CLASS : XIth
DATE :

## Solutions

## Topic :- LAWS OF MOTION

1

2

3
(d)

Let the tension in the strings $A P_{2}$ and $P_{2} P_{1}$ beT. Considering the force on pulley $P_{1}$, we get $T=W_{1}$. Further, let $\angle A P_{1} P_{1}=2 \theta$
Resolving tensions in horizontal and vertical directions and considering the forces on pulley $P_{2}$, we get $2 T \cos \theta=W_{2}$
or $2 W_{1} \cos \theta=W_{2}$ or $\cos \theta=1 / 2$
or $\theta=60^{\circ}$ So $\angle A P_{2} P_{1}=2 \theta=120^{\circ}$
(c)

In equilibrium (figure)

$T=m \mathrm{~g}, N=3 \mathrm{mg}$ and $f=2 T=2 \mathrm{mg}$
In limiting case $f<f_{\text {max }}$
$2 m \mathrm{~g}<\mu N \Rightarrow 2 m \mathrm{~g} \leq 3 \mu \mathrm{mg} \Rightarrow \mu \geq \frac{2}{3}$
(d)

Time taken by the bullet and ball to strike the ground is
$t=\sqrt{\frac{2 h}{g}}=\sqrt{\frac{2 \times 5}{10}}=1 \mathrm{~s}$
Let $v_{1}$ and $v_{2}$ are the velocities of ball and bullet after collision. Then applying
$x=v t$
We have, $20=v_{1} \times 1$
or $v_{1}=20 \mathrm{~m} / \mathrm{s}$
$100=v_{2} \times 1$ or $v_{2}=100 \mathrm{~m} / \mathrm{s}$
Now, from conservation of linear momentum before and after collision we have,
$0.01 v=(0.2 \times 20)+(0.01 \times 100)$
On solving, we get
$v=500 \mathrm{~m} / \mathrm{s}$
(b)

Before cutting the string, the tension in string joining $m_{4}$ and the ground is $T=$ ( $\left.m_{1}+m_{2}-m_{3}-m_{4}\right) \mathrm{g}$ and the spring force in the spring joining $m_{3}$ and $m_{4}$ is $T+m_{4} \mathrm{~g}$. As the string is cut, the spring forces do not change instantly, so just after cutting the string the equilibrium of $m_{1}, m_{2}$ and $m_{3}$ would be maintained but $m_{4}$ accelerates in upward direction with acceleration given by
$a=\frac{T+m_{4} \mathrm{~g}-m_{4} \mathrm{~g}}{m_{4}}$
(d)

Condition of sliding is
$m g \sin \theta>\mu m g \cos \theta$
or $\tan \theta>\mu$
$\operatorname{ortan} \theta>\sqrt{3} \ldots$ (i)
condition of toppling is


Torque of $m g \sin \theta$ about $O>$ torque of $m g \cos \theta$ about.
$\therefore \quad(m g \sin \theta)\left(\frac{15}{2}\right)>(m g \cos \theta)\left(\frac{10}{2}\right)$
or $\tan \theta>\frac{2}{3}$
With increase in value of $\theta$, condition of sliding is satisfied first.

6 (c)
Friction between 2 kg and 8 kg blocks is kinetic in nature, so
$F=m \times 2 \mathrm{~g}=0.3 \times 2 \times 10=6 \mathrm{~N}$


For 2 kg block, $10-6=2 a_{1}$
For 8 kg block, $6=8 a_{2}$
$\Rightarrow a_{1}=2 \mathrm{~ms}^{-2}, a_{2}=\frac{3}{4} \mathrm{~ms}^{-2}$
Acceleration of 2 kg block relative to 8 kg block is
$a_{\text {ref }}=a_{1}-a_{2}=\frac{5}{4} \mathrm{~ms}^{-2}$
Using the equation of motion, $3=\frac{1}{2} \times \frac{5}{4} r^{2}$
$t=2.19 \mathrm{~s}$
(c)

From 0 to 2 s: at any time $t, F=10 t$
$\Rightarrow a=F / m=10 t / m$
$\Rightarrow \int_{0}^{v} d v=\int_{0}^{t} \frac{10 t}{m} d t \Rightarrow v=\frac{5 t^{2}}{m}$
Momentum: $P=m v=5 t^{2}$
At $t=2 \mathrm{~s}, P=5(2)^{2}=20 \mathrm{~kg} \mathrm{~ms}^{-1}, v=20 / m$
From 2 to $4 \mathrm{~s} ; F=40-10 t$
$\int_{20 / m}^{v} d v=\int_{2}^{t} \frac{40-10 t}{m} d t \Rightarrow v=\frac{1}{m}\left[40 t-40-5 t^{2}\right]$
$P=m v=40 t-40-5 t^{2}$
(a)
$V_{\max }=\sqrt{\frac{R g(\tan \theta-\mu)}{1-\mu \tan \theta}}$
(a)

