

Topic :- ELECTROSTATIC POTENTIAL AND CAPACITANCE

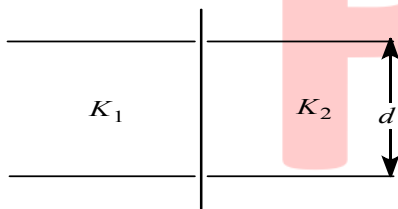
1 (a)

Potential gradient relates with electric field according to the relation, $E = -\frac{dV}{dr}$

$$= -\frac{10}{20 \times 10^{-2}} = 50 \text{ Vm}^{-1}$$

2 (b)

Initially, the capacitance of capacitor



$$C = \frac{\epsilon_0 A}{d}$$

$$\therefore \frac{\epsilon_0 A}{d} = 1 \mu\text{F} \quad \dots(i)$$

When it is filled with dielectric of dielectric constant K_1 and K_2 as shown, then there are two capacitors connected in parallel. So,

$$C' = \frac{K_1 \epsilon_0 (\frac{A}{2})}{d} + \frac{K_2 \epsilon_0 (\frac{A}{2})}{d}$$

(as area becomes half)

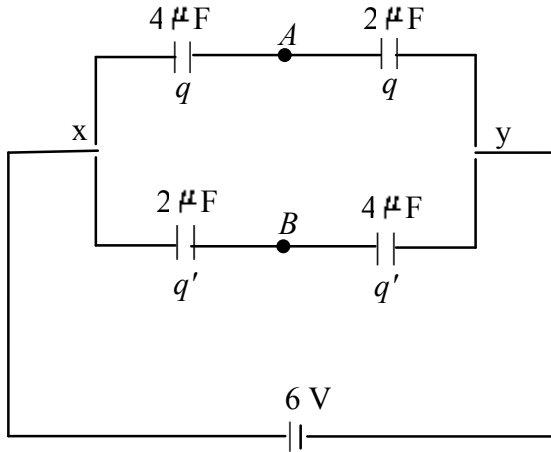
$$C' = \frac{4\epsilon_0 A}{2d} + \frac{6\epsilon_0 A}{2d} = \frac{2\epsilon_0 A}{d} + \frac{3\epsilon_0 A}{d}$$

Using Eq. (i), we obtain

$$C' = 2 \times 1 + 3 \times 1 = 5 \mu\text{F}$$

3 (a)

Consider the charge distribution as shown. Considering the branch on upper side, we have



$$\frac{q}{V_x - V_A} = 4 \times 10^{-6}$$

$$\frac{q}{V_A - V_y} = 2 \times 10^{-6}$$

Here, $V_x = 6$ volt, $V_y = 0$

$$\therefore \frac{q}{6 - V_A} = 4 \times 10^{-6} \quad \dots(i)$$

$$\frac{q}{V_A - 0} = 2 \times 10^{-6} \quad \dots(ii)$$

From Eqs. (i) and (ii), we get

$$\frac{V_A}{6 - V_A} = 2$$

$$\therefore V_A = 4 \text{ volt}$$

Similarly for the lower side branch

$$\frac{q'}{6 - V_B} = 2 \times 10^{-6} \quad \dots(iii)$$

$$\frac{q'}{V_B - 0} = 4 \times 10^{-6} \quad \dots(iv)$$

From Eqs. (iii) and (iv)

$$\frac{V_B}{6 - V_B} = \frac{1}{2}$$

$$\therefore V_B = 2 \text{ volt}$$

$$\therefore V_A - V_B = 4 - 2 = 2 \text{ volt}$$

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(a)

The system will be equivalent to series combination of two capacitors of half thickness *ie.*, each of capacity $2C$

$$\therefore \frac{1}{C_s} = \frac{1}{2c} + \frac{1}{2c} = \frac{1}{c} \text{ or } C_s = c$$

\therefore capacity remains the same

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(b)

In parallel, potential is same, say V

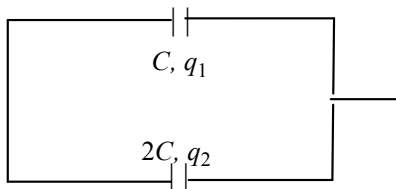
$$\frac{Q_1}{Q_2} = \frac{C_1 V}{C_2 V} = \frac{C_1}{C_2}$$

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(c)The charge $q_1 = CV_0$

or

$$V_0 = \frac{q_1}{C} \quad \dots(i)$$



∴

Capacitors are in parallel, in parallel V_0 is same for all capacitors.

$$\therefore \text{For second capacitor } V_0 = \frac{q_2}{2C} \quad \dots(ii)$$

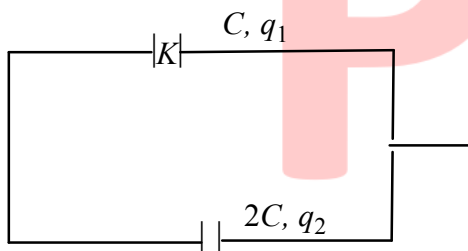
From Eqs. (i) and (ii),

$$q_2 = 2q_1 \quad \dots(iii)$$

After disconnecting the battery, the region between the plates of the capacitor C is completely filled with a material of dielectric constant ($K = 2$).

$$\text{Then, } V_1 = \frac{q_1}{CK} = \frac{q_1}{2C}$$

$$\text{and } V_1 = \frac{q_2}{2C} = \frac{2q_1}{2C} = \frac{q_1}{C} \quad [\text{from Eq. (iii)}]$$



