

## Topic :- ELECTROSTATIC POTENTIAL AND CAPACITANCE

1 (b)

Capacitance of two capacitors each of area  $\frac{A}{2}$ , plate separation  $d$  but dielectric constants  $K_1$  and  $K_2$  respectively joined in parallel

$$C_1 = \frac{K_1 \epsilon_0 \left(\frac{A}{2}\right)}{d/2} + \frac{K_2 \epsilon_0 \left(\frac{A}{2}\right)}{d/2} = \frac{(K_1 + K_2) \epsilon_0 A}{d}$$

It is in series with a capacitor of plate area  $A$ , plate separation  $d/2$  and dielectric constant  $K_3$  i.e.,  $C_2 = \frac{K_3 \epsilon_0 A}{d/2}$ .

If resultant capacitance be taken as  $C = \frac{K \epsilon_0 A}{d}$ ,

$$\text{Then } \frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\therefore \frac{d}{K \epsilon_0 A} = \frac{d}{(K_1 + K_2) \epsilon_0 A} + \frac{d/2}{K_3 \epsilon_0 A}$$

$$\Rightarrow \frac{1}{K} = \frac{1}{K_1 + K_2} + \frac{1}{2K_3}$$

2 (b)

For a charged sphere or shell of charge potential

$$V_s = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r}$$

Hence, charge on both the spheres will be equal.

3 (b)

Potential at the centre of hollow metallic sphere

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{R}$$

- 4 **(a)**  
Potential difference between two points in a electric fields is,

$$V_A - V_B = \frac{W}{q_0}$$

Where  $W$  is work done by moving charge  $q_0$  from point  $A$  to  $B$ .

So,

$$V_A - V_B = \frac{2}{20}$$

(Here  $W = 2, q_0 = 20C$ ) = 0.1V

- 5 **(d)**  
 $C_p = 1 + 1 + 1 = 3\mu F$

$$\frac{1}{C_s} = \frac{1}{3} + \frac{1}{1} = \frac{4}{3}$$

$$\therefore C_s = \frac{3}{4}\mu F$$

- 6 **(a)**  
 $\phi_E = \frac{q}{K\epsilon_0} = \frac{0.5}{10 \times 8.85 \times 10^{12}} = 5.65 \times 10^9$

- 7 **(b)**  
Common potential of system

$$V = \frac{C_1V_1 + C_2V_2}{C_1 + C_2}$$

$$40 = \frac{10 \times 100 + C_2 \times 0}{10 + C_2}$$

$$\text{or } 40(10 + C_2) = 1000$$

$$\Rightarrow C_2 = 15 \mu F$$

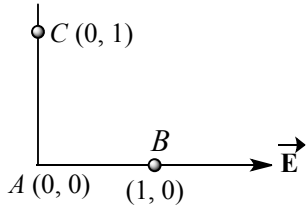
- 8 **(d)**  
Variation of different variables ( $Q, C, V, E$  and  $U$ ) of parallel plate capacitor when dielectric ( $K$ ) is introduced when battery is removed is

$$C' = KC E' = E / K$$

$$Q' = QU' = U / K$$

$$V' = V / K$$

- 9 **(b)**  
As electric field is along positive  $x$ -axis and  $E = -\frac{dV}{dx}$ , hence potential at  $A$  must be greater than that at  $B$  ie,  $V_A > V_B$



10.

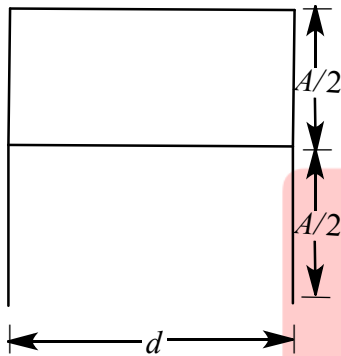
(c)

$$\begin{aligned} \text{Energy given to conductor} &= \frac{1}{2}CV^2 \\ &= \frac{1}{2} \times 5 \times 10^{-6} \times (800)^2 \\ &= 1.6 \text{ J} \end{aligned}$$

11.

