

TOPIC :- MOTION IN A STRAIGHT LINE

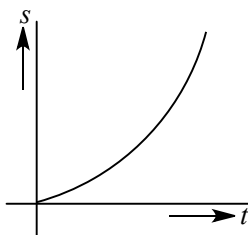
2

(a)

The equation of motion

$$s = ut + \frac{1}{2} at^2$$
$$= 0 + \frac{1}{2} at^2 = \frac{1}{2} at^2$$

The graph plot is as shown.



3

(b)

Let the initial velocity of ball be u

Time of rise $t_1 = \frac{u}{g+a}$ and height reached $= \frac{u^2}{2(g+a)}$

Time of fall t_2 is given by

$$\frac{1}{2}(g-a)t_2^2 = \frac{u^2}{2(g+a)}$$

$$\Rightarrow t_2 = \frac{u}{\sqrt{(g+a)(g-a)}} = \frac{u}{(g+a)} \sqrt{\frac{g+a}{g-a}}$$

$\therefore t_2 > t_1$ because $\frac{1}{g+a} < \frac{1}{g-a}$

4

(b)

$$v = u + at = u + \left(\frac{F}{m}\right)t = 20 + \left(\frac{100}{5}\right) \times 10 = 220 \text{ m/s}$$

5 **(d)**

If t_1 and t_2 are the time, when body is at the same height then,

$$h = \frac{1}{2}gt_1t_2 = \frac{1}{2} \times g \times 2 \times 10 = 10g$$

6 **(b)**

Relative velocity of one train w.r.t. other

$$= 10 + 10 = 20 \text{ m/s}$$

Relative acceleration = $0.3 + 0.2 = 0.5 \text{ m/s}^2$

If train crosses each other then from $s = ut + \frac{1}{2}at^2$

$$\text{As, } s = s_1 + s_2 = 100 + 125 = 225$$

$$\Rightarrow 225 = 20t + \frac{1}{2} \times 0.5 \times 0.5 \times t^2 \Rightarrow 0.5t^2 + 40t - 450 = 0$$

$$\Rightarrow t = \frac{-40 \pm \sqrt{1600 + 4 \cdot (0.05) \times 450}}{1} = -40 \pm 50$$

$\therefore t = 10 \text{ sec}$ (Taking +ve value)

7 **(a)**

Distance between the balls = Distance travelled by first ball in 3 seconds - Distance travelled by second ball in 2 seconds = $\frac{1}{2}g(3)^2 - \frac{1}{2}g(2)^2 = 45 - 20 = 25 \text{ m}$

8 **(b)**

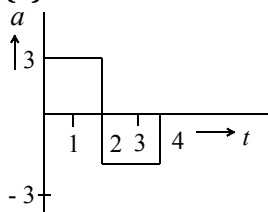
The velocity of balloon at height h , $v = \sqrt{2\left(\frac{g}{8}\right)h}$

When the stone released from this balloon, it will go upward with velocity, $= \frac{\sqrt{gh}}{2}$ (Same as that of balloon). In this condition time taken by stone to reach the ground

$$t = \frac{v}{g} \left[1 + \sqrt{1 + \frac{2gh}{v^2}} \right] = \frac{\sqrt{gh}/2}{g} \left[1 + \frac{2gh}{gh/4} \right]$$

$$= \frac{2\sqrt{gh}}{g} = 2\sqrt{\frac{h}{g}}$$

9 **(a)**



Taking the motion from 0 to 2 s

$$u = 0, a = 3 \text{ m/s}^2, t = 2 \text{ s}, v = ?$$

$$v = u + at = 0 + 3 \times 2 = 6 \text{ m/s}^{-1}$$

Taking the motion from 2 s to 4 s

$$v = 6 + (-3)(2) = 0 \text{ m/s}^{-1}$$

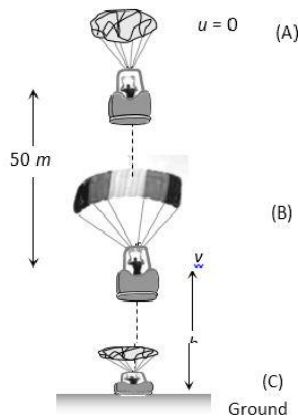
10 (a)

$$H_{\max} = \frac{u^2}{2g} \Rightarrow H_{\max} \propto \frac{1}{g}$$

On planet B value of g is $1/9$ times to that of A. So value of H_{\max} will become 9 times *i.e.* $2 \times 9 = 18 \text{ metre}$

