

## Topic :- KINETIC THEORY

1 (d)

$$\frac{V_{rmsHe}}{V_{rmsAr}} = \frac{\sqrt{\frac{3RT}{m_{He}}}}{\sqrt{\frac{3RT}{m_{Ar}}}} = \sqrt{\frac{m_{Ar}}{m_{He}}} = \sqrt{\frac{40}{4}} = \sqrt{10} \approx 3.16$$

2 (c)

We know that  $C_p - C_v = \frac{R}{J}$

$$\Rightarrow J = \frac{R}{C_p - C_v}$$

$$C_p - C_v = 1.98 \frac{\text{cal}}{\text{g} \cdot \text{mol} \cdot \text{K}}$$

$$R = 8.32 \frac{\text{J}}{\text{g} \cdot \text{mol} \cdot \text{K}}$$

$$\therefore J = \frac{8.32}{1.98} = 4.20 \text{ J/cal}$$

3 (c)

S.I. unit of  $R$  is  $\text{J/mol} \cdot \text{K}$

4 (a)

According to Boyle's law  $PV = \text{constant}$

5 (a)

$$v_{rms} \propto \sqrt{\frac{3RT}{M}}$$

$$\Rightarrow T \propto v_{rms}^2$$

$$\Rightarrow \frac{T_2}{T_1} = \left[ \frac{v_2}{v_1} \right]^2 = \frac{1}{4} \Rightarrow T_2 = \frac{T_1}{4} = \frac{273 + 327}{4}$$

$$= 150 \text{ K} = -123^\circ\text{C}$$

6 (a)

The total pressure exerted by a mixture of non-reacting gases occupying a vessel

is equal to the sum of the individual pressure which each gas exert if it alone occupied the same volume at a given temperature.

For two gases,

$$p = p_1 + p_2 = p + p = 2p$$

7 **(b)**

According to ideal gas equation  $PV = nRT$

$$PV = \frac{m}{M}RT, P = \frac{\rho}{M}RT \text{ or } \frac{\rho}{P} = \frac{M}{RT} \text{ or } \frac{\rho}{P} \propto \frac{1}{T}$$

Here,  $\frac{\rho}{P}$  represent the slope of graph

Hence  $T_2 > T_1$

8 **(c)**

$$PV = \mu RT = \frac{m}{M}RT \Rightarrow P \propto mT$$

$$\Rightarrow \frac{P_2}{P_1} = \frac{m_2 T_2}{m_1 T_1} = \frac{1}{2} \times \frac{(273 + 27 + 50)}{(273 + 27)} = \frac{7}{12}$$

$$\Rightarrow P_2 = \frac{7}{12} P_1 = \frac{7}{12} \times 20 = 11.67 \text{ atm. } \approx 11.7 \text{ atm}$$

9 **(a)**

Since  $c_{rms} \ll V_e$ , hence molecules do not escape out

11 **(b)**

In case of given graph,  $V$  and  $T$  are related as  $V = aT - b$ , where  $a$  and  $b$  are constants.

From ideal gas equation,  $PV = \mu RT$

$$\text{We find } P = \frac{\mu RT}{aT - b} = \frac{\mu R}{a - b/T}$$

Since  $T_2 > T_1$ , therefore  $P_2 < P_1$

12 **(c)**

Gas equation for  $N$  molecules  $PV = NkT$

$$\Rightarrow N = \frac{PV}{kT} = \frac{1.2 \times 10^{-10} \times 13.6 \times 10^3 \times 10 \times 10^{-4}}{1.38 \times 10^{-23} \times 300}$$

$$= 3.86 \times 10^{11}$$

13 **(c)**

$$E \propto T$$

14 **(a)**

$$v_{rms} \propto \sqrt{T}, \frac{v_2}{v_1} = \sqrt{\frac{T_2}{T_1}} \Rightarrow v_2 = \sqrt{\frac{(273 + 927)}{(273 + 27)}} v_1 \Rightarrow v_2 = 2v_1$$

15 **(c)**

For ideal gas, on free expansion there is no change in temperature. Hence  $C_a = C_b$

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**(b)**

$$v_{rms} > v_{av} > v_{mp}$$

17

**(a)**

According to Boyle's law,  $pV = k$  (a constant)

$$\text{Or } p \frac{m}{\rho} = k \quad \text{or } p = \frac{pm}{k}$$

$$\text{Or } p = \frac{p}{k} \text{ (where, } \frac{k}{m} = k \text{ a constant)}$$

$$\text{So, } \rho_1 = \frac{p_1}{k} \text{ and } V_1 \frac{p_1}{k} = \frac{m_1}{\rho_1} = \frac{m_1}{p_1/k} = \frac{km_1}{\rho_1}$$

$$\text{Similarly, } V_2 = \frac{km_2}{\rho_2}$$

$$\text{Total volume} = V_1 + V_2 = k \left( \frac{m_1}{\rho_1} + \frac{m_2}{\rho_2} \right)$$

Let  $p$  be the common pressure and  $\rho$  be the common density of mixture. Then

$$\rho = \frac{m_1 + m_2}{V_1 + V_2} = \frac{m_1 + m_2}{k \left( \frac{m_1}{\rho_1} + \frac{m_2}{\rho_2} \right)}$$

$$\therefore p = k\rho = \frac{m_1 + m_2}{\frac{m_1}{\rho_1} + \frac{m_2}{\rho_2}} = \frac{P_1 P_2 (m_1 + m_2)}{(m_1 P_2 + m_2 P_1)}$$

18

**(c)**

$v_{rms} = \sqrt{\frac{3RT}{M}}$ . According to problem  $T$  will become  $2T$  and  $M$  will become  $M/2$  so the value of  $v_{rms}$  will increase by  $\sqrt{4} = 2$  times, i.e., new root mean square velocity will be  $2v$

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**(a)**

$$\text{Here, } \frac{K_1}{K_2} = \frac{1}{2} \frac{r_1}{r_2} = \frac{1}{2}$$

$$\therefore \frac{A_1}{A_2} = \frac{1}{4}$$

$$\frac{dx_1}{dx_2} = \frac{1}{2}, \frac{dQ_2}{dt} = 4 \text{ cal s}^{-1}, \frac{dQ_1}{dt} = ?$$

$$\frac{dQ_2/dt}{dQ_1/dt} = \frac{K_2 A_2 dT/dx_2}{K_1 A_1 dT/dx_1} = \frac{K_2 A_2 dx_1}{K_1 A_1 dx_2}$$

$$= 2 \times 4 \times \frac{1}{2} = 4$$

$$\frac{dQ_1}{dt} = \frac{dQ_2/dt}{4} = \frac{4}{4} = 1 \text{ cal s}^{-1}$$

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**(b)**

At lower pressure we can assume that given gas behaves as ideal gas so  $\frac{PV}{RT} = \text{constant}$  but when pressure increases, the decrease in volume will not take place in same proportion so  $\frac{PV}{RT}$  will increase

| ANSWER-KEY |    |    |    |    |    |    |    |    |    |    |
|------------|----|----|----|----|----|----|----|----|----|----|
| Q.         | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
| A.         | D  | C  | C  | A  | A  | A  | B  | C  | A  | C  |
|            |    |    |    |    |    |    |    |    |    |    |
| Q.         | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| A.         | B  | C  | C  | A  | C  | B  | A  | C  | A  | B  |
|            |    |    |    |    |    |    |    |    |    |    |

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