Charge will flow from 2 to 1 till

$$\frac{q'_2}{2C} = \frac{q'_1}{KC}$$

$$\frac{q'_2}{2C} = \frac{q'_1}{2C}$$

$$\text{ie, } q'_1 = q'_2$$

$$\text{Earlier potential } V_0 = \frac{q_1}{C}$$

$$\text{Now it is } V_0 = \frac{q'_1}{2C}$$

$$\text{Now, } q_1 + q_2 = 3q_1 \quad [\text{from Eq.(iii)}]$$

$$\text{and } q'_1 + q'_2 = 3q_1$$

$$\text{or } 2q'_1 = 3q_1 \text{ or } q'_1 = \frac{3q_1}{2}$$

$$\therefore \text{ Now potential } \frac{q'_1}{2C} = \frac{3q_1}{4C}$$

$$V = \frac{3V_0}{4}$$

$$[\because q_1 = V_0 C]$$

8 **(c)**
Electric flux may be due to the charges present inside the Gaussian surface, but for the purpose of calculation of electric field E at any point we shall have to consider contribution of all the charges.

9 **(d)**
Frequency $n = 50\text{Hz}$
Time period $T = \frac{1}{50}\text{ s}$
Time taken for voltage to change from its peak value to zero
 $= \frac{T}{4} = \frac{1}{4 \times 50} = \frac{1}{200} = 5 \times 10^{-3}\text{s}$

10 **(d)**
 $E = \left(\frac{1}{2}\right)CV^2 \quad \dots(i)$
The energy stored in capacitor is lost in form of heat energy
 $H = ms \Delta T \dots(ii)$
From Eqs. (i) and (ii), we have
 $ms \Delta T = \left(\frac{1}{2}\right)CV^2$
 $V = \sqrt{\frac{2ms\Delta T}{C}}$

11 **(b)**
As the electrostatic force are conservative, work done is independent of path .
 $W = \vec{F} \cdot \vec{ds} = q E \hat{i} \cdot [(0 - a)\hat{i} + (0 - b)\hat{j}]$
 $= -q E a$

12 **(d)**
 $E_1 = \frac{1}{2}C_1V^2$
 $= \frac{1}{2} \times 2 \times 10^{-6} \times 100^2 = 0.01\text{J}$
 $E_1 = \frac{1}{2}C_2V^2$
 $\frac{1}{2} \times 10 \times 10^{-6} \times (100)^2 = 0.05\text{ J}$
Energy change $= E_2 - E_1$
 $= 0.05 - 0.01 = 0.04\text{J} = 4 \times 10^{-2}\text{J}$

13 **(a)**
Potential energy of electric dipole, $U = -\vec{p} \cdot \vec{E} = -pE \cos \theta$.

In Fig. (a), $\theta = \pi$ rad hence $U = -pE \cos \pi = +pE = \text{maximum}$.

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(a)

$$C_s = \frac{10 \times 20}{10 + 20} = \frac{200}{30} = \frac{20}{3} \mu\text{F}$$

$$Q = C_s V$$

$$Q = \frac{20}{3} \mu\text{F} \times 200\text{V}$$

$$Q = \frac{4000}{3} \mu\text{C}$$

$$\text{Now, } V = \frac{4000 \mu\text{C}}{3 \times 30 \mu\text{F}} = \frac{4000}{90} \text{V} = \frac{400}{9} \text{V}$$

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(b)

Electrostatic potential energy of system of two electrons

$$U = \frac{1}{4\pi\epsilon_0} \frac{(-e)(-e)}{r} = \frac{1}{4\pi\epsilon_0} \frac{e^2}{r}$$

Thus, as r decreases, potential energy U increases.

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(b)

Electrical pressure (force/area)

$$\Rightarrow p = \frac{1}{2} \epsilon_0 E^2 \text{ and } E = \frac{V}{r} \therefore p = \frac{1}{2} \epsilon_0 \frac{V^2}{r^2}$$

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(a)

Bob will experience an additional force $F = qE$ in vertically upward direction and hence effective acceleration due to gravity is reduced from g to $(g - a) = \left(g - \frac{qE}{m}\right)$.

Consequently, time period of oscillation will become $T = 2\pi \sqrt{\frac{l}{(g - a)}}$ ie, time period will increase.

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(d)

The three capacitors are in parallel hence, their equivalent capacitance = $3C$

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(c)

Electric potential inside the hollow conducting sphere is constant and equal to potential at the surface of the sphere = $\frac{Q}{4\pi\epsilon_0 R}$.

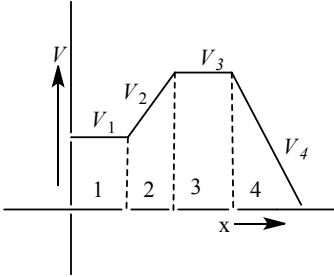
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(b)

Electric field

$$E = -\frac{dV}{dx}$$

For I region, $V_1 = \text{constant}$



$$\therefore \frac{dV_1}{dx} = 0$$

$$\therefore E_1 = 0$$

For II region,

$$V_2 = +ve = +f(x)$$

$$\therefore E_2 = -\frac{dV_2}{dx} = -ve$$

For III region.

$$V_3 = \text{constant}$$

$$\therefore \frac{dV_3}{dx} = 0$$

$$\therefore E_3 = 0$$

For IV region, $V_4 = -f(x)$

$$\therefore E_4 = -\frac{dV_4}{dx} = +ve$$

From these values, we have

$$E_2 > E_4 > E_1 = E_3$$

PE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	B	A	A	D	B	C	C	D	D
Q.	11	12	13	14	15	16	17	18	19	20
A.	B	D	A	A	B	B	A	D	C	B

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