11 (a)

After bailing out from point A parachutist falls freely under gravity. The velocity acquired by it will 'v'



$$\text{From } v^2 = u^2 + 2as = 0 + 2 \times 9.8 \times 50 = 980$$

$$[\text{As } u = 0, a = 9.8 \text{ m/s}^2, s = 50 \text{ m}]$$

At point B, parachute opens and it moves with retardation of 2 m/s^2 and reach at ground (point C) with velocity of 3 m/s

For the part 'BC' by applying the equation $v^2 = u^2 + 2as$

$$v = 3 \text{ m/s}, u = \sqrt{980} \text{ m/s}, a = -2 \text{ m/s}^2, s = h$$

$$\Rightarrow (3)^2 = (\sqrt{980})^2 + 2 \times (-2) \times h \Rightarrow 9 = 980 - 4h$$

$$\Rightarrow h = \frac{980 - 9}{4} = \frac{971}{4} = 242.7 \approx 243 \text{ m}$$

So, the total height by which parachutist bail out = $50 + 243 = 293 \text{ m}$

12 (d)

Acceleration due to gravity is independent of mass of body

13 (b)

$$\text{Distance average speed} = \frac{2v_1v_2}{v_1 + v_2} = \frac{2 \times 2.5 \times 4}{2.5 + 4}$$

$$= \frac{200}{65} = \frac{40}{13} \text{ km/hr}$$

14 (d)

$S \propto u^2$. If u becomes 3 times then S will become 9 times

i.e. $9 \times 20 = 180 \text{ m}$

15 (d)

$$\text{Average speed} = \frac{\text{Total distance}}{\text{Total time}} = \frac{x}{t_1 + t_2}$$

$$= \frac{x}{\frac{x/3}{v_1} + \frac{2x/3}{v_2}} = \frac{1}{\frac{1}{3 \times 20} + \frac{2}{3 \times 60}} = 36 \text{ km/hr}$$

16 (d)

$$\because v = 0 + na \Rightarrow a = v/n$$

Now, distance travelled in $n \text{ sec.} \Rightarrow S_n = \frac{1}{2}an^2$ and

distance travelled in $(n - 2) \text{ sec} \Rightarrow S_{n-2} = \frac{1}{2}a(n - 2)^2$

\therefore Distance travelled in last 2 seconds,

$$= S_n - S_{n-2} = \frac{1}{2}an^2 - \frac{1}{2}a(n - 2)^2$$

$$\frac{a}{2}[n^2 - (n - 2)^2] = \frac{a}{2}[n + (n - 2)][n - (n - 2)]$$

$$= a(2n - 2) = \frac{v}{n}(2n - 2) = \frac{2v(n - 1)}{n}$$

17 (c)

When packet is released from the balloon, it acquires the velocity of balloon of value 12 m/s . Hence velocity of packet after 2 sec , will be

$$v = u + gt = 12 - 9.8 \times 2 = -76 \text{ m/s}$$

18 (b)

Distance covered = Area enclosed by $v - t$ graph

$$= \text{Area of triangle} = \frac{1}{2} \times 4 \times 8 = 16 \text{ m}$$

19 (c)

Mass does not affect maximum height

$$H = \frac{u^2}{2g} \Rightarrow H \propto u^2, \text{ So if velocity is doubled then height will become four times. i.e. } H = 20 \times 4 = 80 \text{ m}$$

20 (c)

Distance covered in a particular time is

$$s_n = u + \frac{1}{2}g(2n - 1)$$

$$s_1 = 0 + \frac{1}{2}g(2 \times 1 - 1) = \frac{g}{2}$$

$$s_2 = 0 + \frac{1}{2}g(2 \times 2 - 1) = \frac{3}{2}g$$

$$\text{And } s_3 = 0 + \frac{1}{2}g(2 \times 3 - 1) = \frac{5}{2}g$$

Hence, the required ratio is

$$s_1 : s_2 : s_3 = \frac{g}{2} : \frac{3}{2}g : \frac{5}{2}g = 1 : 3 : 5$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	C	A	B	B	D	B	A	B	A	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	D	B	D	D	D	C	B	C	C

PE