

Topic :- RAY OPTICS AND OPTICAL INSTRUMENTS

1 (b)

$$m = 1 + \frac{D}{f} = 1 + DP \text{ [} m \text{ increases with } P \text{]}$$

2 (d)

For first lens, $\mu_1 = -30\text{cm}, f_1 = 10\text{cm}$

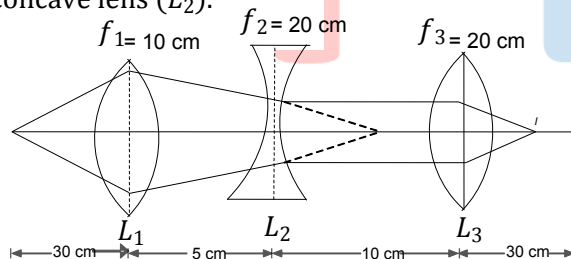
$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\text{or } \frac{1}{v} = \frac{1}{f} + \frac{1}{u}$$

$$\text{or } \frac{1}{v} = \frac{1}{10} - \frac{1}{30} = \frac{1}{15}$$

$$\text{or } v = 15\text{ cm}$$

Therefore, image formed by convex lens (L_1) is at point I_1 and acts as virtual object for concave lens (L_2).



The image I_1 is formed at focus of concave lens (as shown) and so emergent rays will be parallel to the principle axis. For lens L_2 , $\mu_2 = 15 - 5 = 10\text{ cm}$, $f_2 = -10\text{cm}$. These parallel rays are incident on the third convex lens (L_3) and will be brought to convergence at the focus of the lens (L_3)

Hence, distance of final image from third lens L_3

$$v_2 = f_3 = 30\text{ cm}$$

3 (c)

For no deviation,

$$(\mu - 1)A + (\mu' - 1)A' = 0$$

$$\Rightarrow A' = -\frac{(\mu - 1)A}{(\mu' - 1)} = \frac{(1.54 - 1)4^\circ}{(1.72 - 1)} = -3^\circ$$

Negative sign implies that two prisms should be connected in opposition.

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(b)

When an object is placed in front of such a lens, the rays are first of all refracted from the convex surface and again refracted from convex surface.

Let f_1, f_m be focal lengths of convex surface and mirror (plane polished surface)

respectively, then effective focal length is

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_m} + \frac{1}{f_1} = \frac{2}{f_1} + \frac{1}{f_m}$$

Since,

$$f_m = \frac{R}{2} = \infty$$

$$\therefore \frac{1}{F} = \frac{2}{f_1}$$

From lens formula

$$\frac{1}{f_1} = (\mu - 1)\left(\frac{1}{R}\right)$$

$$\therefore \frac{1}{F} = \frac{2(\mu - 1)}{R}$$

$$\Rightarrow F = \frac{R}{2(\mu - 1)}$$

$$\text{or } R_{eq} = 2F = \frac{R}{(\mu - 1)}$$

PE

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(b)

When a ray of light passes from glycerine (denser, $\mu = 1.47$) to water (rarer, $\mu = 1.33$) the angle of refraction (r) is greater than angle of incidence (i), then from Snell's law

$$\frac{\sin i}{\sin r} = \frac{\mu_2}{\mu_1} < 1$$

When $r = 90^\circ$, corresponding angle of incidence is known as critical angle, *ie*, $i = \theta_c$

$$\therefore \frac{\sin \theta_c}{\sin 90^\circ} = \frac{\mu_2}{\mu_1}$$

$$\Rightarrow \sin \theta_c = \frac{\mu_2}{\mu_1}$$

$$\Rightarrow \theta_c = \sin^{-1}\left(\frac{\mu_2}{\mu_1}\right)$$

$$= \sin^{-1}\left(\frac{1.33}{1.47}\right)$$

$$\theta_c = 64^\circ 48'$$

6 **(b)**
Note that two refractive indices are involved. Therefore, two images will be formed

9 **(a)**
Image formed by convex mirror is virtual for real object placed anywhere

