

## Topic :- RAY OPTICS AND OPTICAL INSTRUMENTS

1

(a)

$$\text{For the objective, } \frac{1}{v_o} - \frac{1}{-1/3.8} = \frac{1}{1/4}$$

$$\text{Or } \frac{1}{v_o} + 3.8 = 4 \text{ or } \frac{1}{v_o} = 0.2 = \frac{1}{5}$$

$$\text{or } v_o = 5 \text{ cm}$$

$$\text{Now, } M_o = \frac{5}{-\frac{1}{3.8}} = -19$$

$$\text{Again, } M = M_o \times M_e$$

$$-95 = -19 \times M_e \text{ or } M_e = \frac{95}{19} = 5$$

2

(b)

Frequency does not change with medium but wavelength and velocity decrease with the increase in refractive index

3

(b)

$$f = \frac{R}{\mu - 1} = \frac{10}{(1.5 - 1)} = 20 \text{ cm}$$

$$\frac{1}{f} = \frac{2}{f_1} + \frac{1}{f_m}, f_m = \infty \Rightarrow f = \frac{f_1}{2} = \frac{20}{2} = 10 \text{ cm}$$

4

(b)

$$f = \frac{f_1 f_2}{f_1 + f_2} = \frac{10(-10)}{10 + (-10)} = \frac{-100}{10 - 10} = \infty$$

5

(c)

$$\frac{1}{f} = (\mu - 1) \left( \frac{2}{R} \right) \text{ or } f = \frac{R}{2(\mu - 1)}$$

$$\text{Now, } f > R$$

$$\therefore \frac{R}{2(\mu - 1)} > R$$

$$\text{Or } \frac{1}{2(\mu - 1)} > 1 \text{ or } 2(\mu - 1) < 1$$

$$\text{Or } \mu - 1 < \frac{1}{2} \text{ or } \mu < \left( 1 + \frac{1}{2} \right)$$

$$\text{Or } \mu < 1.5$$

6

**(c)**

$$n = \frac{f}{f + u}$$

$$f + u = \frac{f}{n}$$

$$\text{Or } u = \frac{f}{n} - f = \left(\frac{1-n}{n}\right)f$$

$$\text{Or } u = -\left(\frac{n-1}{n}\right)f, |u| = \frac{n-1}{n}f$$

7

**(a)**

According to mirror formula

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

Here  $u = -9 \text{ m}$  and  $f = -1 \text{ m}$

$$\frac{1}{(-1)} - \frac{1}{(-9)} = \frac{1}{v}$$

$$\Rightarrow v = -\frac{9}{8} \text{ m}$$

As the object moves at a constant speed of 5 m/s after 1 s the new position of image is

$$u' = -9 \text{ m} + 5 \text{ m} = -4 \text{ m}$$

$$\therefore \frac{1}{(-1)} - \frac{1}{(-4)} = \frac{1}{v'}$$

$$\Rightarrow v' = -\frac{4}{3} \text{ m}$$

The shift in the position of image in 1 s is

$$v - v' = -\frac{9}{8} + \frac{4}{3} = \frac{1}{5}$$

$$\therefore \text{Average speed of image} = \frac{1}{5} \text{ m/s}$$

8

**(d)**

The image of object at infinity should be formed at 100 cm from the eye

$$\frac{1}{f} = \frac{1}{\infty} - \frac{1}{100} = -\frac{1}{100}$$

$$\text{So the power} = \frac{-100}{100} = -1 \text{ D}$$

[Distance is given in cm but  $P = \frac{1}{f}$  in metres]

9

**(b)**

$$\mu = \cot \frac{A}{2} = \frac{\sin\left(\frac{A + \delta m}{2}\right)}{\sin A/2}$$

$$\text{or } \frac{\cos \frac{A}{2}}{\sin \frac{A}{2}} = \frac{\sin\left(\frac{A + \delta m}{2}\right)}{\sin A/2}$$

$$\text{or } \sin\left(90^\circ - \frac{A}{2}\right) = \sin\left(\frac{A + \delta m}{2}\right)$$

$$\text{or } 90^\circ - \frac{A}{2} = \left(\frac{A + \delta m}{2}\right)$$

$$\text{or } 180^\circ - A = A + \delta m$$

$$\delta m = 180^\circ - 2A = \pi - 2A$$

10 (c)

Speed of light in air

Speed of light in aqueous humor

Wavelength of light in air

=  $\frac{\text{Wavelength of light in air}}{\text{Wavelength of light in aqueous humor}}$

$$\Rightarrow \frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2}$$

$$\text{Or } v_2 = \frac{\lambda_2}{\lambda_1} \times v_1 = \frac{474}{633} \times 3 \times 10^8$$

$$= 2.25 \times 10^8 \text{ms}^{-1}$$

11 (a)

$$M = \frac{f_o}{f_e}, 10 = \frac{f_o}{20}, f_o = 200 \text{ cm}$$

12 (a)

$$I \propto \frac{1}{r^2} \Rightarrow \frac{I_2}{I_1} = \frac{r_1^2}{r_2^2} = \frac{60^2}{180^2} = \frac{1}{9}$$

