

DPP

DAILY PRACTICE PROBLEMS

Class : XIth
Date :

Solutions

SUBJECT : PHYSICS
DPP No. : 2

TOPIC :- GRAVITATION

1 (b)

For a moving satellite kinetic energy = $\frac{GMm}{2r}$

Potential energy = $\frac{-GMm}{r} \Rightarrow \therefore \frac{\text{Kinetic energy}}{\text{Potential energy}} = \frac{1}{2}$

2 (b)

$I = \frac{-dV}{dr}$. If $I = 0$ then $V = \text{constant}$

3 (b)

$$v = \sqrt{2gR} \Rightarrow \frac{v_A}{v_B} = \sqrt{\frac{g_A}{g_B} \times \frac{R_A}{R_B}} = \sqrt{k_1 \times k_2} = \sqrt{k_1 k_2}$$

4 (d)

Orbital radius of satellites $r_1 = R + R = 2R$
 $r_2 = R + 7R = 8R$

$$U_1 = -\frac{GMm}{r_1} \text{ and } U_2 = -\frac{GMm}{r_2}$$

$$K_1 = \frac{GMm}{2r_1} \text{ and } K_2 = \frac{GMm}{2r_2}$$

$$E_1 = \frac{GMm}{2r_1} \text{ and } E_2 = \frac{GMm}{2r_2}$$

$$\therefore \frac{U_1}{U_2} = \frac{K_1}{K_2} = \frac{E_1}{E_2} = 4$$

6 (c)

If no external torque acts on a system, then angular momentum of the system does not change.

ie, If $\tau = 0$

$$\Rightarrow \frac{dL}{dt} = 0$$

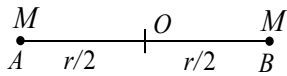
$\therefore L = \text{constant}$

Hence, $mv_{\max}r_{\min} = mv_{\min}r_{\max}$

$$\Rightarrow r_{\min} = \frac{v_{\min} \times r_{\max}}{v_{\max}}$$

$$= \frac{1 \times 10^3 \times 4 \times 10^4}{3 \times 10^4} = \frac{4}{3} \times 10^3 \text{ km}$$

7 (d)



Gravitational potential of A at O = $-\frac{GM}{r/2} = -\frac{2GM}{r}$

For B, potential at O = $-\frac{GM}{r/2} = -\frac{2GM}{r}$

\therefore Total potential = $-\frac{4GM}{r}$

8 (b)

Orbital radius of Jupiter > Orbital radius of Earth

$\frac{v_J}{v_e} = \frac{r_e}{r_J}$. As $r_J > r_e$ therefore $v_J < v_e$

9 (d)

% change in T = $\frac{3}{2}$ (% change in R) = $\frac{3}{2} \times (2)\% = 3\%$

11 (b)

From Kepler's third law of planetary motion

$$T^2 \propto R^3$$

Given, $T_1 = 1, T_2 = 8, R_1 = R$

$$\therefore \frac{T_1^2}{T_2^2} = \frac{R_1^3}{R_2^3}$$

$$R_2^3 = R_1^3 \frac{T_2^2}{T_1^2}$$

$$R_2^3 = R_1^3 \times (8)^2$$

$$R_2^3 = R^3 \times (2^3)^2$$

$$\Rightarrow R_2 = R \times 4 = 4R$$

12 (c)

$$g = \frac{4}{3} G \pi R \rho \Rightarrow \frac{g_1}{g_2} = \frac{\rho_1 R_1}{\rho_2 R_2} = \frac{1}{2} \times \frac{4}{1} = \frac{2}{1}$$

13 (b)

Gravitational acceleration is given by

$$g = \frac{GM}{R^2}$$

where G = gravitational constant

$$\therefore \frac{g}{G} = \frac{M}{R^2}$$

15 (c)

Let x be the distance of point from the smaller body where gravitational intensity is

zero.

$$\therefore \frac{Gm_1}{(1-x)^2} = \frac{Gm_2}{x^2}$$

$$\text{or } \frac{x}{1-x} = \sqrt{\frac{m_2}{m_1}} = \sqrt{\frac{1000}{100,000}} = \frac{1}{10}$$

$$\text{or } 10x = 1-x$$

$$\text{or } x = (1/11)m$$

17 **(b)**

From Kepler's third law of planetary motion:

$$T^2 \propto R^3$$

$$\text{Given, } T_p = 27T_e$$

$$\frac{T_e^2}{T_p^2} = \frac{R_e^3}{R_p^3}$$

$$\frac{T_e^2}{(27T_e)^2} = \frac{R_e^3}{R_p^3}$$

$$\frac{R_p}{R_e} = (27)^{1/2}$$

$$\frac{R_p}{R_e} = 3^2$$

$$R_p = 9R_e$$

18 **(a)**

$$g' = g \left(\frac{R}{R+h} \right)^2 = g \left(\frac{R}{R+\frac{R}{2}} \right)^2 = \frac{4}{9}g$$

$$\therefore W' = \frac{4}{9} \times W = \frac{4}{9} \times 72 = 32N$$

19 **(b)**

The acceleration due to gravity

$$g = \frac{GM}{R^2}$$

At a height h above the earth's surface, the acceleration due to gravity is

$$g' = \frac{GM}{(R+h)^2}$$

$$\therefore \frac{g}{g'} = \left(1 + \frac{h}{R}\right)^2 = \left(1 + \frac{h}{R}\right)^2$$

$$\frac{g'}{g} = \left(1 + \frac{h}{R}\right)^{-2} = \left(1 - \frac{2h}{R}\right)$$

$$\text{but } g' = \frac{g}{2} \quad (\text{given})$$

$$\therefore \frac{g/2}{g} = 1 - \frac{2h}{R}$$

$$\frac{2h}{R} = \frac{1}{2}$$

$$h = \frac{R}{4}$$

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(b)

Since, gravitation provides centripetal force

$$\frac{mv^2}{r} = \frac{k}{r^{5/2}} \text{ ie, } v^2 = \frac{k}{mr^{3/2}}$$

$$\text{So that } T = \frac{2\pi r}{v} = \sqrt{\frac{mr^{3/2}}{k}} \text{ ie, } T^2 = \frac{4\pi^2 m}{k} r^{7/2}$$

$$\therefore T^2 \propto r^{7/2}$$

PE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	B	B	B	D	A	C	D	B	D	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	C	B	C	C	A	B	A	B	B

PE