

Topic :- KINETIC THEORY

1 (d)

Let initial conditions = V, T

And final conditions = V', T'

By Charle's law $V \propto T$ [P remains constant]

$$\frac{V}{T} = \frac{V'}{T'} \Rightarrow \frac{V}{T} = \frac{V'}{1.2T'} \Rightarrow V' = 1.2V$$

But as per question, volume is reduced by 10% means

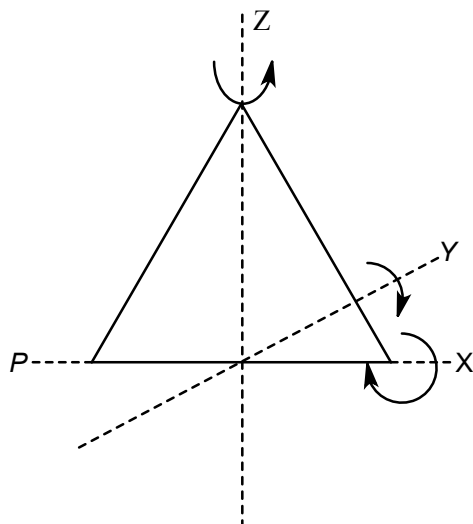
$$V' = 0.9V$$

So percentage of volume leaked out

$$= \frac{(1.2 - 0.9)V}{1.2V} \times 100 = 25\%$$

2 (c)

As temperature requirement is not given so, the molecule of a triatomic gas has a tendency of rotating about any of three coordinate axes. So, it has 6 degrees of freedom; 3 translational and 3 rotational.



Thus,

(3 translational+3 rotational) at room temperature.

3 (c)

$$\begin{aligned} \text{We have } v_{\text{rms}} &= \sqrt{\frac{v_1^2 + v_2^2 + \dots + v_n^2}{n}} \\ &= \sqrt{\frac{4 + 25 + 9 + 36 + 9 + 25}{6}} \\ &= \sqrt{\frac{108}{6}} = \sqrt{18} = 3\sqrt{2} = 3 \times 1.414 = 4.242 \text{ unit.} \end{aligned}$$

4 (a)

According to ideal gas equation

$$PV = nRT \text{ or } \frac{V}{T} = \frac{nR}{P}$$

At constant pressure

$$\frac{V}{T} = \text{constant}$$

Hence graph (a) is correct

5 (a)

Temperatures $T_1 = 15^\circ\text{C} = 15 + 273 = 288 \text{ K}$

$T_2 = 35^\circ\text{C} = 35 + 273 = 308 \text{ K}$

Volume remains constant.

$$\text{So, } \frac{p_1}{T_1} = \frac{p_2}{T_2}$$

$$\frac{p_1}{p_2} = \frac{T_1}{T_2} \Rightarrow \frac{p_1}{p_2} = \frac{288}{308}$$

$$\frac{p_2}{p_1} = \frac{308}{288}$$

$$\begin{aligned} \% \text{ increases in pressure} &= \frac{p_2 - p_1}{p_1} \times 100 \\ &= \frac{308 - 288}{288} \times 100 \approx 7\% \end{aligned}$$

6 (c)

$$v_{\text{av}} = \sqrt{\frac{8RT}{\pi M}} \Rightarrow T \propto M \quad [\because v_{\text{av}}, R \rightarrow \text{constant}]$$

$$\Rightarrow \frac{T_{H_2}}{T_{O_2}} = \frac{M_{H_2}}{M_{O_2}} \Rightarrow \frac{T_{H_2}}{(273 + 31)} = \frac{2}{32}$$

$$\Rightarrow T_{H_2} = 19 \text{ K} = -254^\circ\text{C}$$

7 (d)

Kinetic energy per *g mole* $E = \frac{f}{2}RT$

If nothing is said about gas then we should calculate the translational kinetic energy

$$\text{i.e., } E_{\text{Trans}} = \frac{3}{2}RT = \frac{3}{2} \times 8.31 \times (273 + 0) = 3.4 \times 10^3 \text{ J}$$

8 (a)

According to Gay Lussac's law $p \propto T$

$$\begin{aligned}\therefore \frac{dp}{p} \times 100 &= \frac{dT}{T} \times 100 \\ 1 &= \frac{1}{T} \times 100 \\ \Rightarrow T &= 100 \text{ K}\end{aligned}$$

9 (c)

Specific heat at constant pressure (C_p) is the amount of heat (Q) required to raise n moles of substance by $\Delta\theta$ when pressure is kept constant. Then

$$C_p = \frac{Q}{n\Delta\theta}$$

Given, $Q=70$ cal, $n = 2$,
 $\Delta\theta = (35 - 30)^\circ\text{C} = 5^\circ\text{C}$

$$\therefore C_p = \frac{70}{2 \times 5} = 7 \text{ cal mol}^{-1} \cdot \text{K}^{-1}$$

