

**Topic :- KINETIC THEORY**

1 (d)

$$\gamma_{\text{mixture}} = \frac{\frac{\mu_1 \gamma_1}{\gamma_1 - 1} + \frac{\mu_2 \gamma_2}{\gamma_2 - 1}}{\frac{\mu_1}{\gamma_1 - 1} + \frac{\mu_2}{\gamma_2 - 1}}$$

$$\mu_1 = \text{moles of helium} = \frac{16}{4} = 4$$

$$\mu_2 = \text{moles of oxygen} = \frac{16}{32} = \frac{1}{2}$$

$$\Rightarrow \gamma_{\text{mix}} = \frac{\frac{4 \times 5/3}{5/3 - 1} + \frac{1/2 \times 7/5}{7/5 - 1}}{\frac{4}{5/3 - 1} + \frac{1/2}{7/5 - 1}} = 1.62$$

2 (a)

$$\text{Mean free path, } \lambda = \frac{1}{\sqrt{2} \pi d^2 n}$$

Where,  $n$  = Number of molecules per unit volume

$d$  = Diameter of the molecules

3 (b)

Speed of sound in gases is given by

$$v_{\text{sound}} = \sqrt{\frac{\gamma P}{\rho}} \Rightarrow \frac{v_1}{v_2} = \sqrt{\frac{\rho_2}{\rho_1}} = \sqrt{\frac{d_2}{d_1}}$$

4 (c)

$$n_1 C_{v1} \Delta T_1 = n_2 C_{v2} \Delta T_2$$

$$\Rightarrow n_1 \times \frac{3}{2} R \times 10 = n_2 \times \frac{5}{2} R \times 6 \Rightarrow \frac{n_1}{n_2} = 1$$

5 (a)

We treat water like a solid. For each atom average energy is  $3k_B T$ . Water molecule has three atoms, two hydrogen and one oxygen. The total energy of one mole of water is

$$U = 3 \times 3k_B T \times N_A = 9RT \quad \left[ \because k_B = \frac{R}{N_A} \right]$$

$\therefore$  Heat capacity per mole of water is

$$C = \frac{\Delta Q}{\Delta T} = \frac{\Delta U}{\Delta T} = 9R$$

6 (a)

K.E. is function of temperature. So  $\frac{E_{H_2}}{E_{O_2}} = \frac{1}{1}$

7 (c)

According to kinetic theory of gases the temperature of a gas is a measure of the kinetic energies of the molecules of the gas.

8 (c)

At constant volume

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} \Rightarrow T_2 = \left(\frac{P_2}{P_1}\right)T_1$$

$$\Rightarrow T_2 = \left(\frac{3P}{P}\right) \times (273 + 35) = 3 \times 308 = 924K = 651^\circ C$$

9 (d)

$$\frac{3}{2}kT = 1 \text{ eV} \Rightarrow T = \frac{2 \text{ eV}}{3 k} = \frac{\frac{2}{3} \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23}} = 7.7 \times 10^3 K$$

11 (b)

Vander Waal's gas equation for  $\mu$  mole of real gas

$$\left(P + \frac{\mu^2 a}{V^2}\right)(V - \mu b) = \mu RT$$

$$P = \left(\frac{\mu RT}{V - \mu b} - \frac{\mu^2 a}{V^2}\right)$$

Given equation,

$$P = \left(\frac{RT}{2V - b} - \frac{a}{4b^2}\right)$$

On comparing the given equation with this standard equation, we get

$$\mu = \frac{1}{2}$$

Hence,  $\mu = \frac{m}{M}$

$$\Rightarrow \text{mass of gas, } m = \mu M = \frac{1}{2} \times 44 = 22g$$

12 (d)

$$C_p = \left(\frac{f}{2} + 1\right)R = \left(\frac{5}{2} + 1\right)R = \frac{7}{2}R$$

13 (c)

$$\frac{R}{C_p} = \frac{R}{7/2R} = \frac{2}{7} \quad \left[ \because C_p = \frac{7}{2}R \right]$$

14 (c)

As temperature decreases to half and volume made twice, hence pressure becomes  $\frac{1}{4}$  times

15 (d)

$$\begin{aligned} p &= p_1 + p_2 + p_3 \\ &= \left(\frac{nRT}{V}\right)_{O_2} + \left(\frac{nRT}{V}\right)_{N_2} + \left(\frac{nRT}{V}\right)_{CO_2} \\ &= (n_{O_2} + n_{N_2} + n_{CO_2}) \frac{RT}{V} \\ &= \frac{(0.25 + 0.5 + 0.5)(8.31) \times 300}{4 \times 10^{-3}} \\ &= 7.79 \times 10^5 \text{ Nm}^{-2} \end{aligned}$$

16 (a)

$$\begin{aligned} PV &= \mu RT = \frac{m}{M} RT \Rightarrow V = \frac{mRT}{MP} \\ &= \frac{2 \times 10^{-3} \times 8.3 \times 300}{32 \times 10^{-3} \times 10^5} = 1.53 \times 10^{-3} \text{ m}^3 = 1.53 \text{ litre} \end{aligned}$$

17 (c)

According to Boyle's law  
 $(P_1 V_1)_{\text{At top of the lake}} = (P_2 V_2)_{\text{At the bottom of the lake}}$

$$\begin{aligned} \Rightarrow P_1 V_1 &= (P_1 + h) V_2 \Rightarrow 10 \times \frac{4}{3} \pi \left(\frac{5r}{4}\right)^3 \\ \Rightarrow (10 + h) \times \frac{4}{3} \pi r^3 &\Rightarrow h = \frac{610}{64} = 9.53 \text{ m} \end{aligned}$$

18 (d)

We have  $v_{\text{rms}} = \sqrt{\frac{3RT}{M}}$ ; at  $T = T_0$  (NTP)

$$v_{\text{rms}} = \sqrt{\frac{3RT_0}{M}}$$

But at temperature  $T$ ,

$$v_{\text{rms}} = 2 \times \sqrt{\frac{3RT_0}{M}}$$

$$\Rightarrow \sqrt{\frac{3RT}{M}} = 2 \sqrt{\frac{3RT_0}{M}}$$

$$\Rightarrow \sqrt{T} = \sqrt{4T_0}$$

$$\text{or } T = 4T_0$$

$$T = 4 \times 273\text{K} = 1092\text{K}$$

$$\therefore T = 819^{\circ}\text{C}$$

19 **(b)**

$$E = \frac{f}{2}RT; f = 5 \text{ for diatomic gas} \Rightarrow E = \frac{5}{2}RT$$

20 **(d)**

Average kinetic energy

$$E = \frac{3}{2}kT \Rightarrow \frac{E_1}{E_2} = \frac{T_1}{T_2} = \frac{(273 - 23)}{(273 + 227)} = \frac{250}{500} = \frac{1}{2}$$

$$\Rightarrow E_2 = 2E_1 = 2 \times 5 \times 10^{-14} = 10 \times 10^{-14} \text{ erg}$$

PE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	D	A	B	C	A	A	C	C	D	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	D	C	C	D	A	C	D	B	D

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