CLASS : XITh

## Solutions

## Topic :- OSCILLATIONS

1

2
(b)

The acceleration of a particle in SHM is,

$$
\alpha_{\max }=-\omega^{2} A
$$

Where $\omega$ is angular velocity and $A$ the amplitude.
Given, $\quad y=2 \sin \left[\frac{\pi t}{2}+\emptyset\right]$
Standard equation of a wave in SHM is

$$
\begin{equation*}
y=A \sin (\omega t+\varnothing) \tag{iii}
\end{equation*}
$$

Comparing Eq. (i) with Eq. (ii), we get

$$
\begin{gathered}
A=2 \mathrm{~cm}, \omega=\frac{\pi}{2} \\
\therefore \quad \alpha_{\max }=-\left(\frac{\pi}{2}\right)^{2} \times 2 \\
=\frac{\pi^{2}}{2} \mathrm{cms}^{-2}
\end{gathered}
$$

(c)

When $t=0, x=r \cos \frac{\pi \times 0}{2}=r$;
When $t=3 s, x=r \cos \frac{\pi \times 3}{2}=0$
Here $\omega=\frac{\pi}{2}$ or $\frac{2 \pi}{T}=\frac{\pi}{2}$ or $T=4 s$
$\therefore$ In 3 sec , the particle goes from one extreme to other extreme and then back to mean position. So the distance travelled $=2 r+r=3 r$

Time period $T=2 \pi \sqrt{\frac{L}{g}}$
(b)

Force constant of a spring is given by $F=k x$

$$
6.4=k(0.1) \text { or } k=64 \mathrm{~N} / \mathrm{m}
$$

$$
\because T=2 \pi \sqrt{\frac{m}{k}} \Rightarrow \frac{\pi}{4}=2 \pi \sqrt{\frac{m}{64}} ; \frac{m}{64}=\left(\frac{1}{8}\right)^{2} ; m=1 \mathrm{~kg}
$$

(d)
$\tau_{A}=\tau_{B}=\left(m \mathrm{~g} \frac{L}{2} \sin \theta+M \mathrm{~g} L \sin \theta\right)$

$$
=\text { Restoring torque about point } O \text {. }
$$

In case $A$, moment of inertia will be more. Hence, angular acceleration ( $\alpha=\tau / I$ ) will be less. Therefore angular frequency will be less. Note Question is difficult because this type of SHM is rarely.

(d)

Function of wrist watch depends upon spring action so it is not effected by gravity but pendulum clock has time period, $T=2 \pi \sqrt{\frac{l}{g}}$. During free fall effective acceleration becomes zero, so time period comes out to be infinity, i.e., the clock stops
(d)

If $m$ is the mass, $r$ is the amplitude of oscillation, then maximum kinetic energy,
$K_{0}=\frac{1}{2} m \omega^{2} r^{2}$ or $\quad r=\left(\frac{2 K_{0}}{m \omega^{2}}\right)^{\frac{1}{2}}$
The displacement equation can be
$y=r \sin \omega t=\left(\frac{2 K_{0}}{m \omega}\right)^{\frac{1}{2}} \sin \omega t$
(c)


Spring $P$ and $Q, R$ and $S$ are in parallel then, $x=k+k=2 k \quad[$ for $P, Q]$
and $y=k+k=2 k \quad[$ for $R, S]$
$x$ and $y$ both in series
$\therefore \frac{1}{k^{\prime \prime}}=\frac{1}{x}+\frac{1}{y}=\frac{1}{k}$
Time period $T=2 \pi \sqrt{\frac{m}{k^{\prime \prime}}}=2 \pi \sqrt{\frac{m}{k}}$

10

12
(a)

$$
\begin{aligned}
& T=2 \pi \sqrt{\frac{m}{k}} \\
& =2 \pi \sqrt{\frac{0.2}{80}}=0.315
\end{aligned}
$$

(b)

Total potential energy $=0.04 \mathrm{~J}$
Resting potential energy $=0.01 \mathrm{~J}$
Maximum kinetic energy $=(0.04-0.01)$
$=0.03 \mathrm{~J}=\frac{1}{2} m \omega^{2} a^{2}=\frac{1}{2} k a^{2}$
$0.03=\frac{1}{2} \times k \times\left(\frac{20}{1000}\right)^{2}$
$k=0.06 \times 2500 \mathrm{~N} / \mathrm{m}=150 \mathrm{~N} / \mathrm{m}$


Spherical hollow ball filled with water $T=2 \pi \sqrt{\frac{l}{g}}$


Spherical hollow ball half filled with water $T_{1}=2 \pi \sqrt{\frac{l+\Delta l}{g}}$


Spherical hollow ball

$$
T_{2}=2 \pi \sqrt{\frac{l}{g}}
$$

and

$$
T_{1}>T_{2}
$$

Hence, time period first increases and then decreases to the original value.
(d)


Kinetic energy will be maximum at mean position.
From law of conservation of energy maximum kinetic energy at mean position = Potential energy at displaced position
$\Rightarrow K_{\text {max }}=m g \mathrm{~h}=m g l(1-\cos \theta)$
(a)

In this case time period of pendulum becomes

$T^{\prime \prime}=2 \pi \sqrt{\frac{l}{\left(g+\frac{q E}{m}\right)}}$
$\Rightarrow T^{\prime \prime}<T$
(c)
$y=0.25 \sin 200 t$;
Speed, $\frac{d y}{d t}=0.25 \times 200 \cos 200 t$
Max. speed $=0.25 \times 200=50 \mathrm{~cm} \mathrm{~s}^{-1}$
(d)

In simple harmonic motion
$y=a \sin \omega t$ and $v=a \omega \cos \omega t$ from this have $\frac{y^{2}}{a^{2}}+\frac{v^{2}}{a^{2} \omega^{2}}=1$, which is a equation of ellipse
(b)
$x=3 \sin \omega t+4 \sin (\omega t+\pi / 3)$
Comparing it with the equations
$x=r_{1} \sin \omega t+r_{2} \sin (\omega t+\phi)$
We have, $r_{1}=3 \mathrm{~cm}, r_{2}=4 \mathrm{~cm}$ and $\phi=\pi / 3$
The amplitude of combination is

$$
\begin{aligned}
& r=\sqrt{r_{1}^{2}+r_{2}^{2}+2 r_{1} r_{2} \cos \phi} \\
& =\sqrt{3^{2}+4^{2}+2 \times 3 \times 4 \times \cos \pi / 3} \\
& =\sqrt{37}=6 \mathrm{~cm}
\end{aligned}
$$

(c)

Time period is independent of mass of pendulum

19

20
(b)

A total restoring force, $F=k X=m g$
Or $k=m g / X$
Total mass that oscillates $=(M+m)$
$\therefore \quad T=2 \pi \sqrt{\frac{(M+m)}{m g / X}}=2 \pi \sqrt{\frac{(M+m) X}{m g}}$
(b)

Let $x$ be the maximum extension of the spring. From energy conservation


Loss in gravitational potential energy
= Gain in potential energy of spring
$M g x=\frac{1}{2} K x^{2}$
$\Rightarrow x=\frac{2 M g}{K}$

| ANSWER-KEY |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Q. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |  |  |
| A. | B | B | C | A | B | D | D | D | C | A |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Q. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |  |  |  |
| A. | B | A | D | A | C | D | B | C | B | B |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |



