CLASS : XITh
Solutions
SUBJECT : PHYSICS
DPP NO. : 7

## Topic:- OSCILLATIONS

1

2
(d)

For SHM, $\frac{d^{2} y}{d t^{2}} \propto-y$
(a)
$a_{x}=a \cos \alpha=\mathrm{g} \sin \alpha \cos \alpha$ acting on the bob is given by

$=\mathrm{g}^{2} \cos ^{2} \alpha$
$\therefore \quad g_{\text {eff }}=\mathrm{g} \cos \alpha$
Now, $T^{\prime}=2 \pi \sqrt{\frac{L}{e_{\text {eff }}}}$
$=2 \pi \sqrt{\frac{L}{g \cos \alpha}}$
(b)

The acceleration of the vehicle down the plane $=g \sin \alpha$.
The reaction force acting on the bob of pendulum gives it an acceleration $a(=\operatorname{gsin} \alpha$ ) up the plane. This acceleration has two rectangular components,

And $a_{y}=a \sin \alpha=\mathrm{g} \sin ^{2} \alpha$ as shown in figure. The effective acceleration due to gravity
$\mathrm{g}_{\text {eff }}^{2}=a_{x}^{2}+\left(\mathrm{g}-a_{y}\right)^{2}=a_{x}^{2} \mathrm{~g}^{2}+a_{y}^{2}-2 \mathrm{~g} a_{y}$
$=\mathrm{g}^{2} \sin ^{2} \alpha \cos ^{2} \alpha+\mathrm{g}^{2} \sin ^{4} \alpha-2 \mathrm{~g} \times \operatorname{gsin}^{2} \alpha$
$=g^{2} \sin ^{2} \alpha\left(\cos ^{2} \alpha+\sin ^{2} \alpha\right)+g^{2}-2 g^{2} \sin ^{2} \alpha$
$=\mathrm{g}^{2} \sin ^{2} \alpha+\mathrm{g}^{2}-2 \mathrm{~g}^{2} \sin ^{2} \alpha=\mathrm{g}^{2}\left(1-\sin ^{2} \alpha\right)$

Torque acting on the bob
$=I \alpha=-(m g) l \sin \theta$
Or $\left(m_{i} l^{2}\right) \alpha=-\left(m_{g} g\right) l \theta$
Or $\alpha=-\left(\frac{m_{g} g}{m_{i} l}\right) \theta=-\omega^{2} \theta$;
Where $\omega^{2}=\frac{m_{g} g}{m_{i} l}$
$\therefore T=\frac{2 \pi}{\omega}=2 \pi \sqrt{\frac{m_{i} l}{m_{g} g}}$
(d)

The energy of simple harmonic oscillator

$$
E=\frac{1}{2} m \omega^{2} A^{2}
$$

or $\quad E \propto A^{2}$
$i e$, energy is proportional to square of the amplitude.
(c)

$$
\begin{aligned}
& y=0.2 \sin (10 \pi t+1.5 \pi) \cos (10 \pi t+1.5 \pi) \\
& =0.1 \sin 2(10 \pi t+1.5 \pi) \quad[\because \sin 2 A=2 \sin A \cos A] \\
& =0.1 \sin (20 \pi t+3.0 \pi) \\
& \therefore \text { Time period, } T=\frac{2 \pi}{\omega}=\frac{2 \pi}{20 \pi}=\frac{1}{10}=0.1 \mathrm{sec}
\end{aligned}
$$

## (b)

Two springs each of spring constant $k_{1}$ in parallel, given equailvalent spring constant of 2 $k_{1}$ and this is in series with spring of constant $k_{2}$, so equivalent spring constant,
$k=\left(\frac{1}{k_{2}}+\frac{1}{2 k_{1}}\right)^{-1}$
(b)

For displacement $O Q=40 \mathrm{~cm}$; let $t_{1}$ be the time taken then
$40=41 \sin \frac{2 \pi}{24} t_{1}$, on solving $t_{1}=5.16 \mathrm{~s}$
For displacement $O Q=-9 \mathrm{~cm}$, let $t_{2}$ be the time taken then $9=41 \sin \frac{2 \pi}{12} t_{2}$,
On solving $t_{2}=0.84 \mathrm{~s}$
Total time $=5.16+0.84=6.00 \mathrm{~s}$
(d)

The time period ( $T$ ) of a simple pendulum length $l$, is given by

$$
T=2 \pi \sqrt{\frac{l}{g}}=\frac{1}{\text { frequency }(n)}
$$

where g is acceleration due to gravity.

