

Topic :- ELECTROSTATIC POTENTIAL AND CAPACITANCE

1 (a)

Since the two spheres are joined by a wire, their potential are equal ie,

$$\frac{q_1}{4\pi\epsilon_0 R_1} = \frac{q_2}{4\pi\epsilon_0 R_2} \Rightarrow \frac{q_1}{q_2} = \frac{R_1}{R_2}$$

$$\text{Now, } \sigma_1 = \frac{q_1}{4\pi\epsilon_0 R_1^2}$$

$$\text{And } \sigma_2 = \frac{q_2}{4\pi\epsilon_0 R_2^2},$$

$$\text{Hence } \frac{\sigma_2}{\sigma_1} = \frac{\sigma_2}{\sigma_1} \times \frac{R_1^2}{R_2^2} = \left(\frac{R_2}{R_1}\right) \left(\frac{R_1}{R_2}\right)^2$$

$$\Rightarrow \frac{\sigma_2}{\sigma_1} = \frac{R_1}{R_2}$$

2 (d)

(n-1) capacitors are made by n plates and all are connected in parallel because plates are connected alternately.

$$\therefore \text{ Total capacitance} = (n - 1)x$$

3 (c)

The capacitance of air capacitor

$$C = \frac{\epsilon_0 A}{d}$$

When a dielectric slab of thickness $t = \frac{d}{2}$ is inserted between plates, the capacity becomes

$$C' = \frac{A\epsilon_0}{d - \frac{d}{2}\left(1 - \frac{1}{K}\right)}$$

$$\frac{4}{3} \frac{A\epsilon_0}{d} = \frac{\epsilon_0 A}{d - \frac{d}{2}\left(1 - \frac{1}{K}\right)}$$

$$3d = 4d\left(1 - \frac{1}{2} + \frac{1}{2K}\right)$$

$$3 = 4\left(\frac{1}{2} + \frac{1}{2K}\right)$$

$$\text{or } \frac{4}{2K} = 3 - 2$$

$$\text{or } K = 2$$

4

(a)

$$r_b - r_a = 1\text{mm} = 10^{-3}\text{m}$$

$$\text{From } C = \frac{4\pi\epsilon_0 r_a r_b}{r_b - r_a}$$

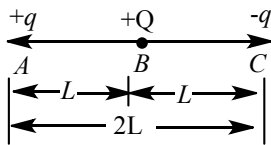
$$10^{-6} = \frac{1(r_b - 10^{-3})r_b}{9 \times 10^9(10^{-3})}$$

$$r_b^2 = 9, r_b = 3\text{m}$$

5

(d)

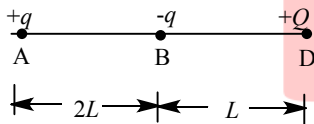
In Ist case, when charge $+Q$ is situated at C.



Electric potential energy of system

$$U_1 = \frac{1}{4\pi\epsilon_0} \frac{(q)(-q)}{2L} + \frac{1}{4\pi\epsilon_0} \frac{(-q)Q}{L} + \frac{1}{4\pi\epsilon_0} \frac{qQ}{L}$$

In IInd case, when charge $+Q$ is moved from C to D.



Electric potential energy of system in that case

$$U_2 = \frac{1}{4\pi\epsilon_0} \frac{(q)(-q)}{2L} + \frac{1}{4\pi\epsilon_0} \frac{qQ}{3L} + \frac{1}{4\pi\epsilon_0} \frac{(-q)(Q)}{L}$$

$$\therefore \text{Work done} = \Delta U = U_2 - U_1$$

$$= \left(\frac{1}{4\pi\epsilon_0} \frac{q^2}{2L} + \frac{1}{4\pi\epsilon_0} \frac{qQ}{3L} - \frac{1}{4\pi\epsilon_0} \frac{qQ}{L} \right)$$

$$- \left(\frac{1}{4\pi\epsilon_0} \frac{q^2}{2L} + \frac{1}{4\pi\epsilon_0} \frac{qQ}{L} + \frac{1}{4\pi\epsilon_0} \frac{qQ}{L} \right)$$

$$= \frac{qQ}{4\pi\epsilon_0} \left[\frac{1}{3L} - \frac{1}{L} \right]$$

$$= \frac{qQ}{4\pi\epsilon_0} \frac{(1-3)}{3L}$$

$$= \frac{-2qQ}{12\pi\epsilon_0 L} = -\frac{qQ}{6\pi\epsilon_0 L}$$

6 (c)

$$C_0 = \frac{\epsilon_0 A}{d} = 18$$

$$C_0 = \frac{K\epsilon_0 A}{3d} = 72$$

Dividing Eq. (ii) by Eq. (i)

$$\frac{k}{3} = \frac{72}{18} = 4$$

$$K = 12$$

7 (d)

$$\frac{1}{C_s} = \frac{1}{1} + \frac{1}{1} + \frac{1}{1} = 3$$

$$C_s = \frac{1}{3}$$

Capacitance between *A* and *B*

$$C_p = \frac{1}{3} + 1$$

$$\frac{4}{3} \mu\text{F} = 1.33 \mu\text{F}$$

9 (c)

