

Topic :- MOTION IN A STRAIGHT LINE

1 (a)

$$s = ut + \frac{1}{2}at^2$$

$$s = \frac{1}{2}at^2 \quad [\because u = 0]$$

It is an equation of parabola

2 (b)

Speed of stone in a vertically upward direction is 20m/s. So for vertical downward motion we will consider $u = -20 \text{ m/s}$

$$v^2 = u^2 + 2gh = (-20)^2 + 2 \times 9.8 \times 200 = 4320 \text{ m/s}$$

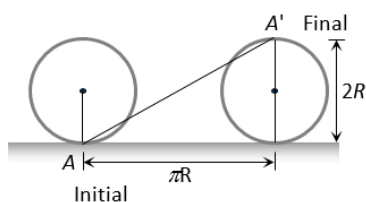
$$\therefore v \approx 65 \text{ m/s}$$

3 (a)

$$h = \frac{1}{2}gt^2 = \frac{1}{2} \times 10 \times (4)^2 = 80 \text{ m}$$

4 (c)

Horizontal distance covered by the wheel in half revolution = πR



So the displacement of the point which was initially in contact with ground

$$= AA' = \sqrt{(\pi R)^2 + (2R)^2}$$

$$= R\sqrt{\pi^2 + 4} = \sqrt{\pi^2 + 4} \quad [\text{As } R = 1\text{m}]$$

5 (b)

$$h = \frac{1}{2}gt^2$$

$$h' = \frac{1}{2}g(t - t_0)^2$$

$$h - h' = \frac{1}{2}g[t^2 - (t - t_0)^2]$$

$$= \frac{1}{2}g[t^2 - t^2 - t_0^2 + 2tt_0]$$

$$\Delta h = \frac{1}{2}gt_0(2t - t_0)$$

Δh is increasing with time

6 **(d)**

$$\begin{aligned} \text{Average acceleration} &= \frac{\text{Change in velocity}}{\text{Time taken}} = \frac{v_2 - v_1}{t_2 - t_1} \\ &= \frac{[10 + 2(5)^2] - [10 + 2(2)^2]}{3} = \frac{60 - 18}{3} = 14 \text{ m/s}^2 \end{aligned}$$

7 **(d)**

Relative velocity

$$= 10 + 5 = 15 \text{ m/sec}$$

$$\therefore t = \frac{150}{15} = 10 \text{ sec}$$

8 **(a)**

If a body starts from rest with acceleration α and then retards with retardation β and comes to rest. The total time taken for this journey is t and distance covered is S

$$\text{Then } S = \frac{1}{2} \frac{\alpha \beta t^2}{(\alpha + \beta)} = \frac{1}{2} \frac{5 \times 10}{(5 + 10)} \times t^2$$

$$\Rightarrow 1500 = \frac{1}{2} \frac{5 \times 10}{(5 + 10)} \times t^2 \Rightarrow t = 30 \text{ sec}$$

9 **(a)**

$$h = \frac{1}{2}gt^2 = \frac{1}{2} \times 10 \times (4)^2 = 80 \text{ m}$$

10 **(a)**

Effective speed of bullet

= speed of bullet + speed of police jeep

$$= 180 \text{ m/s} + 45 \text{ km/h} = (180 + 12.5) \text{ m/s} = 192.5 \text{ m/s}$$

Speed of thief's jeep = 153 km/h = 42.5 m/s

Velocity of bullet w.r.t. thief's car = 192.5 - 42.5 = 150 m/s

11 **(b)**

$$v = u + at$$

$$2 \times 100 = 100 + 10t \text{ or } t = 10 \text{ s}$$

12 **(b)**

Bullet will take $\frac{100}{1000} = 0.1 \text{ sec}$ to reach target.

