

Topic :- MOTION IN A STRAIGHT LINE

1

(c)

$$\text{As } v^2 = v^2 - 2as \Rightarrow u^2 = 2as \quad (\because v = 0)$$

$$\Rightarrow u^2 \propto s \Rightarrow \frac{u_2}{u_1} = \left(\frac{s_2}{s_1}\right)^{1/2}$$

$$\Rightarrow u_2 = \left(\frac{9}{4}\right)^{1/2} u_1 = \frac{3}{2} u_1 = 300 \text{ m/s}$$

2

(b)

$$\int_0^x dx = \int_0^1 (v_0 + gt + ft^2) dt$$

$$x = v_0 + g\left(\frac{1}{2}\right) + f\left(\frac{1}{3}\right)$$

3

(d)

Let the car accelerate at rate α for time t_1 then maximum velocity attained,

$$v = 0 + at_1 = at_1$$

Now, the car decelerates at a rate β for time $(t - t_1)$ and finally comes to rest. Then,

$$0 = v - \beta(t - t_1) \Rightarrow 0 = at_1 - \beta t + \beta t_1$$

$$\Rightarrow t_1 = \frac{\beta}{\alpha + \beta} t$$

$$\therefore v = \frac{\alpha\beta}{\alpha + \beta} t$$

4

(b)

$$a = \sqrt{a_x^2 + a_y^2}$$

$$= \left[\left(\frac{d^2x}{dy}\right)^2 + \left(\frac{d^2y}{dt^2}\right)^2 \right]^{1/2}$$

Here, $\frac{d^2y}{dx^2} = 0$

Hence, $a = \frac{d^2x}{dt^2} = 8\text{ms}^{-2}$

5

(a)

Let t_1 and t_2 be times taken by the car to go from X to Y and then from Y to X respectively.

Then, $t_1 + t_2 = \frac{XY}{v_u} + \frac{XY}{v_d} = XY \left(\frac{v_u + v_d}{v_u v_d} \right)$

Total distance travelled

$$= XY + XY = 2 XY$$

Therefore, average speed of the car for this round trip is

Average speed = $\frac{\text{distance travelled}}{\text{time taken}}$

$$v_{\text{av}} = \frac{2 XY}{XY \left(\frac{v_u + v_d}{v_u v_d} \right)} \text{ or } v_{\text{av}} = \frac{2v_u v_d}{v_u + v_d}$$

6

(d)

Stopping distance $s \propto u^2$

$$\Rightarrow \frac{s_2}{40} = \left(\frac{90 \times \frac{5}{18}}{50 \times \frac{5}{18}} \right)^2$$

$$\Rightarrow s_2 = 129.6 \text{ m}$$

7

(c)

$$S \propto t^2 \Rightarrow \frac{S_1}{S_2} = \left(\frac{10}{20} \right)^2 \Rightarrow S_2 = 4S_1$$

8

(b)

$$\int_{6.25\sqrt{v}}^0 \frac{dv}{\sqrt{v}} = -2.5 \int_0^t dt$$

$$|2\sqrt{v}|_{6.25\sqrt{v}}^0 = -2.5t$$

$$2\sqrt{6.25} = 2.5t$$

$$t = 2 \text{ sec}$$

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(a)

$$\frac{1}{2} at^2 = vt \Rightarrow t = \frac{2v}{a}$$

10

(d)

Acceleration due to gravity is independent of mass of body

11 **(b)**

$$v = u + at$$

$$\Rightarrow -2 = 10 + a \times 4$$

$$\therefore a = -3 \text{ ms}^{-2}$$

12 **(c)**

$$\text{Acceleration} = a = \frac{dv}{dt} = 0.1 \times 2t = 0.2t$$

Which is time dependent *i.e.* non-uniform acceleration

13 **(c)**

Since acceleration due to gravity is independent of mass, hence time is also independent of mass (or density) of object

14 **(b)**

$$\text{Time of ascent} = \frac{u}{g} = 6 \text{ sec} \Rightarrow u = 60 \text{ m/s}$$

$$\text{Distance in first second } h_{\text{first}} = 60 - \frac{g}{2}(2 \times 1 - 1) = 55 \text{ m}$$

Distance in seventh second will be equal to the distance in first second of vertical downward motion

$$h_{\text{seventh}} = \frac{g}{2}(2 \times 1 - 1) = 5 \text{ m} \Rightarrow h_{\text{first}}/h_{\text{seventh}} = 11:1$$

15 **(b)**

$$x = a + bt^2, v = \frac{dx}{dt} = 2bt$$

$$\text{Instantaneous velocity } v = 2 \times 3 \times 3 = 18 \text{ cm/sec}$$

16 **(d)**

$$u = \sqrt{2gh} = \sqrt{2 \times 10 \times 20} = 20 \text{ m/s}$$

$$\text{and } T = \frac{2u}{g} = \frac{2 \times 20}{10} = 4 \text{ sec}$$

17 **(c)**

If a stone is dropped from height h then

$$h = \frac{1}{2}gt^2 \quad \dots\text{(i)}$$

if a stone is thrown upward with velocity u then

$$h = -u t_1 + \frac{1}{2}gt_1^2 \quad \dots\text{(ii)}$$

If a stone is thrown downward with velocity u then

$$h = ut_2 + \frac{1}{2}gt_2^2 \quad \dots\text{(iii)}$$

From (i) (ii) and (iii) we get

$$-ut_1 + \frac{1}{2}gt_1^2 = \frac{1}{2}gt^2 \quad \dots\text{(iv)}$$

$$ut_2 + \frac{1}{2}gt_2^2 = \frac{1}{2}gt^2 \quad \dots\text{(v)}$$

Dividing (iv) and (v) we get

$$\therefore \frac{-ut_1}{ut_2} = \frac{\frac{1}{2}g(t^2 - t_1^2)}{\frac{1}{2}g(t^2 - t_2^2)}$$

Or $\frac{t_1}{t_2} = \frac{t^2 - t_1^2}{t^2 - t_2^2}$

By solving $t = \sqrt{t_1 t_2}$

18

(d)

$$3t = \sqrt{3x} + 6 \Rightarrow 3x = (3t - 6)^2$$

$$\Rightarrow x = 3t^2 - 12t + 12$$

$$v = \frac{dx}{dt} = 6t - 12, \text{ for } v = 0, t = 2 \text{ sec}$$

$$x = 3(2)^2 - 12 \times 2 + 12 = 0$$

19

(b)

Let the total distance travelled by the body is $2S$. If t_1 is the time taken by the body to travel first half of the distance, then

$$t_1 = \frac{S}{2}$$

Let t_2 be the time taken by the body for each time interval for the remaining half journey.

$$\therefore S = 3t_2 + 5t_2 = 8t_2$$

So, average speed = $\frac{\text{Total distance travelled}}{\text{Total time taken}}$

$$= \frac{2S}{t_1 + 2t_2} = \frac{2S}{\frac{S}{2} + \frac{S}{4}} = \frac{8}{3} \text{ms}^{-1}$$

20

(a)

Displacement = Area of upper trapezium - Area of lower trapezium

$$= \frac{1}{2}(2 + 4) \times 4 - \frac{1}{2}(2 + 4)2 = 12 - 6 = 6\text{m}$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	C	B	D	B	A	D	C	B	A	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	C	C	B	B	D	C	D	B	A

PE