Here,

$$\vec{E} = \vec{E}_1 + \vec{E}_2 + \vec{E}_3 = \left(+\frac{\sigma}{2\epsilon_0} \right) (-\hat{k}) + \left(\frac{2\sigma}{2\epsilon_0} \right) (-\hat{k}) + \left(\frac{\sigma}{2\epsilon_0} \right) (-\hat{k})$$

$$= -\left(\frac{2\sigma}{\epsilon_0} \right) \hat{k}$$

10 (a)

$$V = \frac{\sum q}{4\pi\epsilon_0 r} = \frac{-10 + 10}{4\pi\epsilon_0 r} = 0$$

11 (b)

Linear momentum of electron, $p_e = \sqrt{2m_e eV}$

Linear momentum of photon, $p_p = \sqrt{2m_p eV}$

$$\frac{p_e}{p_p} = \frac{\sqrt{2m_e eV}}{\sqrt{2m_p eV}}$$

$$\frac{p_e}{p_p} = \sqrt{\frac{m_e}{m_p}}$$

12 (a)

Number of capacitors to be connected in series

$$V = \frac{\text{voltage rating required}}{\text{voltage rating of given capacitor}} = \frac{700}{200} = 3.5 \text{ie, } 4$$

$$C_{\text{eq}} = \frac{10}{4} = 2.5 \mu\text{F}$$

Number of rows required

$$= \frac{\text{capacitor required}}{\text{capacity of each row}} = \frac{10}{2.5} = 4$$

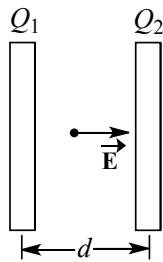
$$\therefore \text{total number of capacitors required} = 4 \times 4 = 16$$

14 (a)

Net capacity of 5 capacitors joined in parallel = $5 \times 2 = 10 \mu\text{F}$. now it is connected with two capacitors of $2 \mu\text{F}$ each in series, hence equivalent capacitance is $\frac{10}{11} \mu\text{F}$.

15 (d)

On bringing the charged metal plates closer, electric field \vec{E} in the intervening space is



$$E = \frac{\sigma_1}{2\epsilon_0} - \frac{\sigma_2}{2\epsilon_0} = \frac{\sigma_1}{2A\epsilon_0} - \frac{\sigma_2}{2A\epsilon_0}$$

$$\text{Or } E = \frac{Q_1 - Q_2}{2A\epsilon_0} = \frac{V}{d} \text{ or } V = \frac{(Q_1 - Q_2)d}{2A\epsilon_0}$$

$$\Rightarrow V = \frac{Q_1 - Q_2}{2C} \quad \left(\because C = \frac{\epsilon_0 A}{d} \right)$$

16 (c)

Potential energy

$$U = \frac{q_1 q_2}{4\pi\epsilon_0 r}$$

$$\text{Or } U \propto \frac{1}{r}$$

When r decreases U increases and *vice – versa*. Moreover, potential energy as well as force is positive, if there is repulsion between the particles and negative if there is attraction.

17 (b)

Work done = potential energy of configuration of charges

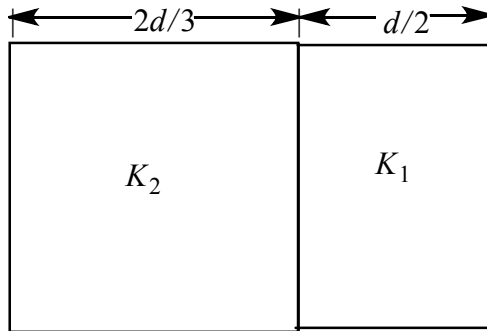
$$\frac{1}{4\pi\epsilon_0 a} [q(-q) + (9-q)q + q(-q) + (-q)(q)] + \frac{(-q)(-q) + q^2}{4\pi\epsilon_0 a\sqrt{2}}$$

$$= \frac{1}{4\pi\epsilon_0} \left[-\frac{4q^2}{a} + \frac{2q^2}{a\sqrt{2}} \right] = -\frac{2.6 q^2}{4\pi\epsilon_0 a}$$

18

(c)

$$C = \frac{C_1 C_2}{C_1 + C_2} \quad \dots(i)$$



$$\text{where } C_1 = \frac{K_1 \epsilon_0 A}{d/3} \quad \dots(ii)$$

$$\text{And } C_2 = \frac{K_2 \epsilon_0 A}{2d/3} \quad \dots(iii)$$

$$\text{It is given that } \frac{\epsilon_0 A}{d} = 9 \mu\text{F}$$

On substituting Eqs. (ii) and (iii) in Eq. (i), we get the result

$$C_{\text{eq}} = 40.5 \mu\text{F}$$

19

(b)

$$C = \frac{A\epsilon_0}{d}$$

After inserting the slab

$$C' = \frac{A\epsilon_0}{(d-b)} = \frac{A\epsilon_0}{d - \frac{d}{2}}$$

$$C' = \frac{2A\epsilon_0}{d} \quad \therefore \frac{C'}{C} = \frac{2}{1}$$

20

(d)

Net electric flux of surface

$$(\phi_2 - \phi_1) = \frac{1}{\epsilon_0} (q) \Rightarrow q = \epsilon_0 (\phi_2 - \phi_1)$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	D	C	A	D	C	D	C	C	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	A	B	A	D	C	B	C	B	D

PE