{10}}{2} = 1.5 \times 10^{10} \text{ cms}^{-1}$$

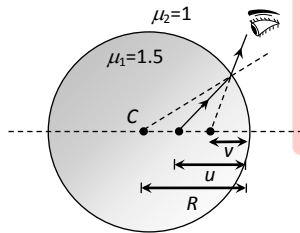
15 **(c)**

$$\mu_1 = 2, \mu_2 = \frac{3}{2}$$

$$2 \sin i \geq \frac{3}{2} \sin 90^\circ \Rightarrow \sin i \geq \frac{3}{4} \Rightarrow i \geq \sin^{-1}\left(\frac{3}{4}\right)$$

16 **(a)**

$v = 1 \text{ cm}, R = 2 \text{ cm}$



By using

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$
$$\frac{1}{-1} - \frac{1.5}{u} = \frac{1 - 1.5}{-2}$$

$$\Rightarrow u = -1.2 \text{ cm}$$

17 **(a)**

Lens maker's formula

$$\frac{1}{f} = (\mu - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

Where, $R_2 = \infty, R_1 = 0.3 \text{ m}$

$$\therefore \frac{1}{f} = \left(\frac{5}{3} - 1 \right) \left(\frac{1}{0.3} - \frac{1}{\infty} \right)$$

$$\Rightarrow \frac{1}{f} = \frac{2}{3} \times \frac{1}{0.3}$$

Or $f = 0.45 \text{ m}$

18 **(b)**

For an equilateral prism, angle of prism of refracting angle $A = 60^\circ$

Here, $\delta_m = A = 60^\circ$

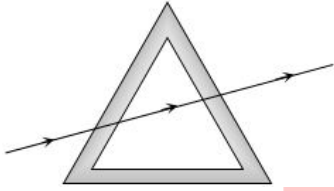
\therefore Refractive index,

$$\mu = \frac{\sin\left(\frac{A + \delta_m}{2}\right)}{\sin\frac{A}{2}} = \frac{\sin\left(\frac{60^\circ + 60^\circ}{2}\right)}{\sin\left(\frac{60^\circ}{2}\right)}$$

$$= \frac{\sin 60^\circ}{\sin 30^\circ} = \frac{\sin 60^\circ}{\cos 60^\circ}$$
$$= \tan 60^\circ = \sqrt{3}$$

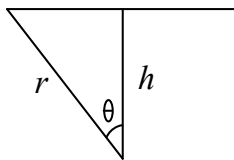
19 **(a)**

Effectively there is no deviation or dispersion



20 **(c)**

$$E = \frac{I \cos \theta}{r^2} \Rightarrow E = \frac{Ih}{r^3}$$



$$\text{Or } E \propto \frac{1}{r^3}$$

PEE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	A	D	B	D	B	D	A	A	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	D	B	C	A	C	A	A	B	A	C

PE