(c)

The dielectric is introduced such that, half of its area is occupied by it.



In the given case the two capacitors are in parallel.

$$\therefore C' = C_1 + C_2$$

$$C_1 = \frac{A\epsilon_0}{2d}$$

And

$$C_2 = \frac{KA\epsilon_0}{2d}$$

Thus,

$$C' = \frac{A\epsilon_0}{2d} + \frac{KA\epsilon_0}{2d}$$

$$C' = \frac{C}{2}(1 + K)$$

12.

(a)

The material suitable for use as dielectric must have high dielectric strength  $X$  and large dielectric constant  $K$ .

13.

(a)

The energy stored is given by

$$E = \frac{1}{2}CV^2$$

When capacitors are connected in parallel, resultant capacitance is

$$C' = C_1 + C_2$$

$$= 2\mu\text{F} + 2\mu\text{F} = 4\mu\text{F}$$

$$V = 100 \text{ volt}$$

$$\therefore = \frac{1}{2} \times 4 \times 10^{-6} \times (100)^2$$

$$E = 0.02 \text{ J}$$

14.

**(d)**

With  $S_1$  and  $S_3$  closed, the capacitors  $C_1$  and  $C_2$  are in series arrangement. In series arrangement potential difference developed across capacitors are in the inverse ratio of their capacities. Hence,

$$\frac{V_1}{V_2} = \frac{C_2}{C_1} = \frac{3\mu\text{F}}{2\mu\text{F}} = \frac{3}{2} \text{ and}$$

$$V_1 + V_2 = V_1 + V_2 = 30 + 20 = 50 \text{ V}$$

On simplification, we get  $V_1 = 30 \text{ V}$  and  $V_2 = 20 \text{ V}$

15.

**(b)**

$$E = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\lambda = 2\pi\epsilon_0 r E$$

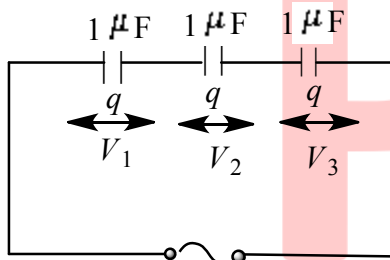
$$= \frac{1}{2 \times 9 \times 10^9} \times 2 \times 10^{-2} \times 9 \times 10^4$$

$$= 10^{-7} \text{ Cm}^{-1}$$

16.

**(d)**

Let potential difference between the plates of the capacitors  $C_1, C_2$  and  $C_3$  be  $V_1, V_2$  and  $V_3$  and  $q$  be the charge.



$$V = 11 \text{ volt}$$

$$\text{Then, } V = \frac{q}{C_1}, V_2 = \frac{q}{C_2}, V_3 = \frac{q}{C_3}$$

The total potential difference  $V = 11 \text{ volt}$

$$\therefore V = V_1 + V_2 + V_3$$

$$\Rightarrow V = \frac{q}{C_1} + \frac{q}{C_2} + \frac{q}{C_3} = 11$$

Given,  $C_1 = 1\mu\text{F}, C_2 = 2\mu\text{F}, C_3 = 3\mu\text{F}$

$$\therefore 11 = q\left(\frac{1}{1} + \frac{1}{2} + \frac{1}{3}\right)$$

$$\Rightarrow 11 = \frac{11q}{6}$$

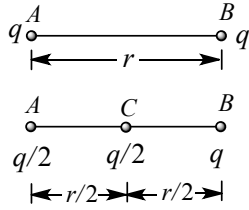
$$\Rightarrow q = 6\mu\text{C}$$

$$\therefore V_1 = \frac{q}{C_1} = \frac{6}{1} = 6 \text{ V}$$

17.

