

### Topic :- Electric charges and fields

1 (c)

$$\frac{1}{C} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} \Rightarrow C = \frac{2}{3}F$$

2 (a)

By using  $\frac{1}{2}m(v_1^2 - v_1^2) = QV$

$$\Rightarrow \frac{1}{2} \times 10^{-3} [v_1^2 - (0.2)^2] = 10^{-8} (600 - 0)$$

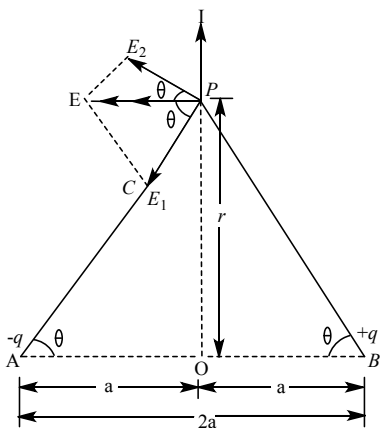
$$\Rightarrow v_1 = 22.8 \text{ cm/s}$$

3 (d)

Potential energy of dipole in electric field  $U = -PE \cos \theta$ ; where  $\theta$  is the angle between electric field and dipole

4 (a)

Consider an electric dipole consisting of two point charges  $-q$  and  $+q$  separated by a small distance  $AB = 2a$  with centre at  $O$ ,



As shown in figure, on equatorial line, the resultant electric field  $E$  of  $E_1$  and  $E_2$  is parallel to the axis of the dipole but opposite to the direction of the dipole moment  $p$  as it is

directed from negative charge to positive charge.

5 **(d)**

Number of electric transferred,  $n = \frac{q}{e}$   
 Mass transferred  $= m_e \times n = m_e \times \left(\frac{q}{e}\right)$   
 $= 9.1 \times 10^{-31} \times \left(\frac{2 \times 10^{-7}}{1.6 \times 10^{-19}}\right)$   
 $11.38 \times 10^{-19} \text{ kg}$

6 **(c)**

Electric force  $qE = ma \Rightarrow a = \frac{qE}{m}$   
 $\therefore a = \frac{1.6 \times 10^{-19} \times 1 \times 10^3}{9 \times 10^{-31}} = \frac{1.6}{9} \times 10^{15}$

$u = 5 \times 10^6$  and  $v = 0$

$\therefore$  From  $v^2 = u^2 - 2as \Rightarrow s = \frac{u^2}{2a}$

$\therefore$  Distance  $s = \frac{(5 \times 10^6)^2 \times 9}{2 \times 1.6 \times 10^{15}} = 7 \text{ cm. (approx)}$

7 **(c)**

Capacitance of a parallel plate capacitor with air is  $C = \frac{\epsilon_0 A}{d}$

Capacitance of a same parallel plate capacitor with the introduction of a dielectric medium

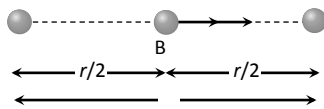
is  $C' = \frac{K \epsilon_0 A}{d}$  where  $K$  is the dielectric constant of a medium

$\Rightarrow \frac{C'}{C} = K$  or  $\frac{15}{3} = 5$  or  $K = \frac{\epsilon}{\epsilon_0}$

$\Rightarrow \epsilon = K \epsilon_0 = 5 \times 8.854 \times 10^{-12} = 0.4427 \times 10^{-10} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$

8 **(c)**

Initially, force between  $A$  and  $C$   $F = K \frac{Q^2}{r^2}$



When a similar sphere  $B$  having charge  $+Q$  is kept at the mid point of the line joining  $A$

and  $C$ , then Net force on  $B$  is  $F_{net} = F_A + F_C = k \frac{Q^2}{(r/2)^2} + \frac{kQ^2}{(r/2)^2} = 8 \frac{kQ^2}{r^2} = 8F$