During this period vertical distance (downward) travelled by the bullet = $\frac{1}{2}gt^2 = \frac{1}{2} \times 10 \times (0.1)^2 \text{ m} = 5 \text{ cm}$

So the gun should be aimed 5 cm above the target

13 **(a)**

$$\text{Average velocity} = \frac{2 \times 8 \times 12}{8 + 12} \text{ ms}^{-1} = 9.6 \text{ ms}^{-1}$$

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(a)

$$s = \frac{1}{2}gt^2, v = \frac{1}{2}g \times 2t = gt$$

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(b)

Average speed is the ratio of distance to time taken

Distance travelled from 0 to 5s = 40 m

Distance travelled from 5 to 10s = 0 m

Distance travelled from 10 to 15s = 60 m

Distance travelled from 15 to 20s = 20 m

So, total distance = 40 + 0 + 60 + 20 = 120 m

Total time taken = 20 minutes

Hence, average speed

$$= \frac{\text{distance travelled (m)}}{\text{time (min)}} = \frac{120}{20} = 6 \text{ m/min}$$

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(c)

From given figure, it is clear that the net displacement is zero. So average velocity will be zero

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(d)

$$v = \sqrt{2gh} \quad \dots(i)$$

After rebound, $v^2 = u^2 - 2gh$

Or $u^2 = v^2 + 2gh'$

$\therefore u^2 = 2gh' \quad \dots(ii)$

$$\therefore \frac{v^2}{u^2} = \frac{2gh}{2gh'}$$

Or $h' = h \times \frac{u^2}{v^2}$

$$= h \times \left(\frac{80}{100}\right)^2 = 0.64 h$$

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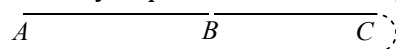
(b)

In this problem point starts moving with uniform acceleration a and after time t (Position B) the direction of acceleration get reversed i.e. the retardation of same value works on the point. Due to this velocity of points goes on decreasing and at position C its velocity becomes zero. Now the direction of motion of point reversed and it moves from C to A under the effect of acceleration a .

We have to calculate the total time in this motion.

Starting velocity at position A is equal to zero.

Velocity at position $B \Rightarrow v = at$ [As $u = 0$]



Distance between A and B, $S_{AB} = \frac{1}{2}at^2$

As same amount of retardation works on a point and it comes to rest therefore

$$S_{BC} = S_{AB} = \frac{1}{2}at^2$$

$\therefore S_{AC} = S_{AB} + S_{BC} = at^2$ and time required to cover this distance is also equal to t .

\therefore Total time taken for motion between A and C = $2t$

Now for the return journey from C to A ($S_{AC} = at^2$)

$$S_{AC} = ut + \frac{1}{2}at^2 \Rightarrow at^2 = 0 + \frac{1}{2}at_1^2 \Rightarrow t_1 = \sqrt{2}t$$

Hence total time in which point returns to initial point

$$T = 2t + \sqrt{2}t = (2 + \sqrt{2})t$$

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(c)

$$t = \sqrt{\frac{2h}{g+a}} = \sqrt{\frac{2 \times 2.7}{9.8 + 1.2}} = \sqrt{\frac{5.4}{11}} = \sqrt{0.49} = 0.7 \text{ sec}$$

As $u = 0$ and lift is moving upward with acceleration

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(d)

Man walks from his home to market with a speed of 5 km/h . Distance = 2.5 km and time

$= \frac{d}{v} = \frac{2.5}{5} = \frac{1}{2} \text{ hr}$ and he returns back with speed of 7.5 km/h in rest of time of 10 minutes

$$\text{Distance} = 7.5 \times \frac{10}{60} = 1.25 \text{ km}$$

$$\text{So, Average speed} = \frac{\text{Total distance}}{\text{Total time}}$$
$$= \frac{(2.5 + 1.25) \text{ km}}{(40/60) \text{ hr}} = \frac{45}{8} \text{ km/hr}$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	B	A	C	B	D	D	A	A	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	B	A	A	B	C	D	B	C	D

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