

Topic :- Dual nature of radiation and matter

- 2 (a)
According to Einstein's photoelectric equation

$$eV = hc \left[\frac{1}{\lambda} - \frac{1}{\lambda_0} \right]$$

1st case $3eV_s = hc \left[\frac{1}{\lambda} - \frac{1}{\lambda_0} \right]$... (i)

IInd case $eV_s = hc \left[\frac{1}{2\lambda} - \frac{1}{\lambda_0} \right]$... (ii)

Dividing Eq. (i) by Eq. (ii), we get
 $\lambda_0 = 4\lambda$

- 3 (d)
 K_{\max} of photoelectrons doesnot depend upon intensity of incident light.

4 (b)
 $\frac{\lambda_1}{\lambda_2} = \frac{h}{\frac{\sqrt{2mE}}{hc}} \quad \text{or} \quad \frac{\lambda_1}{\lambda_2} \propto E^{1/2}$

6 (b)
 $p = \frac{E}{c} = \frac{h\nu}{c}$

- 7 (d)
The mass of electron is about $\frac{1}{1836}$ times that of a neutron and angular momentum of electron is quantised in the hydrogen atoms but not the linear momentum of electron

8 (d)
 $h\nu - W_0 = \frac{1}{2}mv_{\max}^2 \Rightarrow \frac{hc}{\lambda} - \frac{hc}{\lambda_0} = \frac{1}{2}mv_{\max}^2$

$$\Rightarrow hc \left(\frac{\lambda_0 - \lambda}{\lambda \lambda_0} \right) = \frac{1}{2} m v_{\max}^2 \Rightarrow v_{\max} = \sqrt{\frac{2hc}{m} \left(\frac{\lambda_0 - \lambda}{\lambda \lambda_0} \right)}$$

When wavelength is λ and velocity is v , then

$$v = \sqrt{\frac{2hc}{m} \left(\frac{\lambda_0 - \lambda}{\lambda \lambda_0} \right)} \quad \dots(i)$$

When wavelength is $\frac{3\lambda}{4}$ and velocity is v' then

$$v' = \sqrt{\frac{2hc}{m} \left[\frac{\lambda_0 - (3\lambda/4)}{(3\lambda/4) \times \lambda_0} \right]} \quad \dots(ii)$$

Divide equation (ii) by (i), we get

$$\frac{v'}{v} = \sqrt{\frac{[\lambda_0 - (3\lambda/4)] \times \lambda \lambda_0}{\frac{3}{4} \lambda \lambda_0}} \times \frac{\lambda \lambda_0}{\lambda_0 - \lambda}$$

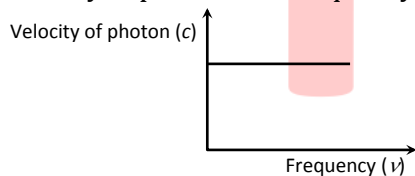
$$v' = v \left(\frac{4}{3} \right)^{1/2} \sqrt{\frac{[\lambda_0 - (3\lambda/4)]}{\lambda_0 - \lambda}}$$

$$i.e. v' > v \left(\frac{4}{3} \right)^{1/2}$$

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(a)

Velocity of photon (*i.e.* light) does not depend upon frequency. Hence the graph between velocity of photon and frequency will be as follows



10

(b)

$$\lambda_{\min} = \frac{hc}{eV} \Rightarrow \lambda_1 = \frac{hc}{eV_1} \text{ and } \lambda_2 = \frac{hc}{eV_2}$$

$$\therefore \Delta \lambda = \lambda_2 - \lambda_1 = \frac{hc}{e} \left[\frac{1}{V_2} - \frac{1}{V_1} \right]. \text{ Given } V_2 = 1.5 V_1$$

on solving we get $V_1 = 16000 \text{ volt} = 16 \text{ kV}$

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(a)

$$\lambda_{\min} = \frac{12375}{40 \times 10^3} = 0.309 \text{ \AA} \approx 0.31 \text{ \AA}$$

