

Topic :- Dual nature of radiation and matter

1 (b)

The work function of sodium

$$W = \frac{hc}{\lambda}$$

$$W = \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{5 \times 10^{-7}}$$

or

$$W = 3.96 \times 10^{-19} \text{ J}$$

or

$$W = 2.47 \text{ eV} \quad (\because 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J})$$

or

$$W = 2.5 \text{ eV (approximately)}$$

2 (b)

$$p = \frac{h}{\lambda} = \frac{6.6 \times 10^{-34}}{0.01 \times 10^{-10}} = 6.6 \times 10^{-22} \text{ kg} \cdot \text{m/s}$$

4 (b)

If an electron and a photon propagates in the form of waves having the same wavelength, it implies that they have same momentum. This is according to de-Broglie equation

$$p \propto \frac{1}{\lambda}$$

6 (b)

Retarding potential,

$$V_s = \frac{hc}{\lambda e} - \frac{\phi_0}{e} = \frac{1240 \times 10^{-9}}{330 \times 10^{-9}} - 1.07$$
$$= 3.73 - 1.07 = 2.66 \text{ V}$$

7 (b)

$$K_{\max} = (h\nu - W_0); \nu = \text{frequency of incident light}$$

8 (c)

$$\lambda_{\min} = \frac{12375}{50 \times 10^3} \text{ \AA} = 0.247 = 0.25 \text{ \AA}$$

9 (c)

$$E_K - E_L = \frac{hc}{\lambda} = \frac{(6.6 \times 10^{-34})(3 \times 10^8)}{(0.021 \times 10^{-9})(1.6 \times 10^{-19})} \text{ eV} = 59 \text{ KeV}$$

10 (a)

$$\text{Maximum KE} = E - \phi_0 = 3.4 - 2 = 1.4 \text{ eV}$$

11 (a)

The cut-off wavelength λ_{\min} corresponds to an electron transferring (approximately) all of its energy to an X-ray photon, thus producing a photon with the greatest possible frequency and least possible wavelength.

From relation

$$\begin{aligned} \lambda_{\min} &= \frac{hc}{K_0} \\ &= \frac{(4.14 \times 10^{-15})(3 \times 10^8)}{35.0 \times 10^3} \\ &= 3.55 \times 10^{-11} \text{ m} = 35.5 \text{ pm} \end{aligned}$$

12 (d)

de-Broglie wavelength

$$\lambda = \frac{h}{\sqrt{2mE}}$$

$$\begin{aligned} \therefore \frac{\lambda_1}{\lambda_2} &= \sqrt{\frac{E_2}{E_1}} \Rightarrow \frac{1 \times 10^{-9}}{0.5 \times 10^{-9}} = \sqrt{\frac{E_2}{E_1}} \\ \Rightarrow 2 &= \sqrt{\frac{E_2}{E_1}} \Rightarrow \frac{E_2}{E_1} = 4 \end{aligned}$$

$$\therefore E_2 = 4E_1$$

$$\begin{aligned} \therefore \text{Energy to be added} &= E_2 - E_1 \\ &= 4E_1 - E_1 = 3E_1 \end{aligned}$$

13 (c)

We know that

$$qE = mg$$

$$\frac{qQ}{\epsilon_0 A} = mg \text{ or } q = \frac{\epsilon_0 A mg}{Q}$$

$$= \frac{8.85 \times 10^{-12} \times 2 \times 10^{-2} \times 2.5 \times 10^{-7} \times 10}{5 \times 10^{-7}} \text{ C}$$

$$= 8.85 \times 10^{-13} \text{ C}$$

15 (b)

For an electron

$$\text{Mass, } m_e = 9.11 \times 10^{-31} \text{ kg}$$

Kinetic energy, $K = 10eV = 10 \times 1.6 \times 10^{-19}J$

de Broglie wavelength, $\lambda_e = \frac{h}{\sqrt{2m_eK}}$... (i)

For the person Mass, $m = 66kg$

Speed, $v = 100kmhr^{-1} = 100 \times \frac{5}{18}ms^{-1}$

de Broglie wavelength, $\lambda = \frac{h}{mv}$... (ii)

Dividing (i) by (ii), we get

$$\begin{aligned}\frac{\lambda_e}{\lambda} &= \frac{h}{\sqrt{2m_eK}} \times \frac{mv}{h} = \frac{mv}{\sqrt{2m_eK}} \\ &= \frac{66 \times 100 \times \frac{5}{18}}{\sqrt{2 \times 9.11 \times 10^{-31} \times 10 \times 1.6 \times 10^{-19}}} = 1.07 \times 10^{27}\end{aligned}$$

17 (b)

$$\lambda = \frac{h}{mv} = \frac{h\sqrt{1-v^2/c^2}}{m_0v} = 0 \quad (\because v = c)$$

18 (b)

$$\begin{aligned}\text{Slope of } V_0 - v \text{ curve} &= \frac{h}{e} \\ \Rightarrow h &= \text{Slope} \times e = 1.6 \times 10^{-19} \times 4.12 \times 10^{-15} \\ &= 6.6 \times 10^{-34}J\cdot s\end{aligned}$$

19 (b)

The wavelength range of X-ray is $0.1 \text{ \AA} - 100 \text{ \AA}$

20 (b)

$$qV = \frac{1}{2}mv^2 \text{ or } v = \sqrt{2qV/m} \text{ ie, } v \propto \sqrt{V}$$

ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	B	B	B	B	C	B	B	C	C	A
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	D	C	D	B	A	B	B	B	B

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