Initially under equilibrium of mass $m$
$T=m g$
Now, the string is cut. Therefore, $T=m g$ force is decreased on mass $m$ upward and downwards on mass $2 m$.
$\therefore a_{m}=\frac{m g}{m}=g$ (downwards)
and $a_{2 m}=\frac{m g}{2 m}=\frac{g}{2}$ (upwards)
(b)

For the equilibrium of block of mass $M_{1}$ :
Frictional force, $f=$ tension in the string, $T$
Where $T=f=\mu\left(m+M_{1}\right) \mathrm{g}$ (i)
For the equilibrium of block of mass $M_{2}$ :
$T=M_{2} \mathrm{~g}$
Form (i) and (ii), we get $\mu\left(m+M_{1}\right) g=M_{2} g$
$m=\frac{M_{2}}{\mu}-M_{1}$
(d)

If the blocks move together,
$a=\frac{F}{m_{A}+m_{B}}=\frac{10}{6}=\frac{5}{3} \mathrm{~ms}^{-1}$
$f_{B}($ frictional force on $B)=m_{B} a=\frac{m_{B} F}{m_{A}+m_{B}}=\frac{20}{3} \mathrm{~N}$
$f_{B \max }=\mu m_{A} \mathrm{~g}=0.4 \times 2 \times 10=8 \mathrm{~N}$
As $f_{B \max }>f_{B}$, the blocks will not be separated and move together with common acceleration $5 / 3 \mathrm{~ms}^{-2}$
(c)

As sand particles are sliding down, the slope of the hill gets reduced. The sand particle stops coming down when component of gravity force alone hill is balanced by limiting friction force
$m g \sin \theta=\mu_{s} m g \cos \theta$
$\Rightarrow \theta=\tan ^{-1}\left(\mu_{s}\right) \cong 37^{\circ}$ where $\theta$ is the new slope angle of hill
(d)

In the free-body diagram of $B$ (figure (a))

(a)

(b)
$N=m_{B} a$
$f=m_{B} \mathrm{~g}$
$\mu N=m_{B} \mathrm{~g}$
Form (i) and (ii), $a=\frac{\mathrm{g}}{\mu}=20 \mathrm{~ms}^{-2}$
FBD of bob:
$T \sin \theta=m a \quad$ (iii)
$T \cos \theta=m g \quad$ (iv)
From (iii) and (iv)
$\tan \theta=\frac{a}{\mathrm{~g}} \Rightarrow \theta=\tan ^{-1}(2)$
(c)

Let $a$ be the common acceleration of the system
Here $T=M a$ (for block)
$P-T=M a \quad$ (for rope)

$P-M a=m a$
or $P=(m+M) a$ or $a=P /(m+M)$
now $T=M a=\frac{M P}{M+m}$
(d)

Maximum acceleration of $B$ or $C$ can be mg so that they do not slip with each other or on $A$
For the system of $(A+B+C)$
$T=3 \mathrm{ma}=3 \mu \mathrm{mg}$
For $D$ :
$M g-T=M a$
$\Rightarrow M \mathrm{~g}-3 \mu \mathrm{mg}=M \mu \mathrm{~g} \Rightarrow M=\frac{3 \mu \mathrm{~m}}{1-\mu}$
(a)
$v_{2} \cos \alpha+v_{1} \cos \alpha=v_{1} \Rightarrow v_{2}=v_{1}\left[\frac{2 \sin ^{2}(\alpha / 2)}{\cos \alpha}\right]$
(b)

The cloth can be pulled out without dislodging the dishes from the table due to law of inertia, which is Newton's first law. While, the statement II is true, but it is Newton's third law.
(b)

Velocity of liquid through inclined limbs $=\frac{v}{2}$
Rate of change of momentum of the liquid is
$\rho A v^{2}+2\left[\rho A\left(\frac{v}{2}\right)^{2} \cos 60^{\circ}\right]=\frac{5}{4} \rho A v^{2}$
(c)

As the eraser is at rest w.r.t. board, friction between two is static in nature
For figure (a) and (b), the friction force is same as that of gravity force as shown in figure


For (c), $f=F_{2}+M \mathrm{~g}>M \mathrm{~g}$

For (d) $M \mathrm{~g}-F_{2}<M \mathrm{~g}$ as angle by which arm is tilted is very small, so $F_{2}$ would be small

| ANSWER-KEY |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Q. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |  |
| A. | D | C | D | B | D | C | C | A | A | B |  |
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| Q. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |  |
| A. | D | C | B | D | C | D | A | B | B | C |  |
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