

## Topic :- KINETIC THEORY

1 (c)

Kinetic energy  $\propto$  Temperature

2 (d)

$$PV = nRT$$

$$\Rightarrow PV = \frac{\omega}{M} RT$$

$$\frac{PM}{RT} = \frac{\omega}{V} = e$$

$$\Rightarrow e = \frac{PM}{RT} = \frac{P \times m \times N_A}{RT} = \frac{Pm}{\left(\frac{R}{N_A}\right)T} = \frac{Pm}{kT}$$

3 (b)

Thermal energy corresponds to internal energy

$$\text{Mass} = 1 \text{ kg}$$

$$\text{Density} = 4 \text{ kg m}^{-3}$$

$$\text{Volume} = \frac{\text{Mass}}{\text{Density}} = \frac{1}{4} \text{ m}^3$$

$$\text{Pressure} = 8 \times 10^4 \text{ Nm}^{-2}$$

$$\therefore \text{Internal energy} = \frac{5}{2} p \times V = 5 \times 10^4 \text{ J}$$

4 (b)

$$V_t = V_0(1 + at) = 0.5 \left( 1 + \frac{1}{273} \times 819 \right) = 2 \text{ litre} = 2 \times 10^{-3} \text{ m}^3$$

5 (c)

$$\text{Here, } m = 10 \text{ g} = 10^{-2} \text{ kg}$$

$$v = 300 \text{ ms}^{-1}, \theta = ? \text{C}, = 150 \text{ J} \cdot \text{kg}^{-1} \text{K}^{-1}$$

$$Q = \frac{50}{100} \left( \frac{1}{2} mv^2 \right) = \frac{1}{4} \times 10^{-2} (300)^2 = 225 \text{ J}$$

$$\text{From } Q = cm\theta$$

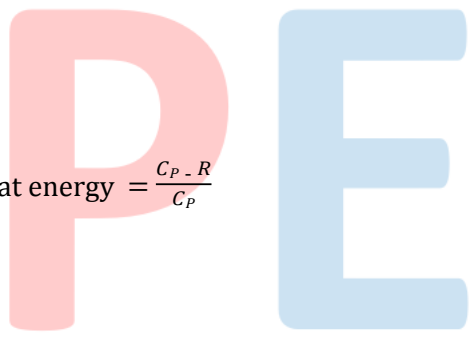
$$\theta = \frac{Q}{cm} = \frac{225}{150 \times 10^{-2}} = 150^\circ\text{C}$$

6 (a)  
 At constant temperature  
 $PV = \text{constant}$   
 $\Rightarrow \frac{P_1}{P_2} = \frac{V_2}{V_1} \Rightarrow \frac{70}{120} = \frac{V_2}{1200} \Rightarrow V_2 = 700 \text{ ml}$

7 (d)  
 $P \propto \frac{1}{V} \Rightarrow \frac{V_2}{V_1} = \frac{P_1}{P_2} = \frac{100}{105} \Rightarrow V_2 = \frac{100}{105} V_1 = 0.953 V_1$   
 % change in volume =  $\frac{V_1 - V_2}{V_1} \times 100$   
 $= \frac{V_1 - 0.953V_1}{V_1} \times 100 = 4.76\%$

8 (a)  
 Average kinetic energy  $E = \frac{f}{2}kT = \frac{3}{2}kT$   
 $\Rightarrow E = \frac{3}{2} \times (1.38 \times 10^{-23})(273 + 30) = 6.27 \times 10^{-21} \text{ J}$   
 $= 0.039 \text{ eV} < 1 \text{ eV}$

9 (c)  
 $\therefore C_p - C_v = R$   
 Fractional part of heat energy =  $\frac{C_p - R}{C_p}$   
 $= \frac{\frac{7}{2}R - R}{\frac{7}{2}R} = \frac{5}{7}$



10 (c)  
 RMS velocity doesn't depend upon pressure, it depends upon temperature only,  
 i.e.,  $v_{\text{rms}} \propto \sqrt{T}$ .  
 $\Rightarrow \frac{v_1}{v_2} = \sqrt{\frac{T_1}{T_2}} \Rightarrow \frac{200}{v_2} = \sqrt{\frac{(273 + 27)}{(273 + 127)}} = \sqrt{\frac{300}{400}}$   
 $\Rightarrow v_2 = \frac{400}{\sqrt{3}} \text{ m/s}$

11 (a)  
 $\frac{F}{2}n_1kT_1 + \frac{F}{2}n_2kT_2 + \frac{F}{2}n_3kT_3$   
 $= \frac{F}{2}(n_1 + n_2 + n_3)kT$   
 $T = \frac{n_1T_1 + n_2T_2 + n_3T_3}{n_1 + n_2 + n_3}$