9 **(d)**

If charge acquired by the smaller sphere is  $Q$  then it's

potential  $120 = \frac{kQ}{2} \dots(i)$

Whole charge comes to outer sphere

Also potential of the outer sphere

$$V = \frac{kQ}{6} \quad \dots(ii)$$

From equation (i) and (ii)  $V = 40 \text{ volt}$

10 **(d)**

$$C = \frac{\epsilon_0 A}{d} \text{ and } C' = \frac{\epsilon_0 A}{\left(d - \frac{d}{2} + \frac{(d/2)}{\infty}\right)} = \frac{2\epsilon_0 A}{d}$$

$$\Rightarrow C' = 2C$$

11 **(d)**

$$C_{air} = \frac{C_{medium}}{K} = \frac{C}{2}$$

12 **(a)**

From Gauss' theorem,

$$E \propto \frac{q}{r^2} \quad (q = \text{charge enclosed})$$

$$\frac{E_2}{E_1} = \frac{q_2}{q_1} = \frac{r_1^2}{r_2^2}$$

$$8 = \frac{\int_0^R (4\pi r^2) k r^a dr}{\int_0^{R/2} (4\pi r^2) k r^a dr} \times \frac{\left(\frac{R}{2}\right)^2}{(R)^2}$$

Solving this equation we get,  $a = 2$

PPE

14 **(d)**

There are 10 electrons and 10 protons in a neutral water molecule.

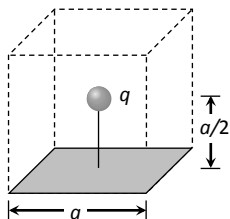
So it's dipole moment is  $p = q(2l) = 10 e (2l)$

Hence length of the dipole *i.e.* distance between centres of positive and negative charges is

$$2l = \frac{p}{10e} = \frac{6.4 \times 10^{-30}}{10 \times 1.6 \times 10^{-19}} = 4 \times 10^{-12} m = 4 \text{ pm}$$

15 **(d)**

An imaginary cube can be made by considering charge  $q$  at the centre and given square is one of it's face



- So flux from given square (*i.e.* one face)  $\phi = \frac{q}{6\epsilon_0}$
- 16 **(c)**  
 Let  $d$  be the distance between the plates and  $k$  be the dielectric constant. Without disconnecting the battery,  $V$  is the same  

$$E_0 = \frac{\sigma}{\epsilon_0}; V_0 = E_0 d; C_0 = \frac{Q}{V_0} = \frac{\epsilon_0 A}{d}$$
 With dielectric,  
 $V$  remains the same, capacitance increases,  $U$  which is energy stored ( $\frac{1}{2} CV^2$ ) increases;  
 $Q = CV$ , charge increases
- 17 **(a)**  
 The potential difference across the parallel plate capacitor is  $10V - (-10V) = 20V$   
 Capacitance  $= \frac{Q}{V} = \frac{40}{20} = 2F$
- 18 **(c)**  
 Common potential  $V = \frac{6 \times 20 + 3 \times 0}{(6 + 3)} = \frac{120}{9} \text{ Volt}$   
 So, charge on  $3 \mu F$  capacitor  

$$Q_2 = 3 \times 10^{-6} \times \frac{120}{9} = 40 \mu C$$
- 19 **(d)**  
 The surface of the conductor is an equipotential surface since there is free flow of electrons within the conductor. Thus potential at  $Q$  is the same as that at  $P$ . That is  $V_P = V_Q = V$ . The electric field  $E$  at a point on the equipotential surface of the conductor is inversely proportional to the square of the radius of curvature  $r$  at that point. That is  $E \propto r^{-2}$   
 Since point  $Q$  has a larger radius of curvature than that at point  $P$ , the electric field at  $Q$  is less than that at  $P$ . That is  $E_Q < E_P = E$

<b>ANSWER-KEY</b>										
<b>Q.</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>
<b>A.</b>	<b>C</b>	<b>A</b>	<b>D</b>	<b>A</b>	<b>D</b>	<b>C</b>	<b>C</b>	<b>C</b>	<b>D</b>	<b>D</b>
<b>Q.</b>	<b>11</b>	<b>12</b>	<b>13</b>	<b>14</b>	<b>15</b>	<b>16</b>	<b>17</b>	<b>18</b>	<b>19</b>	<b>20</b>
<b>A.</b>	<b>D</b>	<b>A</b>	<b>D</b>	<b>D</b>	<b>D</b>	<b>C</b>	<b>A</b>	<b>C</b>	<b>D</b>	<b>A</b>

**PE**