From Mayer's formula $C_p - C_V = R$

where R is gas constant ($= 2 \text{ cal mol}^{-1}$)

$$\therefore 7 - C_V = 2$$

$$\Rightarrow C_V = 5 \text{ cal mol}^{-1} \cdot \text{K}^{-1}$$

Hence, amount of heat required at constant volume (C_V) is

$$Q' = nC_V\Delta\theta$$

$$Q' = 2 \times 5 \times 5 = 50 \text{ cal}$$

10 (b)

$v_{rms} \propto \sqrt{T}$; To double the *rms* velocity temperature should be made four times, *i.e.*,
 $T_2 = 4T_1 = 4(273 + 0) = 1092\text{K} = 819^\circ\text{C}$

11 (b)

In a given mass of the gas

$$n = \frac{pV}{kT}$$

k being Boltzmann's constant.

12 (d)

$$\begin{aligned}PV = NkT &\Rightarrow \frac{N_A}{N_B} = \frac{P_A V_A}{P_B V_B} \times \frac{T_B}{T_A} \\ \Rightarrow \frac{N_A}{N_B} &= \frac{P \times V \times (2T)}{2P \times \frac{V}{4} \times T} = 4\end{aligned}$$

13 (b)

$$VP^3 = \text{constant} = k \Rightarrow P = \frac{k}{V^{1/3}}$$

$$\text{Also } PV = \mu RT \Rightarrow \frac{k}{V^{1/3}} \cdot V = \mu RT \Rightarrow V^{2/3} = \frac{\mu RT}{k}$$

Hence $\left(\frac{V_1}{V_2}\right)^{2/3} = \frac{T_1}{T_2} \Rightarrow \left(\frac{V}{27V}\right)^{2/3} = \frac{T}{T_2} \Rightarrow T_2 = 9T$

14 **(d)**

Vander waal's equation is followed by real gases

15 **(b)**

Molecular mass of He; $M = 4g$

\Rightarrow Molar value of $C_V = MC_V = 4 \times 3 = 12 \frac{J}{mole \cdot kelvin}$

At constant volume $P \propto T$, therefore on doubling the pressure temperature also doubles
i.e., $T_2 = 2T_1 \Rightarrow \Delta T = T_2 - T_1 = 273K$

Also $(\Delta Q)_V = \mu C_V \Delta T = \frac{1}{2} \times 12 \times 273 = 1638J$

16 **(a)**

Here, $h_1 = 50 \text{ cm}$, $t_1 = 50^\circ\text{C}$

$h_2 = 60 \text{ cm}$, $t_2 = 100^\circ\text{C}$

Now, $\frac{h_1}{h_2} = \frac{d_2}{d_1} = \frac{d_0}{1 + \gamma t_2} \times \frac{1 + \gamma t_1}{d_0}$

$\frac{50}{60} = \frac{1 + \gamma \times 50}{1 + \gamma \times 100}$

$\therefore \gamma = \frac{1}{200} = 0.005^\circ\text{C}^{-1}$

17 **(d)**

Vander Waal's gas constant $b = 4 \times$ total volume of all the molecules of the gas in the enclosure

Or $b = 4 \times N \times \frac{4}{3}\pi\left(\frac{d}{2}\right)^3 = \frac{2}{3}\pi N d^3$

$= \frac{2}{3} \times 3.14 \times 6.02 \times 10^{23} \times (2.94 \times 10^{-10})^3 = 32 \times 10^{-6} \frac{m^3}{mol}$

18 **(a)**

From ideal gas equation

$pV = nkT$

$p = \frac{n}{V}kT$

Here, $\frac{n}{V} = 5/\text{cm}^3 = 5 \times 10^6/\text{m}^3$

$\therefore p = (5 \times 10^6/\text{m}^3)(1.38 \times 10^{-23}/\text{JK}^{-1}) \times 3\text{K}$

$p = 20.7 \times 10^{-17} \text{ Nm}^{-2}$

19 **(d)**

Escape velocity from the earth's surface is 11.2 km/sec

So, $v_{rms} = v_{\text{escape}} = \sqrt{\frac{3RT}{M}} \Rightarrow T = \frac{(v_{\text{escape}})^2 \times M}{3R}$

$= \frac{(11.2 \times 10^3)^2 \times (2 \times 10^{-3})}{3 \times 8.31} = 10063\text{K}$

20 **(d)**

$$v = \sqrt{\frac{\gamma P}{\rho}} = \sqrt{\frac{\frac{5}{3} \times 10^3}{2.6}} = 25 \text{ m/s}$$

PE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	D	C	C	A	A	C	D	A	C	B
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	D	B	D	B	A	D	A	D	D

PE