**(b)**

$$\text{Initially, } F_{AB} = \frac{1}{4\pi\epsilon_0} \frac{q \cdot q}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q^2}{r^2}$$



Finally, force on

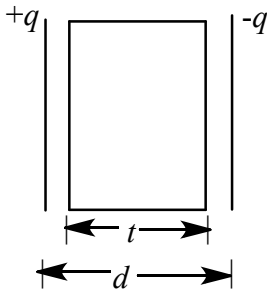
$$F_C = F_{AB} - F_{CA} = \frac{1}{4\pi\epsilon_0} \cdot \frac{\left(\frac{q}{2}\right)(q)}{\left(\frac{r}{2}\right)^2} - \frac{1}{4\pi\epsilon_0} \cdot \frac{\left(\frac{q}{2}\right)\left(\frac{q}{2}\right)}{\left(\frac{r}{2}\right)^2} = \frac{1}{4\pi\epsilon_0} \cdot \frac{q^2}{r^2}$$

$$\Rightarrow F_C = F_{AB}$$

18.

(b)

The capacitance  $C$  of a capacitor of area  $A$  and distance between plates is  $d$ , then



$$C = \frac{\epsilon_0 A}{d}$$

When a dielectric slab of thickness  $t$  is placed between the plates, we have

$$C' = \frac{\epsilon_0 A}{d - t + \frac{t}{K}}$$

Given,  $C = 20\mu\text{F} = 20 \times 10^{-6}\text{F}$ ,

$$d = 2\text{mm} = 2 \times 10^{-3}\text{m}, t = 1\text{mm}$$

$$= 1 \times 10^{-3}\text{m}, K = 2$$

$$\therefore \frac{C'}{C} = \frac{d}{d - t\left(1 - \frac{1}{K}\right)} = \frac{2 \times 10^{-3}}{2 \times 10^{-3} - 1 \times 10^{-3}\left(1 - \frac{1}{2}\right)} = 1.33$$

$$\Rightarrow C' = 1.33 \times 20 \times 10^{-6} = 26.6 \mu\text{F}$$

19.

(b)

$$\vec{E}_1 = \frac{1}{4\pi\epsilon_0} \cdot \frac{2\vec{P}}{r^3} \text{ and}$$

$$\vec{E}_2 = -\frac{1}{4\pi\epsilon_0} \cdot \frac{\vec{P}}{(2r^3)} = -\frac{1}{4\pi\epsilon_0} \cdot \frac{\vec{P}}{8r^3}$$

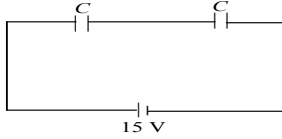
$$\Rightarrow \vec{E}_2 = -\frac{\vec{E}_1}{16}$$

(Here negative sign means direction)

20

(c)

Let capacitance of each capacitor is  $C$ .



Then equivalent capacitance in series is

$$\frac{1}{C'} = \frac{1}{C} + \frac{1}{C} = \frac{2}{C}$$

$$\Rightarrow C' = \frac{C}{2}$$

Charge  $Q = C'V = \frac{C}{2} \cdot 15 \quad \dots(i)$

When filled with dielectric

$$C_1 = 4C, C_2 = C$$

$$\frac{1}{C'} = \frac{1}{4C} + \frac{1}{C} = \frac{5}{4C}$$

$$\Rightarrow C' = \frac{4C}{5}$$

Since, charge is conserved

$$Q = C'V' = \frac{4C}{5}V' \quad \dots(ii)$$

From Eqs. (i) and (ii), we get

$$\frac{C}{2} \times 15 = \frac{4C}{5} \times V'$$

$$\Rightarrow V' = \frac{15 \times 5}{4 \times 2} = 9.4V$$

$$\approx 10V$$

PE

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	B	B	B	A	D	A	B	D	B	C
Q.	11	12	13	14	15	16	17	18	19	20
A.	C	A	A	D	B	D	B	B	B	C

PE