13 (b)

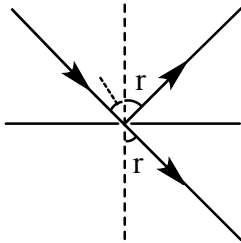
Here  $i = r$

$$r' = 90^\circ - r$$

$$\text{So, } \mu = \frac{\sin r'}{\sin r} = \frac{\sin(90^\circ - r)}{\sin r}$$

$$\mu = \frac{\cos r}{\sin r} = \frac{1}{\tan r}$$

$$\text{But } \mu = \frac{1}{\sin C}$$



Where  $C$  is the critical angle.

$$\text{So, } \frac{1}{\sin C} = \frac{1}{\tan r}$$

$$\Rightarrow \sin C = \tan r$$

$$\text{Or } C = \sin^{-1}(\tan r)$$

14 **(c)**

$$m = m_o \times m_e \Rightarrow m = m_o \times \left(1 + \frac{D}{f_e}\right)$$

$$\Rightarrow 100 = 10 \times \left(1 + \frac{25}{f_e}\right) \Rightarrow f_e = \frac{25}{9} \text{ cm}$$

15 **(a)**

$$n = \frac{360^\circ}{72^\circ} = 5$$

Note that  $\frac{360}{\theta}$  is odd and object line asymmetrically

16 **(d)**

$$f = \frac{1.6}{2} \text{ m} = 0.8 \text{ m}, u = -1 \text{ m}$$

$$\frac{1}{v} = \frac{1}{0.8} - \frac{1}{-1} = \frac{10}{8} + 1 = \frac{18}{8} = \frac{9}{4}$$

$$\text{Or } v = \frac{4}{9} \text{ m}$$

17 **(a)**

$$\frac{1}{f_a} = (\mu - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$= (1.5 - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right) \dots\dots\dots(i)$$

$$\text{and } \frac{1}{f_m} = \frac{\mu_g - \mu_m}{\mu_m} \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{f_m} = \left( \frac{1.5}{1.6} - 1 \right) \left( \frac{1}{R_1} - \frac{1}{R_2} \right) \dots\dots\dots(ii)$$

Thus,

$$\frac{f_m}{f_a} = \frac{(1.5 - 1)}{\left(\frac{1.5}{1.6} - 1\right)} = -8$$

$$f_m = -8 \times f_a$$

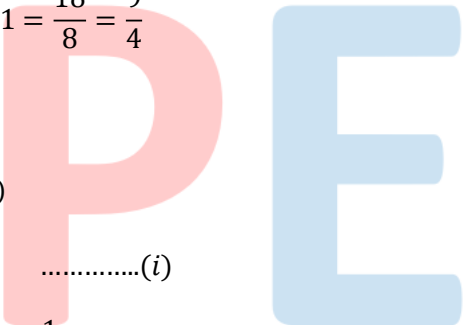
$$= -8 \times \frac{-1}{5} \quad \left( \because f_a = \frac{1}{p} = -\frac{1}{5} \text{ m} \right)$$

$$= 1.6 \text{ m}$$

$$\therefore P_m = \frac{\mu}{f_m}$$

$$= \frac{1.6}{1.6} = 1D$$

18 **(b)**



$$\mu = \frac{\sin\left(\frac{A + \delta_m}{2}\right)}{\sin \frac{A}{2}}$$

$$\sqrt{2} = \frac{\sin\left(\frac{60^\circ + \delta_m}{2}\right)}{\sin \frac{60^\circ}{2}}$$

$$\frac{1}{\sqrt{2}} = \sin\left(\frac{60^\circ + \delta_m}{2}\right)$$

$$\text{Or } \sin 45^\circ = \sin\left(\frac{60^\circ + \delta_m}{2}\right)$$

$$\delta_m = 30^\circ$$

$$\text{Or } i = \frac{A + \delta_m}{2}$$

$$= \frac{60 + 30}{2} = \frac{90}{2} = 45^\circ$$

19

**(c)**

$$\mu_g \sin \theta_c = \mu_1 \sin 90^\circ$$

$$\text{Or } \mu_g \sin \theta_c = 1$$

When water is poured,

$$\mu_w \sin r = \mu_s \sin \theta_c \text{ or } \mu_w \sin r = 1$$

$$\text{Again, } \mu_a \sin \theta = \mu_w \sin r$$

$$\text{Or } \mu_a \sin \theta = 1$$

$$\text{Or } \sin \theta = 1 \text{ or } \theta = 90^\circ$$

20

**(d)**

Form displacement method size of object,  $O = \sqrt{I_1 I_2}$

Here,  $O = 3$  cm,  $I_1 = 9$  cm

$$\therefore 3 = \sqrt{9 I_2}$$

$$\text{Or } I_2 = 1 \text{ cm}$$

<b>ANSWER-KEY</b>										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	B	B	B	C	C	A	D	B	C
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	A	B	C	A	D	A	B	C	D

PE