13

(a)

$$\text{Energy of photon, } E = h\nu = \frac{hc}{\lambda_{ph}}$$

where λ_{ph} is the wavelength of a photon $\lambda_{ph} = \frac{hc}{E}$

Wavelength of the electron, $\lambda_e = \frac{h}{\sqrt{2mE}}$

$$\therefore \frac{\lambda_{ph}}{\lambda_e} = \frac{hc}{E} \times \frac{\sqrt{2mE}}{h} = c \sqrt{\frac{2m}{E}}$$

14 **(b)**

For electron and positron pair production, minimum energy is 1.02 MeV

Energy of photon is given $1.7 \times 10^{-3} \text{ J} = \frac{1.7 \times 10^{-13}}{1.6 \times 10^{-19}}$

$$= 1.06 \text{ MeV}$$

Since energy of photon is greater than 1.02 MeV

So electron positron pair will be created

15 **(d)**

Velocity of photon $c = v\lambda$

16 **(d)**

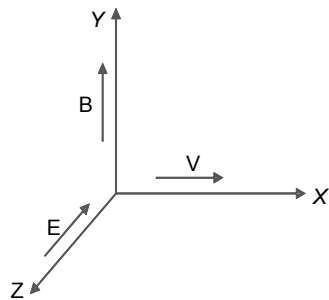
According to Einstein's equation

$$hv = W_o + K_{max} \Rightarrow V_o = \left(\frac{h}{e}\right)v - \frac{W_o}{e}$$

This is the equation of straight line having positive slope (h/e) and intercept on $-V_o$ axis, equal to $\frac{W_o}{e}$

18 **(a)**

The force on a particle is



So, $\mathbf{F} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$

or $\mathbf{F} = \mathbf{F}_e + \mathbf{F}_m$

$$\mathbf{F}_e = q\mathbf{E}$$

$$= -16 \times 10^{-18} \times 10^4 (-\hat{k})$$

$$= 16 \times 10^{-14} \hat{k}$$

and $\mathbf{F}_m = -16 \times 10^{-18} (10\hat{i} \times B\hat{j})$

$$= -16 \times 10^{-17} \times B (+\hat{k})$$

$$= -16 \times 10^{-17} B \times \hat{k}$$

Since, particle will continue to move along + x -axis, so resultant force is equal to 0.

$$\begin{aligned} \mathbf{F}_e + \mathbf{F}_m &= 0 \\ \therefore 16 \times 10^{-14} &= 16 \times 10^{-17} B \\ \Rightarrow B &= \frac{16 \times 10^{-14}}{16 \times 10^{-17}} = 10^3 \\ B &= 10^3 \text{Wb-m}^{-2} \end{aligned}$$

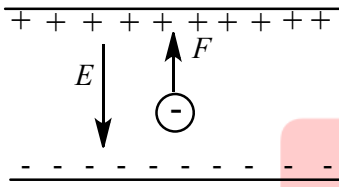
19 (c)

$$\begin{aligned} E &= hv/\lambda = \frac{hc}{e\lambda} \text{ (in eV)} \\ &= \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{1.6 \times 10^{-19} \times 0.21} = 5.9 \times 10^{-6} \text{ eV} \end{aligned}$$

20 (b)

Electric force (F) is straight forwarded, given by

$$F = qE$$



Where, q is charge and E is electric field.

$$\begin{aligned} \text{Given, } q &= 3e \\ \therefore F &= 3eE \quad \dots(i) \end{aligned}$$

From Newton's law, force experienced by a particle of mass $2m$ with acceleration a is

$$F = 2ma \dots(ii)$$

Equating Eqs. (i) and (ii) we get

$$\begin{aligned} 3eE &= 2ma \\ \Rightarrow a &= \frac{3eE}{2m} \end{aligned}$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	A	A	D	B	B	B	D	D	A	B
Q.	11	12	13	14	15	16	17	18	19	20
A.	C	A	A	B	D	D	A	A	C	B

PE