Class: XIIth
Solutions

## Topic :- RAY OPTICS AND OPTICAL INSTRUMENTS

(d)

Convergence (or power) is independent of medium for mirror
(d)
$\frac{1}{F}=\frac{1}{f_{1}}+\frac{1}{f_{2}}=\frac{1}{60}+\frac{1}{(-20)} \Rightarrow F=-30$
(b)
$m=\frac{f}{f-u}$
If $m=+3$, then
$3=\frac{-24}{-24-u}$
Or $-24-u=-8$ or $u+24=8$
Or $u=8-24 \mathrm{~cm}=-16 \mathrm{~cm}$
If $m=-3$, then
$-3=\frac{-24}{-24-u}$
$u+24=-8$
Or $u=-32 \mathrm{~cm}$
(b)

The first images is due to reflection from the front surface ie unpolised surface of the mirror. So, only a small fraction is the incident light energy is reflected. The second image is due to reflection from polished surface. So, a major portion of light is reflected. Thus, the second image is the brightest
(d)

Given focal length of concave mirror
$f=-15 \mathrm{~cm}$
$u=-20 \mathrm{~cm}$
Magnification $m=\frac{f}{u-f}=\frac{-15}{-20+15}$
$m=3 \mathrm{~cm}$
The area enclosed by the image of the wire
$=m^{2}=9 \mathrm{~cm}^{2}$
(b)
$\frac{1}{u}+\frac{1}{v}=\frac{1}{f}$
$-\frac{d u}{u^{2}}-\frac{d v}{v^{2}}=0$
or $-\frac{d v}{v^{2}}=\frac{d u}{u^{2}}$
Or $\frac{d v}{d t}=-\frac{v^{2} d u}{u^{2} d t}=-\frac{10 \times 10}{30 \times 30} \times 9 \mathrm{~ms}^{-1}=-1 \mathrm{~ms}^{-1}$
(a)
$\frac{f}{f-u}=\frac{1}{4}=\frac{f}{f-(-0.5)}$
Or $4 f=f+0.5$ or $3 f=0.5$
Or $f=\frac{0.5}{3} \mathrm{~m}=0.17 \mathrm{~m}$
(c)

The critical angle $C$ is given by
$\sin C=\frac{n_{2}}{n_{1}}=\frac{\lambda_{1}}{\lambda_{2}}=\frac{3500}{7000}=\frac{1}{2} \Rightarrow C=30^{\circ}$
(d)

For a lens $m=\frac{f-v}{f}=-\frac{1}{f} v+1$
Comparing it with $y=m x+c$
Slope $=m=-\frac{1}{f}$
From graph, slope of the line $=\frac{b}{c}$
Hence $-\frac{1}{f}=\frac{b}{c} \Rightarrow|f|=\frac{c}{b}$
(d)
$I=\frac{L}{r^{2}}$
$\Rightarrow \frac{d I}{I}=-\frac{2 d r}{r} \quad[\because L=$ constant $]$
$\Rightarrow \frac{d I}{I} \times 100=-\frac{2 \times d r}{r} \times 100=-2 \times 1=-2 \%$
(c)

The rainbow is seen as a virtual image in the form of a coloured are centered on the antisolar point that is the point below the horizon, directly opposite the sun in the sky. When conditions are favorable two rainbows are seen the brighter is the primary and a fainter second one with the colours reversed. Hence, both primary and secondary rainbow are virtual images.
(d)

$I_{A}=\frac{L}{(2 r)^{2}}$ and $I_{B}=\frac{L}{(r \sqrt{2})^{2}} \cos \theta$
$=\frac{L}{2 r^{2}} \cdot \frac{r}{r \sqrt{2}}=\frac{L}{2 \sqrt{2} r^{2}}$
$\therefore \frac{I_{A}}{I_{B}}=\frac{2 \sqrt{2}}{4}=\frac{1}{\sqrt{2}}$
(a)

For vacuum $t=n \lambda_{o}$
For air $t=(n+1) \lambda_{a} \quad$...(ii)
From equation (i) and (ii)
$t=\frac{\lambda}{\mu-1}=\frac{6 \times 10^{-7}}{1.0003-1}\left(\mu=\frac{\lambda_{o}}{\lambda_{a}}\right)$
$=2 \times 10^{-3} \mathrm{~m}=2 \mathrm{~mm}$
(d)

Time of exposure $\propto \frac{1}{(\text { Aperture })^{2}}$
(c)
$\frac{f_{l}}{f_{a}}=\frac{\left({ }_{a} \mu_{g}-1\right)}{\left(\mu_{g}-1\right)} \Rightarrow f_{l}=\infty$ if $\mu_{g}=1 \Rightarrow{ }_{a} \mu_{l}={ }_{a} \mu_{g}$
(b)

Focal length of convex lens
$\frac{1}{f}=(\mu-1)\left(\frac{1}{R_{1}}-\frac{1}{R_{2}}\right)$
$R_{1}=10 \mathrm{~cm}, R_{2}=-10 \mathrm{~cm}, \mu=1.5$ (for glass)
$\frac{1}{f}=(1.5-1)\left(\frac{1}{10}-\frac{1}{-10}\right)$
$=0.5\left(\frac{2}{10}\right)$
$f=\frac{10}{2 \times 0.5}$
$\Rightarrow f=10 \mathrm{~cm}$
$\therefore$ Focal length of concave mirror
$=10 \mathrm{~cm}$
$\therefore$ Radius of curvature $=2 \times 10=20 \mathrm{~cm}$

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(a)
$u=-25 \mathrm{~cm}, v=+75 \mathrm{~cm}$
$\Rightarrow \frac{1}{f}=\frac{1}{+75}-\frac{1}{-25} \Rightarrow f=+18.75 \mathrm{~cm}$; convex lens
(a)

We have
$\sin C=\frac{1}{\mu}$
But $\mu=\frac{v_{2}}{v_{1}}=\frac{1480}{340}$
$\therefore \sin C=\frac{340}{1480}$
Or $C=\sin ^{-1}\left(\frac{340}{1480}\right)$

$$
=13.28^{\circ} \approx 13.3^{\circ}
$$



| ANSWER-KEY |  |  |  |  |  |  |  |  |  |  |  |  |  |
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| Q. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |  |  |
| A. | B | D | D | B | B | D | B | A | C | D |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Q. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |  |  |  |
| A. | A | D | C | D | A | D | C | B | A | A |  |  |  |
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