$$
\begin{array}{ll}
\therefore & \frac{n_{1}}{n_{2}}=\sqrt{\frac{l_{2}}{l_{1}}} \\
\Rightarrow & \frac{l_{1}}{l_{2}}=\left(\frac{n_{2}}{n_{1}}\right)^{2}
\end{array}
$$

Given, $\quad \frac{n_{2}}{n_{1}}=\frac{3}{2}$
$\therefore \quad \frac{l_{1}}{l_{2}}=\left(\frac{3}{2}\right)^{2}=\frac{9}{4}$
(a)

It is a system of two springs in parallel. The restoring force on the body is due to springs and not due to gravity pull. Therefore slope is irrelevant. Here the effective spring constant $=k+k=2 k$

Thus time period, $T=2 \pi \sqrt{M / 2 k}$
(b)

Here $a=12 \mathrm{cms}^{-2}, x=3 \mathrm{~cm}$
In SHM, acceleration $a=-\omega^{2} x$
$\therefore$ Magnitude of acceleration $a=\omega^{2} x$
(discarding off-ve sign)

$$
\begin{array}{rlrl}
\therefore & & \omega^{2} & =\frac{a}{x} \\
\text { or } & & \omega=\sqrt{\frac{a}{x}} \\
\text { or } & \frac{2 \pi}{T} & =\omega=\sqrt{\frac{a}{x}} \\
\text { or } & & T & =2 \pi \sqrt{\frac{a}{x}} \\
& & =2 \pi \sqrt{\frac{3}{12}} \\
& & =\pi s=3.14 \mathrm{~s}
\end{array}
$$

(d)

In S.H.M. $v=\omega \sqrt{a^{2}-y^{2}}$ and $a=-\omega^{2} y$ when $y=0$
$\Rightarrow v_{\text {max }}=a \omega$ and $a_{\text {min }}=0$
(b)

Body collides elastically with walls of room. So, there will be no loss in its energy and it will remain colliding with walls of room after a regular time interval, so it's motion will be periodic. Since acceleration is not proportional to displacement, so it's motion is not SHM (d)

$$
\begin{gathered}
y=A \sin \left(\frac{2 \pi}{T}\right) t \\
\Rightarrow \quad \frac{A}{2}=A \sin \left(\frac{2 \pi}{T}\right) t \\
\frac{\pi t}{2}=\frac{\pi}{6} \\
t=\frac{1}{3} \mathrm{~s}
\end{gathered}
$$

(b)

Let $k$ be the force constant of the shorter part of the spring of length $l / 3$. In a complete spring, three springs are in series each of force constant $k$

$$
k_{1}=k / 2=\frac{3 k}{2}
$$

$\therefore \frac{k}{k_{1}}=\frac{3 K}{3 K / 2}=2$ or $k: k_{1}=2: 1$
(c)

In S.H.M. frequency of K.E. and P.E.
$=2 \times$ (Frequency of oscillating particle)
(a)
$T=2=2 \pi \sqrt{\frac{M}{k}}$
and $2+1=2 \pi \sqrt{\frac{M+4}{k}}$
or $3=2 \pi \sqrt{\frac{k+4}{k}}$ so $\frac{4}{9}=\frac{M}{M+4}$
or $4 M+16=9 M$ or $M=\frac{16}{5}=3.2 \mathrm{~kg}$
(a)

Given K.E. $=P . E . \Rightarrow \frac{1}{2} m v^{2}=\frac{1}{2} k x^{2}$
$\Rightarrow \frac{1}{2} m \omega^{2}\left(a^{2}-x^{2}\right)=\frac{1}{2} m \omega^{2} x^{2}$
$\Rightarrow a^{2}-x^{2}=x^{2} \Rightarrow x^{2}=\frac{a^{2}}{2} \Rightarrow \frac{x}{a}=\frac{1}{\sqrt{2}}$
(b)

Acceleration in SHM is directly proportional to displacement and is always directed to its mean position
(a)

In S.H.M. when acceleration is negative maximum or positive maximum, the velocity is zero so kinetic energy is also zero. Similarly for zero acceleration, velocity is maximum so kinetic energy is also maximum

## ANSWER-KEY

| Q. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A. | A | D | B | D | C | B | B | B | D | A |
|  |  |  |  |  |  |  |  |  |  |  |
| Q. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| A. | B | D | B | D | B | C | A | A | B | A |
|  |  |  |  |  |  |  |  |  |  |  |