12 (a)  
 As  $\rho - \rho_0(1 - \gamma\Delta T)$

$$\begin{aligned} \therefore 9.7 &= 10(1 - \gamma \times 100) \\ \frac{9.7}{10} &= 1 - \gamma \times 100 \\ \gamma \times 100 &= 1 - \frac{9.7}{10} = \frac{0.3}{10} = 3 \times 10^{-2} \\ \gamma &= 3 \times 10^{-4} \therefore \alpha = \frac{1}{3} \gamma = 10^{-4} \text{C}^{-1}. \end{aligned}$$

14 **(b)**

Let the temperature of junction be  $\theta$ . In equilibrium, rate of flow of heat through rod 1 = sum of rate of flow of heat through rods 2 and 3.

$$\begin{aligned} \left(\frac{dQ}{dt}\right)_1 &= \left(\frac{dQ}{dt}\right)_2 + \left(\frac{dQ}{dt}\right)_3 \\ KA \frac{(\theta - 0)}{l} &= \frac{KA(90^\circ - \theta)}{l} + \frac{KA(90^\circ - \theta)}{l} \\ \theta &= 2(90^\circ - \theta) \\ 3\theta &= 180^\circ, \theta = \frac{180^\circ}{3} = 60^\circ \end{aligned}$$

15 **(a)**

$$\begin{aligned} \frac{P_1 V_1}{T_1} &= \frac{P_2 V_2}{T_2} \\ \frac{(P + h\rho g)1.0}{273 + 12} &= \frac{P \cdot V_2}{273 + 35} \\ V_2 &= 5.4 \text{cm}^3 \end{aligned}$$

16 **(d)**

Average kinetic energy  $\propto$  Temperature

$$\Rightarrow \frac{E_1}{E_2} = \frac{T_1}{T_2} \Rightarrow \frac{100}{E_2} = \frac{300}{450} \Rightarrow E_2 = 150 \text{J}$$

17 **(a)**

Let  $p_1$  and  $p_2$  are the initial and final pressures of the gas filled in A. Then

$$\begin{aligned} p_1 &= \frac{n_A RT}{V} \quad \text{and} \quad p_2 = \frac{n_A RT}{2V} \\ \Delta p &= p_2 - p_1 = -\frac{n_A RT}{2V} \\ &= -\left(\frac{m_A}{M}\right) \frac{RT}{2V} \quad \dots(i) \end{aligned}$$

where  $M$  is the atomic weight of the gas.

$$\text{Similarly, } 1.5\Delta p = -\left(\frac{m_B}{M}\right) \frac{RT}{2V} \quad \dots(ii)$$

Dividing Eq.(ii) by Eq. (i), we get

$$\begin{aligned} 1.5 &= \frac{m_B}{m_A} \quad \text{or} \quad \frac{3}{2} = \frac{m_B}{m_A} \\ \text{or} \quad 3m_A &= 2m_B \end{aligned}$$

18 **(c)**

$$\text{From } \frac{\Delta Q}{\Delta t} = KA \left( \frac{\Delta T}{\Delta x} \right)$$

$$\Delta t = \frac{\Delta Q \Delta x}{KA(\Delta T)}$$

In arrangement (b),  $A$  is doubled and  $\Delta x$  is halved.

$$\therefore \Delta t \rightarrow \frac{1/2}{2} \rightarrow \frac{1}{4} \text{ time}$$

$$\text{ie, } \frac{1}{4} \times 4 \text{ min} = 1 \text{ min}$$

19 **(b)**

Here,  $m = 0.1 \text{ kg}$ ,  $h_1 = 10 \text{ m}$ ,  $h_2 = 5.4 \text{ m}$

$c = 460 \text{ J}\cdot\text{kg}^{-1}\cdot\text{C}^{-1}$ ,  $g = 10 \text{ ms}^{-2}$ ,  $\theta = ?$

Energy dissipated,  $Q = mg(h_1 - h_2)$

$$= 0.1 \times 10(10 - 5.4) = 4.6 \text{ J}$$

From  $Q = cm\theta$

$$\theta = \frac{Q}{cm} = \frac{4.6}{460 \times 0.1} = 0.1^\circ\text{C}$$

20 **(b)**

Root mean square speed

$$v_{\text{rms}} \propto \frac{1}{\sqrt{\rho}}$$

$$\therefore \frac{v_{\text{rms1}}}{v_{\text{rms2}}} = \sqrt{\frac{\rho_2}{\rho_1}}$$

$$\text{Given, } \frac{\rho_1}{\rho_2} = \frac{9}{8}$$

$$\Rightarrow \frac{v_{\text{rms1}}}{v_{\text{rms2}}} = \sqrt{\frac{8}{9}} = \frac{2\sqrt{2}}{3}$$

ANSWER-KEY

Q.	1	2	3	4	5	6	7	8	9	10
A.	C	D	B	B	C	A	D	A	C	C
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	A	A	B	A	D	A	C	B	B

PE