10 **(a)**
Wavelength in vacuum,

$$\lambda = \frac{3 \times 10^8}{5 \times 10^{14}} \times 10^{10} \text{Å} = 0.6 \times 10^4 \text{Å}$$

$$= 6000 \text{Å}$$

$$\text{Now, } \mu = \frac{\lambda}{\lambda'}$$

$$\text{Or } \lambda' = \frac{\lambda}{\mu} = \frac{6000}{1.5} \text{Å} = 4000 \text{Å}$$

11 **(a)**
When two lenses are separated by some distance x , then equivalent power

$$P = P_1 + P_2 - xP_1P_2$$

$$\therefore P = 5 + 5 - x \times 5 \times 5$$

$$\text{or } P = 10 - 25x$$

Power P will be negative, if $10 - 25x$ will be negative

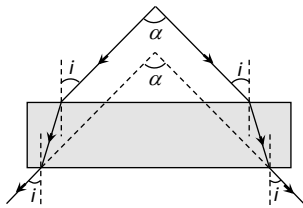
$$\text{ie, } 25x > 10$$

$$\text{or } x > \frac{10}{25}$$

$$\text{or } x > \frac{10}{25} \times 100 \text{ cm}$$

$$\text{or } x > 40 \text{ cm}$$

14 **(b)**
Since rays after passing through the glass slab just suffer lateral displacement hence we have angle between the emergent rays as α



15 **(c)**
 $\delta \propto (\mu - 1) \Rightarrow \mu_R$ is least so δ_R is least

16 **(a)**
The combined focal length of plano-convex lens

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2}$$

Given, $f_1 = \infty$ (for plane surface), $f_2 = f$ (say)

$$\therefore \frac{1}{F} = \frac{1}{\infty} + \frac{1}{f}$$

$$\Rightarrow F = f$$

Now when concave lens of same focal length is joined to first lens, then combined focal length

$$\frac{1}{F'} = \frac{1}{F_1} + \frac{1}{F_2}$$

$$= \frac{1}{f} - \frac{1}{f} \quad (\because F_1 = f, F_2 = -f)$$

$$= 0$$

$$F' = \infty$$

Thus, the image can be focused on infinity (∞) or focus shifts to infinity.

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(b)

In compound microscope objective forms real image while eye piece forms virtual image

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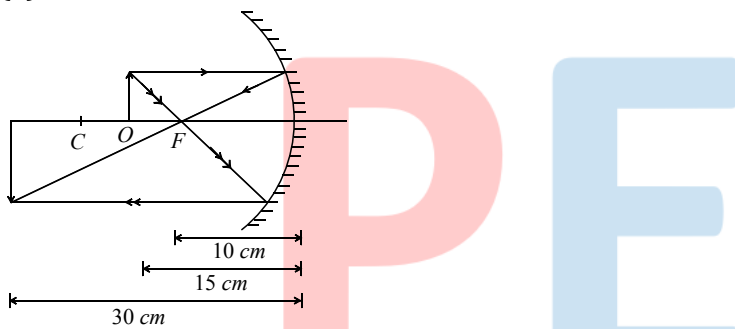
(a)

For viewing far objects, concave lenses are used and for concave lens

$$u = \text{wants to see} = -60 \text{ cm}; v = \text{can see} = -15 \text{ cm so from } \frac{1}{f} = \frac{1}{v} - \frac{1}{u} \Rightarrow f = -20 \text{ cm}$$

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(a)



According to New Cartesian sign convention,

Object distance $u = -15 \text{ cm}$

Focal length of a concave lens, $f = -10 \text{ cm}$

Height of the object $h_o = 2.0 \text{ cm}$

According to mirror formula, $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

$$\frac{1}{v} = \frac{1}{f} - \frac{1}{u} = \frac{1}{-10} - \frac{1}{-15} \Rightarrow v = -30 \text{ cm}$$

This image is formed 30 cm from the mirror on the same side of the object. It is a real image

Magnification of the mirror, $m = \frac{-v}{u} = \frac{h_i}{h_o}$

$$\Rightarrow \frac{-(-30)}{-15} = \frac{h_i}{2} \Rightarrow h_i = -4 \text{ cm}$$

Negative sign shows that image is inverted

The image is real, inverted, of size 4 cm at a distance 30 cm in front of the mirror

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	B	D	C	B	B	B	D	C	A	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	C	B	B	C	A	B	A	A	D

PE